

تَلْيِيْص

lab phsics 1

لاب فیزیک ۱



Calculating error & uncertainty :-

1. Percent error.

الفرق بين القيمة المُعْتَدلة والقيمة التجريبية هي نسبة المُرْتَبطة بالقيمة التجريبية ونُوِّهُ بها في المنهجيات باسم percent error.

$$* \text{percent error} = \frac{|E - A|}{|A|} * 100\%.$$

$E \in \pi$

E: experimental value (قيمة التجربة)

A: accepted value. (قيمة المُعْتَدلة)

* when A (accepted value) is not known we calculate:-

2. Percent difference.

$$\text{Percent diff.} = \frac{|E_2 - E_1|}{\frac{(E_2 + E_1)}{2}} * 100\%$$

* for 3 or more measurements:

Percent diff. = absolute difference between the extreme values
avg

* Average or (mean) value (\bar{x}):-

$$\bar{x} = \frac{x_1 + x_2 + x_3 + \dots + x_n}{n} = \frac{1}{n} \sum_{i=1}^N x_i$$

لما يُمْكِن إيجاد مُقدمة لـ \bar{x} من المُعْتَدلة

غير

(d) standard deviation

$$d_i = x_i - \bar{x}$$

الفرق بين

القيم المُعْتَدلة والقيم التجريبية

$$\sigma = \sqrt{\frac{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}{n}}$$

$$= \sqrt{\frac{d_1^2 + d_2^2 + \dots + d_n^2}{n}}$$

* when we have a small number of measurements
it's better to use:-

$$\delta = \sqrt{\frac{d_1 + d_2 + \dots + d_n}{n-1}}$$

∴ we can use standard deviation σ to calculate the precision or error in the mean of a group set of measured values.

$$\text{error in } \bar{x} = \frac{\delta}{\sqrt{n}} = \sqrt{\frac{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}{n(n-1)}}$$

مقدار الخطأ في المعدل

* هذا القانون يستخدم لمعرفة قيمة الخطأ المعيارية في المعدل أو الزاوية ... ،

* يعين القسم مثل الكثافة تفاصيل أدوات القياس سعة ادواتها مقدرة وسادوي
نصف اصغر حراوة يتبعها؛ قراءتها.

$$\text{مثال: } \text{نصف اصغر حراوة } 0.01 \text{ g}$$

$$\therefore \text{error} = \Delta m = \pm 0.005 \text{ g}$$

* يعين القسم الضروري لعمليات الحساب على قيم معيارية مطلوبة

$$V = \frac{\pi D^2 H}{4}$$

* Rules \Rightarrow قواعد معاينة

$$1. R = x + y \quad \text{or} \quad R = x - y$$

$$\Delta R = \sqrt{(\Delta x)^2 + (\Delta y)^2}$$

x, y are measured values

$$2. R = x * y \quad \text{or} \quad R = x / y$$

$$\Delta R = R \sqrt{\left(\frac{\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2}$$

$\frac{\Delta R}{R}$ = fractional error

$$3. R = x^n$$

$$\frac{\Delta R}{R} = n \left(\frac{\Delta x}{x} \right) \Rightarrow \Delta R = n R \left(\frac{\Delta x}{x} \right)$$

Experiment #1:-

* Purpose:- ١) العلاقة بين t (فترة النضج في قدر الارتفاع) و h (عمق الماء)
٢) قانون مطرد مع الزمن

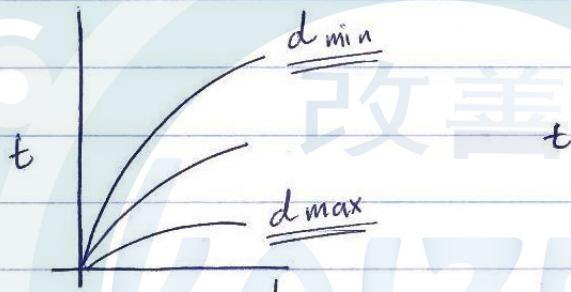
→ Relation

$$t \propto \frac{1}{d^2} \quad (\text{معكوس})$$

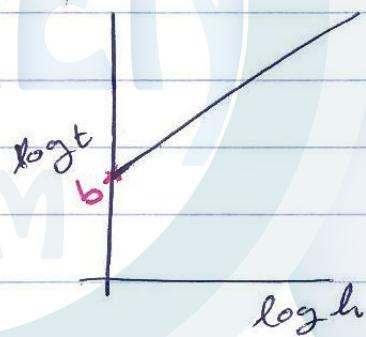
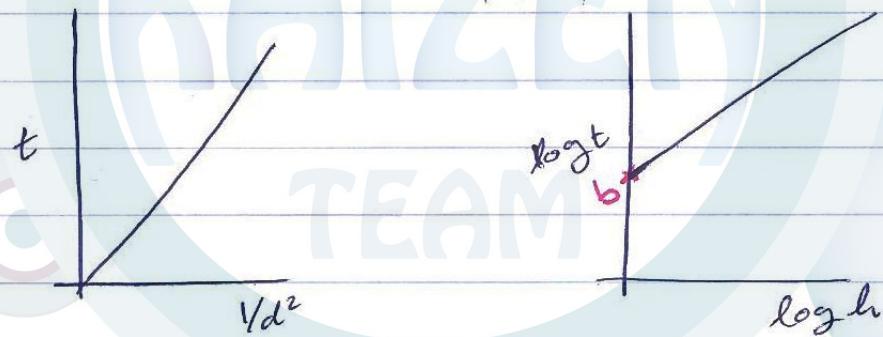
$$\log t \propto \log h \quad (\text{معكوس})$$

Independent variable: d, h (المتغيرات المستقلة)
dependent variable: t (المتغير النابع ...)

graphs



(non-linear & inverse relation).



$$[\text{Slope}] = \frac{S}{m^2} = [S \cdot m^2]$$

$$= C h_0^\alpha$$

$$b = \log(C d_0^\beta)$$

$$[\text{Slope}] = [\alpha] = \left(\frac{S}{cm}\right)$$

$$t(d, h) = C h^\alpha d^\beta \rightarrow \text{constants!}$$

① constant $d : d = d_0$

$$t = (C d_0^\beta) h^\alpha \dots \textcircled{1}$$

$$t = C' h^\alpha$$

$$\log t = \underbrace{\log C'}_{\text{constant}} + \log h^\alpha$$

$$\log t = C_2 + \alpha \log h$$

y x

y-intercept slope

$$y = b + \alpha x \rightarrow b = \log C'$$

$$C' = 10^b$$

$$\alpha = \alpha$$

$$b = \log(d_0^\beta C)$$

$$\text{plug in } \textcircled{1} : t = 10^b \ln(\alpha) \rightarrow \text{slope}$$

② h constant $h : h = h_0$

$$t = (C h_0^\alpha) d^\beta$$

$$t = \underbrace{C'}_{\text{Slope}} d^\beta \quad \boxed{\beta = -2} \Rightarrow t \propto \frac{1}{d^2} \Rightarrow t \propto d^{-2}$$

$$b = 0.85 / \alpha = 0.52 / \beta = -2 / Ch_0^\alpha = 166.67$$

$$t = 10^{0.85} h^{0.52}$$

Experiment #2:-

- purpose:- - Measure length, and mass the use it to
 Calculate volume, & density.
 - Calculate the value of (π)

→ Procedure:- - Calculate value of π using a disk!

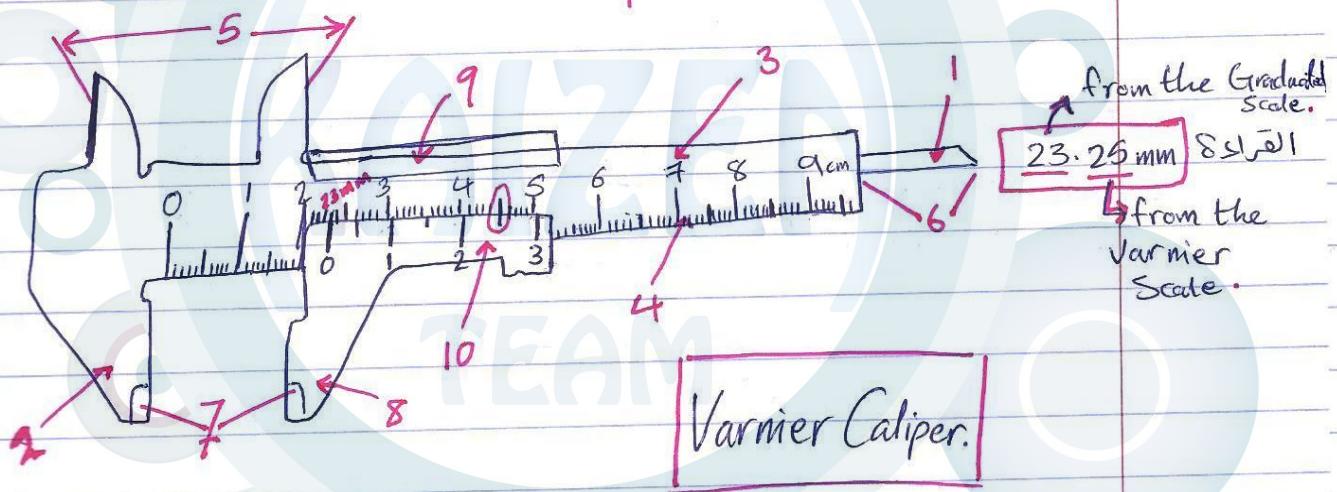
$$C = \pi d$$

C: Circumference of the disk.

→ Can be measured using **Vernier Paper tape**
 & meter stick.

d: ~~radius~~ diameter of the disk.

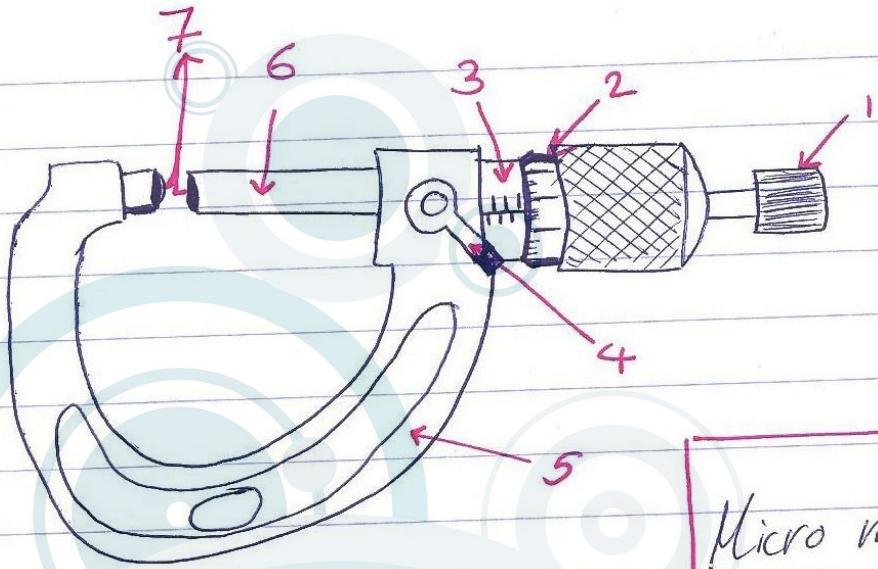
→ Can be measured using **Vernier Caliper**.



- 1 Depth measurement.
- 2 Fixed jaw blade.
- 3 Guide bar.
- 4 Graduated Scale.
- 5 knife-edge measuring faces for inside measurements.
- 6 Measuring faces for Depth measurement.
- 7 Measuring faces for Outside measurement.
- 8 Movable jaw blade.
- 9 Slide.
- 10 Vernier.

$$\text{error in measurement} = \pm 0.025\text{mm}$$

(0.05mm लम्बाई से ज्यादा)



Micro meter.

1 - ratchet knob.

2 - Thimble (Varnier Scale).

3 - main / Graduated Scale.

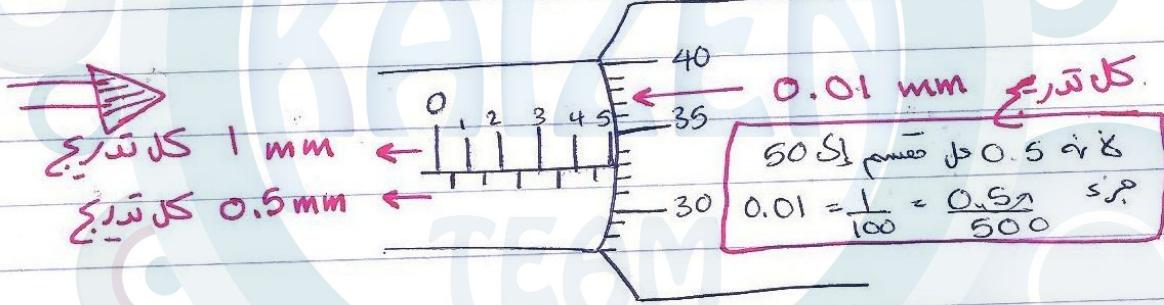
4 - lock.

5 - frame

6 - Spindle

error = ± 0.005 mm

7 - Anvil.



$\frac{\text{exp}}{\# 2}$

- Calculating density of Brass P:-

$$\rho = \frac{m}{V} \rightarrow V = h * \pi (d/2)^2$$



m:- mass; data measured using Pan Balance

$$\Delta m \rightarrow \text{error} = \pm 0.005 \text{ g}$$

h:- length of the rod; measured using Vernier Caliper

$$\Delta h \rightarrow \text{error} = \pm 0.05 \text{ mm}$$

d:- diameter \approx measured using Micrometer

$$\Delta d \rightarrow \text{error} = \pm 0.01 \text{ mm}$$

Calculating errors:-

* Stage # 1 (calculating π)

(diameter) 1. $\bar{d} = \frac{d_1 + d_2 + \dots + d_n}{n}$

2. $\Delta \bar{d} = \pm \sqrt{\frac{(d_1 - \bar{d})^2 + (d_2 - \bar{d})^2 + \dots + (d_n - \bar{d})^2}{n(n-1)}}$

3. $d = \bar{d} \pm \Delta \bar{d}$

repeat the same steps for (C)

(π) 4. $\bar{\pi} = \frac{\bar{c}}{\bar{d}}$

5. $\Delta \bar{\pi} = \bar{\pi} \sqrt{\left(\frac{\Delta \bar{d}}{\bar{d}}\right)^2 + \left(\frac{\Delta \bar{c}}{\bar{c}}\right)^2}$

6. $\pi = \bar{\pi} \pm \Delta \bar{\pi}$

7. which value error contributes most to π .

we calculate $\left(\frac{\Delta \bar{d}}{\bar{d}}\right)^2$ & $\left(\frac{\Delta \bar{c}}{\bar{c}}\right)^2$ and the higher value

contribute most to π .

$3.14 \approx \text{للميل}(للميلان)$

8. Calculate experimental error = $\left| \frac{\pi_{\text{measured}} - \pi_{\text{known}}}{\pi_{\text{known}}} \right| * 100\%$

Stage #2 (calculating ρ)

$$1. \Delta m = \pm 0.005 \text{ g}$$

$$2. \bar{h} = h = \frac{h_1 + h_2 + \dots + h_n}{n} + \sqrt{\frac{(h_1 - \bar{h})^2 + (h_2 - \bar{h})^2 + \dots + (h_n - \bar{h})^2}{n(n-1)}}$$

$$3. d = \bar{d} + \Delta \bar{d}$$

$$4. \bar{\rho} = \frac{m}{\bar{h} \times \pi (\bar{d}/2)^2}$$

$$5. \Delta \bar{\rho} = \bar{\rho} \sqrt{\left(\frac{\Delta m}{m}\right)^2 + \left(\frac{\Delta \bar{h}}{\bar{h}}\right)^2 + \left(\frac{\Delta \pi}{\pi}\right)^2 + \left(\frac{2 \Delta \bar{d}}{\bar{d}}\right)^2}$$

from stage #1

$$6. \rho = \bar{\rho} \pm \Delta \bar{\rho}$$

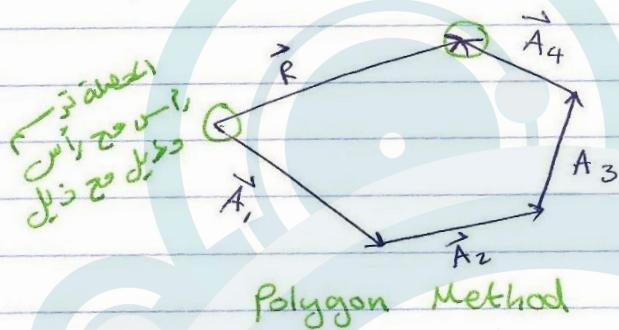
Experiment #3:- Vectors (Force Table).

→ Purpose:- to calculate resultant force using:-

- 1) graphical
- 2) experimental
- 3) Algebraical

methods.

A) Graphical Method:



* we should use a convenient scale.

* $|\vec{R}|$ is determined using a ruler
→ direction of \vec{R} is determined using protractor.

→ magnitude should be multiplied by the chosen scale factor.

B) Method of Components (~~Algebraic~~ Algebraic)

$$\vec{A}_{x_i} = |\vec{A}_i| \cos \theta_i \hat{i}$$

$$\vec{A}_{y_i} = |\vec{A}_i| \sin \theta_i \hat{j}$$

$$\vec{A}_x = \sum_i^n \vec{A}_{x_i} \hat{i}$$

$$\vec{A}_y = \sum_i^n \vec{A}_{y_i} \hat{j}$$

$$|\vec{R}| = \sqrt{(A_x)^2 + (A_y)^2}$$

$$\theta = \tan^{-1} \left(\frac{A_y}{A_x} \right)$$

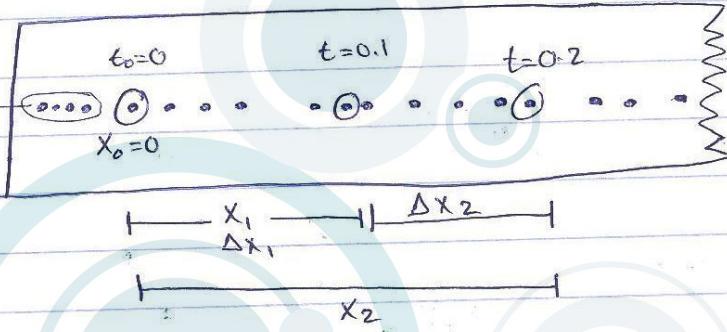
c) Experimental Method (Force table).

⇒ (from manual)

Experiment #4: kinematic of rectilinear motion.

→ Purpose:- Study irregular motion (made by hand).

The first few dots are neglected



→ ticker timer marks a dot on the ticker tape each $(1/50)$ s
so we take every 5 dots to represent (0.1) s.

$$\rightarrow \text{Average Speed } \bar{v}_i = \frac{\Delta x_i}{\Delta t} = \frac{\Delta x_i}{0.1} \text{ cm/s}$$

$$\rightarrow \text{Average Acceleration } \bar{a}_i = \frac{\Delta v_i}{\Delta t} = \frac{\Delta v_i}{0.1} \text{ cm/s}^2$$

نقطة \bar{v}_i هي $\frac{1}{(0.1)}$ امتيازات في Δx \Rightarrow Δx \rightarrow $x_{0.1}$ *

From $t = 0 \rightarrow 0.1$ s \therefore \bar{v}_i

$$\Delta x_1 = 5.9 \text{ cm}$$

$$\therefore \bar{v}_i = 5.9 / 0.1 = 59 \text{ cm/s}$$

$$v_{\text{instantaneous}} \text{ at } t = 0.05 = 5.9 / 0.05 = 118 \text{ cm/s}$$

$$\therefore v_{\text{inst}} = \bar{v}_{\text{avg}} \text{ at } t = 0.05$$

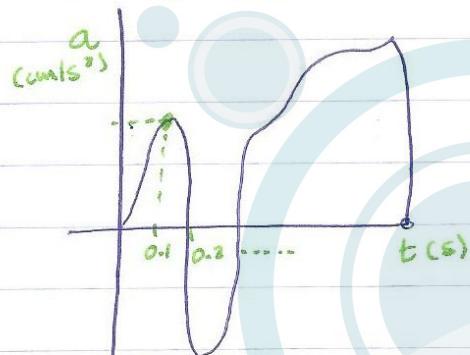
$$\bar{v}_{2-10} / \bar{v}_{3-9} / \bar{v}_{4-8} / \bar{v}_{5-7}$$

النقطة \bar{v}_{2-10}

$$\bar{v}_{a-b} = \frac{x_b - x_a}{\Delta t} \times (x_0 \text{ no available})$$

* V is highest when spaces between dots are longest & vice versa.

→ Graphs



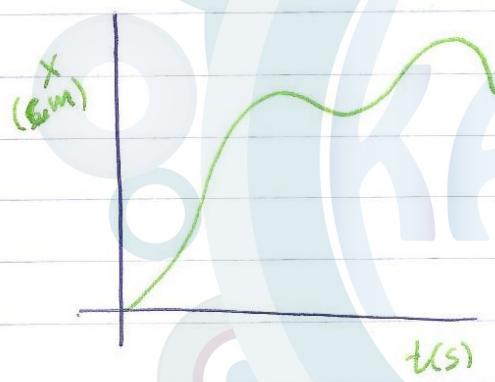
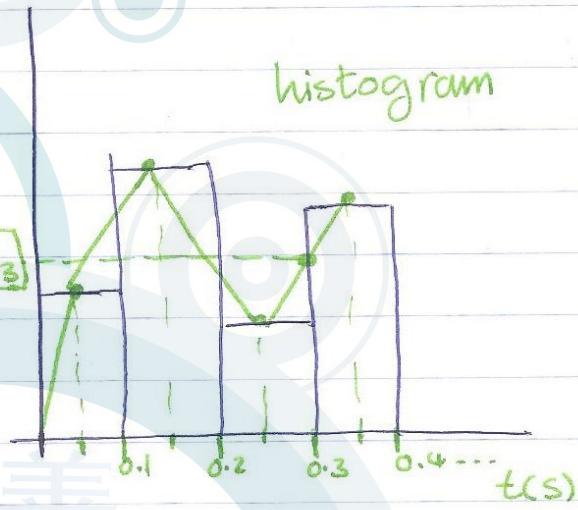
$$\dots 0.260.1 = t \text{ ins } \alpha \text{ ms}$$

$$\bar{a}_{\text{avg}} = \Delta v_i / \Delta t \\ (v_{i+1} - v_i) / \Delta t$$

\checkmark (cm/s)

$V_{0.3}$

histogram



slope of tangent line at $t = a$
 $= V(a)_{\text{ms}}$

Experiment 6:- collision in two dimensions.

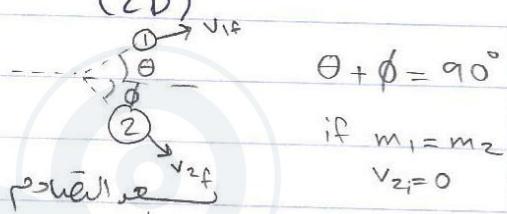
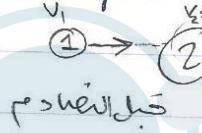
* Purpose :- to prove the conservation of momentum by simulating 2D elastic collision.

* Introduction :-

Collisions

↳ head-on collision (1D) *موجة في اتجاه واحد*

↳ Oblique \rightarrow (2D)



→ from momentum conservation:-

$$(\vec{P}_1)_i + (\vec{P}_2)_i = (\vec{P}_1)_f + (\vec{P}_2)_f$$

$$m_1 \vec{v}_{1i} + m_2 \vec{v}_{2i} = m_1 \vec{v}_{1f} + m_2 \vec{v}_{2f} \quad \dots \text{if } m_1 = m_2$$

$$\vec{v}_{1i} + \vec{v}_{2i} = \vec{v}_{1f} + \vec{v}_{2f} \quad \dots \textcircled{1}$$

→ in an elastic collision:-

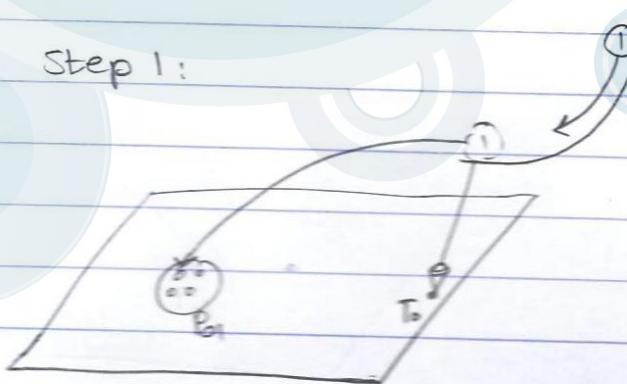
$$K.E_i = K.E_f$$

$$\frac{1}{2} m_1 v_{1i}^2 + \frac{1}{2} m_2 v_{2i}^2 = \frac{1}{2} m_1 v_{1f}^2 + \frac{1}{2} m_2 v_{2f}^2$$

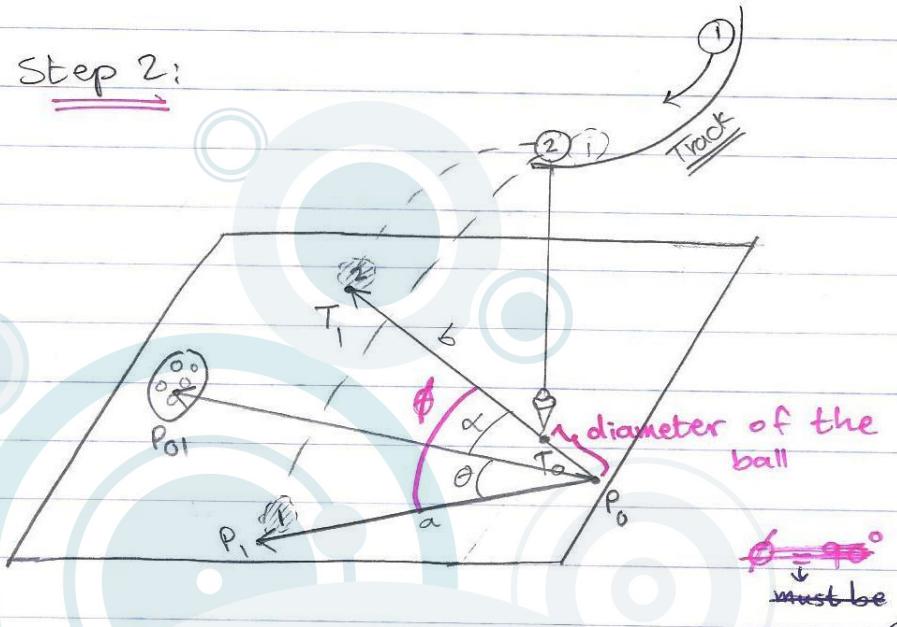
$$v_{1i}^2 + v_{2i}^2 = v_{1f}^2 + v_{2f}^2 \quad \textcircled{2}$$

التجربة تزداد أثمنة تأثير طرق كل من ① و ② حفظ *
• (elastic) potential energy

Step 1:



Step 2:



$p_{01} \equiv$ momentum before collision $\equiv (v_{i1} + v_{i2}) = v_i$
 (projectile) ball 1

$p_0 p_1 + T_0 T_1 \equiv$ momentum after collision $\equiv (v_{f1} + v_{f2})$
 Projectile (1) target (ball 2)

momentum after collision (p_f)

الآن نحسب الموجات المترافقه

$$p_0 p_1 + T_0 T_1$$

$p_0 p_1$ و $T_0 T_1$ هما الموجات المترافقه

$p_i \approx p_f \therefore$ momentum is conserved

from ② before after

$$(v_{i1})^2 \stackrel{?}{=} (v_{f1})^2 + (v_{f2})^2$$

K.E conservation

$$(p_0 p_1)^2 \stackrel{?}{=} (p_0 p_1)^2 + (T_0 T_1)^2$$

$$(p_0 p_1)^2 \approx (p_0 p_1)^2 + (T_0 T_1)^2$$

\therefore K.E is conserved

& the collision is elastic

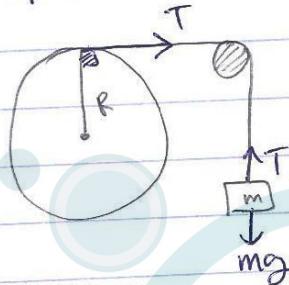
$\phi_A = 90^\circ$ because collision is elastic & $m_1 = m_2$ &
 $v_2 = 0$

$$\phi = \alpha + \theta \rightarrow T_{0T} \text{ & } P_{0P} \text{ مع المروج}$$

$$\text{Percent error} = \left| \frac{\phi - \phi_A}{\phi_A} \right| * 100\%$$

Experiment #7: Rotational motion:

* Purpose:- (I: moment of inertia), law -



$$\text{II) } F = ma$$

$$mg - T = ma$$

$$T = m(g - a) \quad \dots \textcircled{1}$$

¶

$$\boxed{2} \quad \vec{T} = \vec{r} \times (\vec{F}) = I \times \alpha \rightarrow \alpha = a/R$$

$$TR = I\alpha$$

from \textcircled{1}

$$m(g - a)R = I\alpha$$

$$(m(g - aR)R = I\alpha)/\alpha$$

$$mR(\frac{g}{\alpha} - R) = I$$

$$\boxed{I = m(gR - R^2)}$$

* if we have $\alpha, m, R \rightarrow$ we can find I

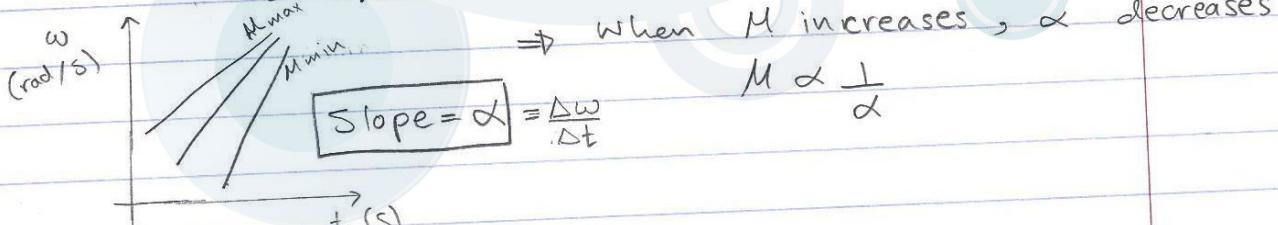
Part 1:-

variable:- M (mass of the disk)

-: اكتفاء

* نقوم بقياس المربعة $\Delta \omega$ لـ ω في قرارات مختلفة لـ M (M) \rightarrow α \propto M $\dots \textcircled{1}$

الفرق ونجد العلاقة بين ω و M \rightarrow ω \propto M^{-1}



\Rightarrow When M increases, α decreases

$$M \propto \frac{1}{\alpha}$$

$\omega \propto t$
linear, direct
relation

مُنْعَلٌ مُؤْخَذٌ مُنْعَلٌ (القانون) moment of inertia $\leftarrow I$ always \textcircled{C}

$$I = \frac{m}{\text{const.}} \left(\frac{\alpha R - R^2}{2} \right)$$

const. = disk radius.
variable

$$\Rightarrow M \propto \frac{1}{\alpha} \propto I$$

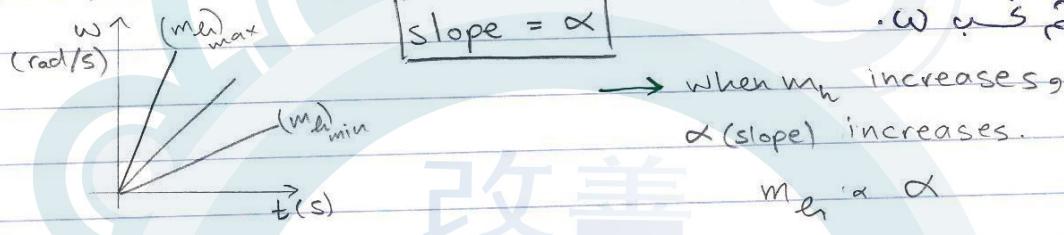
$[I] = \text{g.cm}^2$

Part # 2 :-

variable:- m_h (hanging mass)

أكْثَرَانِ :- *

نَقْوَمٌ يَابِنُ الْمُنْعَلِ الْمُؤْخَذِ لِلْمُنْعَلِ الْمُؤْخَذِ (القانون) ①

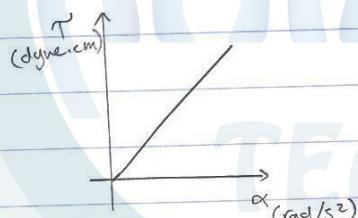


نَقْوَمٌ يَابِنُ τ (القانون) \textcircled{C}

$$\tau = I \alpha$$

$$\tau = R m (g - \alpha R)$$

$$[\tau] = (\text{dyne.cm})$$



كَيْفَيَةُ سَبَقِ الْمُنْعَلِ خِلَالِ الْمُنْعَلِ (القانون) \rightarrow I نَقْوَمُ بِاسْتِهْنَامِ قَانُونِ اِلْمُنْعَلِ

قيمة لـ I في دور فريدة ومحضية

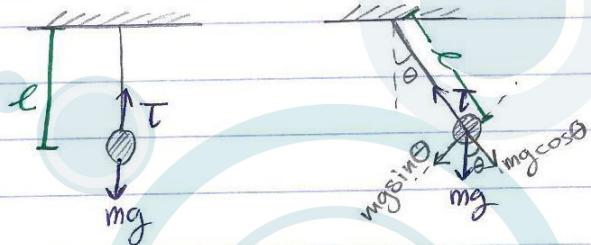
$$\text{Percent difference} = \frac{|I_1 - I_2|}{(I_1 + I_2)/2} \times 100\%$$

Experiment #8: Simple harmonic motion (simple pendulum).

*Purpose: ابره ساده موج دارای مبدأ ملائمه و موج دارای مبدأ ملائمه

$$(l \propto T^2) / (l \propto \frac{1}{T})$$

العلاقة بين
الزوج المدحبي (النرخ) \rightarrow لـ طبل السيرول
نطحه دوران واحد



$$F_r = \frac{mv^2}{r} \quad (\text{أيضاً})$$

$$T - mg \cos \theta = \frac{mv^2}{l} \quad \dots \textcircled{1}$$

$$F_{\text{tangential}} = mg \sin \theta \quad \dots \textcircled{2}$$

$$* T(l) = 2\pi \sqrt{\frac{l}{g}}$$

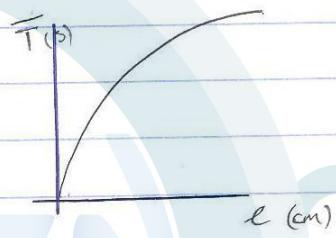
T: period of oscillation (s)

l: length of the pendulum (m)

$$T^2 = \frac{4\pi^2 l}{g}$$

constant = slope

$\therefore T^2 \propto l$ (direct, linear relation) \rightarrow



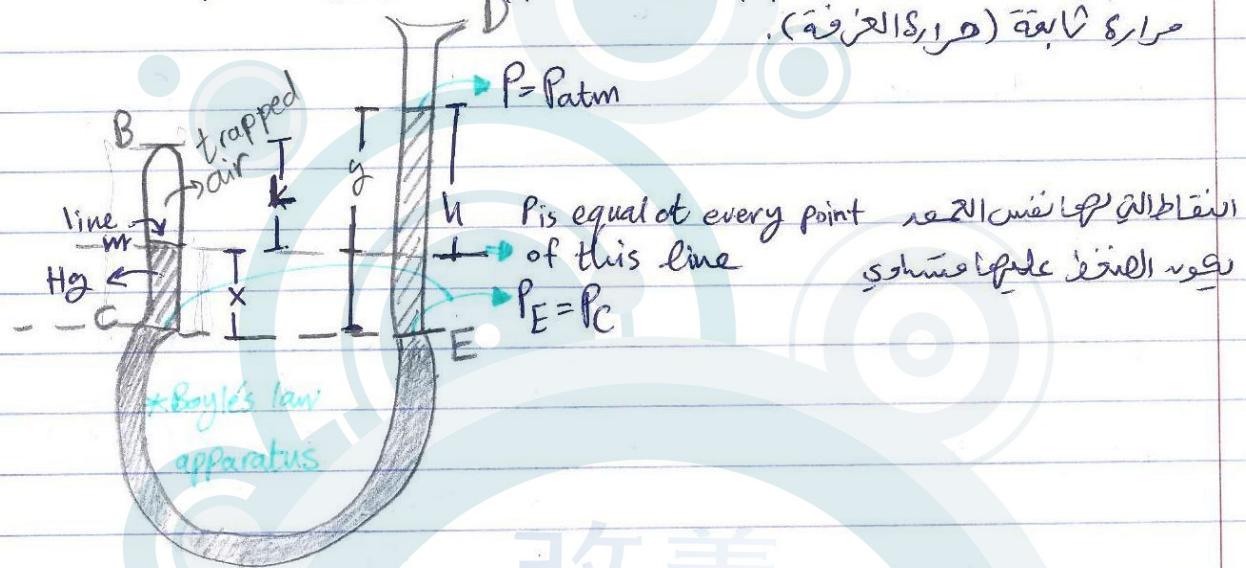
$$\text{slope} = \frac{4\pi^2}{g}$$

$$\therefore g = \left(\frac{4\pi^2}{\text{slope}} \right) = E \quad \xrightarrow{\text{experimental value}}$$

$$\text{Percent error in } (g) = \left| \frac{E - A}{A} \right| * 100\% \quad A = 980 \text{ cm/s}^2$$

Experiment 9:- The laws of gases:-

* purpose :- ان اقصى الصلة بين الضغط والحجم (أعلى درجة من التوصيل)
 اعني (الجهاز) Volume الحجم و pressure الضغط
 صراحتاً (هذا العرض).



* Boyle's law:-

Part 1:- we have constant quantity of trapped gas at constant temp.
 P_f (pressure) and V (volume) are variables (for the trapped air)

$$[P] = \text{pascal}$$

$$P_{\text{fluid}} = \frac{W}{A} = \frac{mg}{A} = \frac{\rho V g}{A} = \rho g h$$

$$\boxed{P = \rho g h}$$

ρ : density

at the line 'm'

$$(P_{\text{gas, right}} = P_{\text{atm}} + \rho_{\text{Hg}} g h) / \rho_{\text{Hg}} g$$

the right side the left side

$$\frac{P_g}{\rho_{\text{Hg}} g} = h + \frac{P_{\text{atm}}}{\rho_{\text{Hg}} g}$$

$$P_g = h + P_{\text{atm}} \quad \dots \text{①}$$

في آخر BC على (I) و DE على (II) ملحوظ
 ملحوظ DE وبشكل ملحوظ.

• X, Y على DE هي جزء من DE على (II) *

(mm Hg) دالة كثافة الهواء

(BG) مع ثابتة PE لارتفاع مئوية للأبخرة في سعر X,Y

$$l = B - x \quad \text{constant}$$

طبل عمود الغاز الماء

$$h = y - x$$

الفرق في طبل عمود الزيت

from ideal gas law

* $P \cdot V = \text{constant}$

$$P = \frac{\text{const.}}{V}$$

$$P = \frac{\text{const.}}{Ae}$$

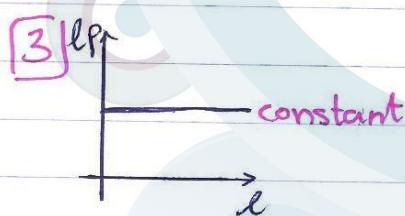
$$P = \text{const.} \cdot \frac{1}{e}$$

$$\therefore P \propto \frac{1}{e}$$

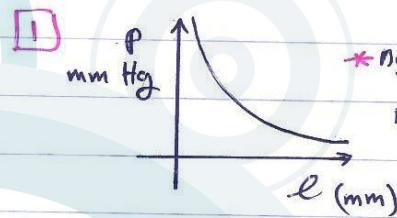
Plug in (1) ...

$\Delta h_{\text{up}} = h - h_0$ slope $y\text{-intercept}$

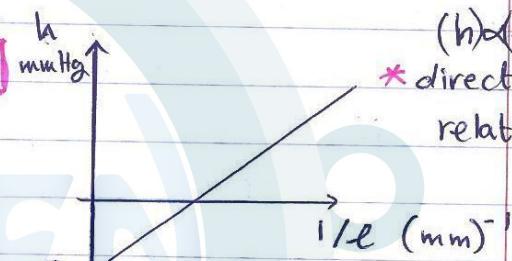
$$h = (\text{const.}) \cdot \frac{1}{e} (-P'_{\text{atm}})$$



(at the same temperature)



* Non linear, inverse relation



$(h) \propto \left(\frac{1}{e}\right)$
* direct, linear relation

Experiment # 11: Specific heat capacity

→ specific heat capacity (C)

$$*[C] = \text{cal}/(\text{g} \cdot \text{c}^\circ)$$

$$\text{Heat capacity} = m C = [\text{cal}/\text{c}^\circ]$$

$$\text{Heat} = Q = m \underset{\substack{\uparrow \\ \text{constant}}}{C} \Delta T \Rightarrow \text{Heat} = m \Delta T, \text{ if } C \text{ is constant}$$

*Note:- (1 cal = 4.18 Joules)

\Rightarrow heat absorbed by one part of a system = heat lost by the other part of the same system

$$Q_{\text{gained by water}} = Q_{\text{lost by brass}}$$

$$m_w C_w \frac{\Delta T}{w} + m_c C_c \frac{\Delta T}{c} = m_b C_b \frac{\Delta T}{b}$$

$\hookrightarrow T_f - T_i$ $\Delta T_c = \Delta T_w$ $|T_b - T_f|$

T_i = initial temperature of water + calorimeter.

T_f = \approx \approx brass.

T_f = equilibrium temperature.

$$\text{let } x = \Delta T_w = \Delta T_c$$

$$y = (m_w C_w + m_c C_c)$$

$$z = \Delta T_b$$

$$\therefore y x = m_b C_b z$$

$$\therefore C_b = \frac{yx}{zm_b} \dots \text{①}$$

error in $C_b = \Delta C_b$

$$\Delta C_b = C_b \sqrt{\left(\frac{\Delta y}{y}\right)^2 + \left(\frac{\Delta x}{x}\right)^2 + \left(\frac{\Delta z}{z}\right)^2 + \left(\frac{\Delta m}{m}\right)^2}$$

$$\Delta x = \sqrt{(\Delta T)^2 + (\Delta t)^2} = \sqrt{2} \Delta T$$

$$\Delta y = \sqrt{(\Delta m_w)^2 + (\Delta m_d)^2}$$

$$\Delta z = \sqrt{2} \Delta T \quad (\text{بشكل فراغت / بغير جو})$$

$$\Delta m = \pm \frac{\text{نوع الماء}}{2} = \pm 0.005 \text{ g}$$

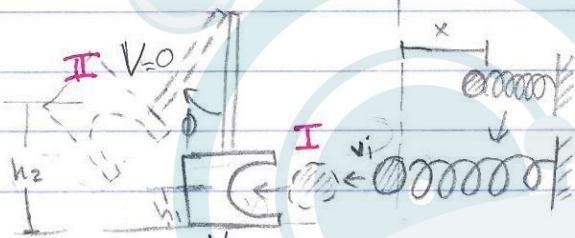
* possible sources of error:-

* (1) energy (heat) lost with the surroundings.

(2) error in readings by the observer.

Experiment 12 : Ballistic Pendulum.

* Purpose:- *to investigate the law of conservation of energy*



\rightarrow Potential $E_p = \text{Kinetic } E_f$

$$\frac{1}{2} K x^2 = \frac{1}{2} m V_f^2 \quad \dots \textcircled{1}$$

$$V_f = \sqrt{\frac{K x^2}{m}} \quad \textcircled{2}$$

* after ball is captured by the pendulum, we can calculate their speed using the conservation of momentum & energy.

$$P_{initial} = P_f \rightarrow \text{conservation}$$

$$m V_i = V (m + M_{tot}) \quad \dots \textcircled{3}$$

m: mass of the ball

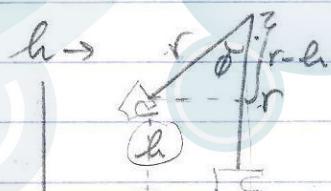
M_{tot} : total mass of the pendulum

$$* K.E_I = P.E_{II} \quad (\text{II is at the maximum height, } V=0 \rightarrow K.E=0)$$

$$\frac{1}{2} (m+M) V^2 = (m+M_{tot}) g \Delta h$$

$$V = \sqrt{\frac{2gr(1-\cos\phi)}{h}}$$

$$\therefore \text{from } \textcircled{3} \quad V = \frac{m+M}{m} \sqrt{2gr(1-\cos\phi)}$$



$$\cos\phi = \frac{r-l}{r} = 1 - \frac{l}{r}$$

$$\therefore l = (1 - \cos\phi)r$$

Procedure:-

* Part 1:- سُبَيْتِ الْمَوَاهِبِ الْجَنَاحِيَّةِ الْمُبَدِّدِ حَتَّى تَغْسِيرِ الْأَرْزَاقِ -

② $V = \sqrt{\frac{kx^2}{m}}$ when x increases V increases.
Non-linear relation $x \propto v$

* Part 2:- سُبَيْتِ الْأَرْزَاقِ الْجَنَاحِيَّةِ خَشْبَنْدِ الْأَنْجَانِ الْمُبَدِّدِ -

• مَا دَعَى

صُمَدَ الْقَانُونَ

$$V = \frac{m+M}{m} \sqrt{2gr(1-\cos\phi)}$$

$$V^2 = \left(\frac{m+M}{m}\right)^2 (2gr(1-\cos\phi))$$

$$\therefore \frac{1-\cos\phi}{y} = \frac{V_i^2}{2gr} \left(\frac{m}{m+M}\right)^2 x$$

slope = α
constants

V : no x in m^2
Part 1



$$y = \alpha x$$

$$(1-\cos\phi)\alpha = \left(\frac{m}{m+M}\right)^2$$

direct - linear relation.

Since ... slope = $\frac{V_i^2}{2gr}$

$$\therefore g = \frac{V_i^2}{2r \times \text{slope}} = E \quad \begin{matrix} \leftarrow \\ \text{experimental value} \end{matrix}$$

$$\text{Percent error in}(g) = \left| \frac{E-A}{A} \right| * 100\% \quad A = 9.80 \text{ m/s}^2$$