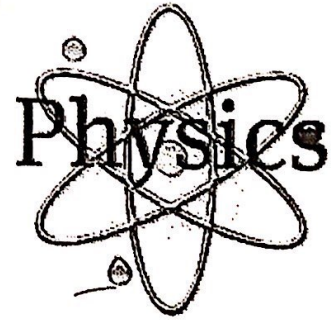


# تلخيص لاب فيزياء 1

شرح التجارب + حل جميع  
أسئلة السنوات

للطالبة: ضحى صالح  
بقلم الطالبة: هديل محمود

engine\_team



www.clipartof.com • 43224

الجامعة الهاشمية + الأردنية

# Name of Experiment 8

Exp 1: Collection and Analysis of Data

Exp 2: Measurement and Uncertainties

Exp 3: Vectors & Force Table

Exp 4: Kinematics of Rectilinear Motion

Exp 5: Force and motion

Exp 6: Collision in Two dimensions

Exp 7: Simple harmonic motion . simple pendulum

Exp 8: The Behavior of Gases with changes in Temp. and pressure

Specific heat Capacity of metals.

\* بالإنجليزية :

Experimental Error and Data Analysis. ( اخطاء )

المقال الذي عن دكتور د. وهذا على بشرى في حال وجود  
(أ) (أشياء أخرى) (أشياء) بذلك على صفحتي على الـ Facebook

Physicist Doha



# Introduction

القديم...

engine\_team

Experimental Error  
and data Analysis.

ملاحظة: يجب دراسة جميع مفاهيم ثم التوصل للتجارب.

# physics

## Lab (1)

### Experimental Error and data Analysis: المقدمة



#### Empirical relations

مهم جداً

دائماً يأتي سؤال  
على العديد من الفيزيائيين على شكل  
#

لحريته هل سؤال إيجاد العلاقة الرياضية:

1 نغذي في معادلة الخط المستقيم

$$y = mx + b$$

$y$ : الشئ الموجود للرمز على محور الصادات

$x$ : الشئ (الرمز) الموجود على محور السينات

$m$ :

slope

الميل  $\rightarrow$

$$\frac{\Delta y}{\Delta x}$$

تغير الصادات

تغير السينات

$b$ :  $y$ -int  $\Rightarrow$  التقاطع مع محور الصادات

" $L_n$ "  $\Rightarrow e$  في حالة الـ

" $\log$ "  $\Rightarrow 10$  في حالة الـ

□ □

نضع أساس

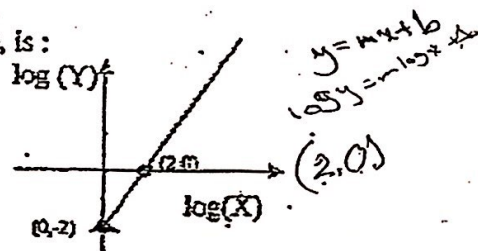


3. نظرًا إلى أن  $10^x$   $\log(x)$   $(+)$   $(X)$  \* قول الجمع إلى في  
 $(\frac{0}{0})$  \* قول الطرح إلى  $(-)$   $(\frac{0}{0})$

(48)

2) The empirical relation which describes the plotted curve, is:

- a)  $Y = 100X$
- b)  $Y = 2X$
- c)  $Y = X/100$
- d)  $Y = 100 - X^2$



\* نكتب حسب الصيغة

Solution :

$$y = mx + b$$

$$\log y = \text{slope} * \log(x) + (-2)$$

\* نكتب إجمال slope:  $\frac{y_2 - y_1}{x_2 - x_1}$  من النسبة أي نقطتين

$$\frac{(0, -2)}{(x_1, y_1)} / \frac{(2, 0)}{(x_2, y_2)}$$

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - (-2)}{2 - 0} = \frac{2}{2} = 1$$

نعوّض في المعادلة  $\Rightarrow \log y = 1 \log x - 2$

نضع الأساس 10 للطرفين  $\Rightarrow \log_{10} y = \log_{10} x - 2 \Rightarrow 10^{\log y} = 10^{\log x - 2}$

$$y = \frac{10^{\log x}}{10^2}$$

$$\Rightarrow y = \frac{x}{100}$$

هذا هو الجواب

9

Ex 2: Which of following empirical relations describes the plotted curve in Fig. 1:

\* Solution :

$$y = mx + b$$

$$m \rightarrow \text{slope} \Rightarrow \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - 3}{1 - 0} = \frac{-3}{1} = -3$$

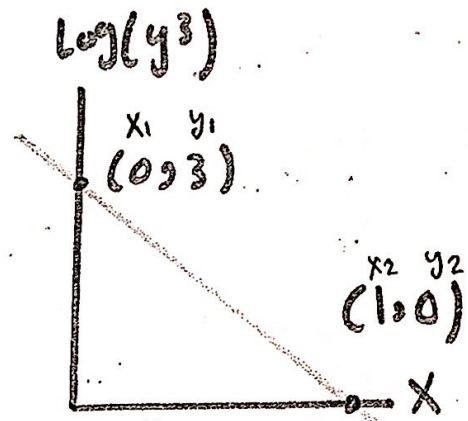


Fig. 1

$$\Rightarrow y = mx + b$$

$$\text{Log } y^3 = -3x + 3$$

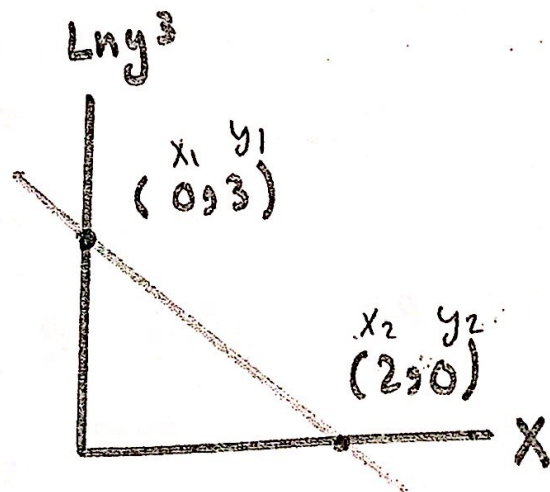
$$\Rightarrow 10^{\text{Log } y^3} = 10^{-3x+3} \Rightarrow y^3 = 10^{-3x} * 10^3 \Rightarrow \sqrt[3]{y^3} = \sqrt[3]{\frac{10^3}{10^{3x}}}$$

$$\Rightarrow y = \frac{10}{10^x}$$

Ex B: Find the empirical relation describes the plotted Curve in fig 2 "

Solution :

$$* \text{ Slope} \Rightarrow m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - 3}{2 - 0} = \frac{-3}{2}$$



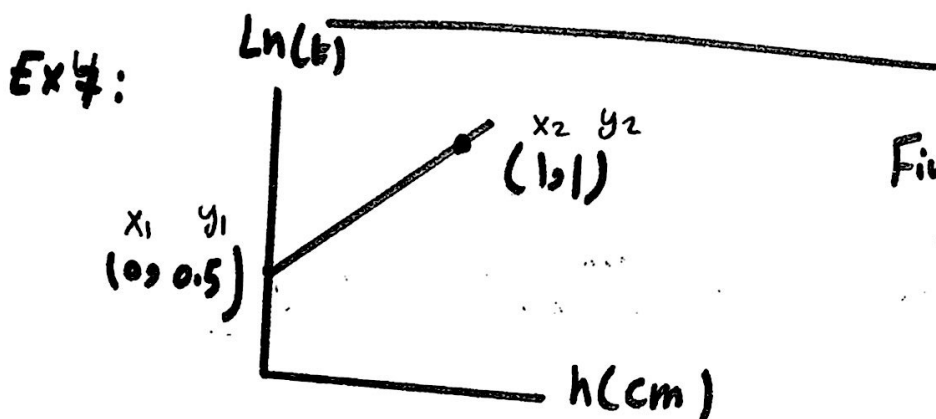


$$\Rightarrow y = mx + b$$

$$\ln y^3 = -\frac{3}{2}x + 3$$

$$\Rightarrow e^{\ln y^3} = e^{3 - \frac{3}{2}x} \Rightarrow y^3 = \frac{e^3}{e^{\frac{3}{2}x}} \Rightarrow \text{نصف العنبر السعير للفرصة} \Rightarrow$$

$$y = \frac{e}{e^{\frac{x}{2}}} \Rightarrow y = e * e^{-x/2}$$



Find the empirical relation: ?!

Solution 8 \* slope =  $\frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 0.5}{1 - 0} = 0.5$

\*  $y = mx + b$

$$\ln(t) = 0.5h + 0.5$$

\*  $e^{\ln(t)} = e^{0.5h + 0.5}$

\*  $t = e^{0.5h} * e^{0.5}$

$$\Rightarrow t = e^{0.5h} * 1.643$$

Ex 8: 2. Given that  $y = \sqrt[3]{x}$ , where  $y$  and  $x$  are variables. If you plot  $\log(y)$  versus  $\log(x)$  to get a straight line, then the  $y$ -intercept will be:

(a) 3  
(b) 1/3

(b) 1  
(c) zero

\* solution:  $y = \sqrt[3]{x}$

$$\Rightarrow \Rightarrow y = x^{\frac{1}{3}}$$

نبدخل اللوغاريتم على الطرفين

$$\Rightarrow \log y = \log x^{\frac{1}{3}}$$

$$\Rightarrow \log y = \frac{1}{3} \log x$$

المطلوب في السؤال :  $y$ -intercept

نقارن المعادلة في الأعلى مع معادلة الخط المستقيم

$$* y = mx + b$$

$$* \log y = \frac{1}{3} \log x + 0$$

$$\boxed{b=0}$$

العبار Zero

Ex 8 2- Given that  $(Z = kx^n)$  where  $k$  and  $n$  are constants. If you plot  $(\log Z)$  versus  $(\log x)$  to get a straight line, then the  $y$ -intercept is:

المطلوب في السؤال : خط  $y$

$$Z = kx^n$$

(b)  $k$

a)  $\log n$

(d)  $\log k$

c)  $n$

$$\log Z = \log(kx^n)$$

$$\log Z = \log k + n \log x$$

y-intercept      slope

15



2

$$R \pm \Delta R$$

رأياً يأتي عليه سؤال على المبدأ  
وسؤال على القائل #

فصل (5) حالات وإيادها سيتم توضيح كل حالة وطرح أسئلة المسائل  
ذكر منها:

1 حالة الفرق والعسمة = جون وعلى علاقة في السؤال مع القيم وليس فقط.

2 حالة طرح وجمع لخطيات

3 حالة الجمع - حالة وجود (خطي) بطرف وجمع أو طرح (وقوة) بطرف آخر

أو وجود (قوة) أو ضرب وقسمة في حدين يفصل بينهم جمع أو طرح

4 حالة حفظ القوانين

5 اظهار على تجارب

سيتم توضيح كل حالة

\* الحالة الأولى :

✓ جون مطبوعاً على علاقة فيها ضرب أو قسمة أو ضرب مع قسمة مع أنس.

✓ لكي نعوام على إياد  $R$  نقو في مباشرة في العلاقة

✓ لكي نجد  $\Delta R$  نطبق على القانون التالي :

$$\Delta R = R \sqrt{\left(\frac{F_1 \Delta x}{x}\right)^2 + \left(\frac{F_2 \Delta y}{y}\right)^2 + \dots}$$

$R$ : وهي القيمة التي أوجدناها

$F_1$  = قوة المتغير الأول

$\Delta x$  = نسبة الخطأ للمتغير  $x$

$x$  = قيمة المتغير.

6

Ex 7]

6- Calculation of errors:

If  $R = XY^3$

$X \pm \Delta X = 2 \pm 0.03$

$Y \pm \Delta Y = 1.5 \pm 0.01$

find  $R \pm \Delta R =$

Solution  $\Rightarrow \boxed{R} = XY^3 \Rightarrow R = (2) * (1.5)^3 = 6.75$

$\Rightarrow \Delta R = R \sqrt{\left(\frac{f_1 \Delta x}{x}\right)^2 + \left(\frac{f_2 \Delta y}{y}\right)^2} = 6.75 \sqrt{\left(\frac{1 * 0.03}{2}\right)^2 + \left(\frac{3 * 0.01}{1.5}\right)^2}$

$\boxed{\Delta R} = 0.16875$

$\Rightarrow R \pm \Delta R = 6.75 \pm 0.16875$

Ex 8]

If  $z = x^3/y$ , where  $x$  and  $y$  measured in the experiment, then the uncertainty in  $z$  is:

(a)  $\Delta z = \sqrt{\left(\frac{3\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2}$

(c)  $\Delta z = z \sqrt{3\left(\frac{\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2}$

~~(b)  $\Delta z = z \sqrt{\left(\frac{3\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2}$~~   
(d)  $\Delta z = z \sqrt{\left(\frac{\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2}$

$z = x^3/y \Rightarrow \Delta z = z \sqrt{\left(\frac{3 * \Delta x}{x}\right)^2 + \left(\frac{1 * \Delta y}{y}\right)^2}$

لـ الحـالـة الـأولـى

$\Rightarrow \underline{b}$

الـجـواب

engine\_team



Please circle the correct answer:

- 1) Given that  $R = 2XY - 5$ , and  $X \pm \Delta X = 2.3 \pm 0.1$ ,  $Y \pm \Delta Y = 6.5 \pm 0.1$ , then the value of  $\Delta R / R$  is equal to:
- a) 0.05      b) 1.38      c) 0.69      d) 0.09

$$R = 2xy - 5$$

ملاحظة هذا السؤال ينحل في الحالة الأولى ولا يستر  
هذه حالات الدرع الآن العوض في الطرف الآخر هو ثابت (5)

$$\Delta R / R \Rightarrow$$

$$\Delta R = R \sqrt{\left(\frac{F_1 \Delta x}{x}\right)^2 + \left(\frac{F_2 \Delta y}{y}\right)^2}$$

نقسم الطرفين على R

$$\Rightarrow \frac{\Delta R}{R} = \sqrt{\left(\frac{1 * 0.1}{2.3}\right)^2 + \left(\frac{1 * 0.1}{6.5}\right)^2} = 0.046 \approx 0.05$$

الجواب a

\* ملاحظة إذا جُل في السؤال حساب R فنحسب بالطريقة الثانية :

$$\Rightarrow R = 2xy - 5$$

$$\Rightarrow R = 2 * (2.3) (6.5) - 5$$

$$\Rightarrow R = 24.9$$

engine\_team

حالة الثانية: مائع مع طرفي الخطأ :

\* إذا كان المطلوب  $R \pm \Delta R$

مكثت المعادلة المعطاة في السؤال:  $R = F_1 A - F_2 B$  (طرح أو جمع)

لأنه يعرف مباشرة المعادلة  $R \pm \Delta R$   $\Delta R = \sqrt{(F_1 \Delta A)^2 + (F_2 \Delta B)^2}$

دائماً مع نفس القواعد المعادلة الرئيسية

علافت: هذه الحالة لم ترد عليها أسئلة سنوات لنا سيتم ذكر مثال للتوضيح فقط:

$x \pm \Delta x = 3 \pm 0.03$

$y \pm \Delta y = 6 \pm 0.1$

$R = 6x - y$

Find  $R \pm \Delta R$ :

$R = 6x - y$

$\Rightarrow R = 6 * (3) - 6 = 18 - 6 = 12$

$\Rightarrow \Delta R = \sqrt{(6 * 0.03)^2 + ((-1) * 0.1)^2} = 0.2$

$12 \pm 0.2$

الحالة الثالثة: حالة الجمع: - وجود خطي في طرف (وقوة أو ضرب وقوة) خاطئ آخر يفصل + أو

وجود قوة أو ضرب وقوة في طرف يفصل بينهما جمع أو طرح:

في حالة الجمع دائماً نتحقق بالتدقيق حتى نرجع المسألة للحالات السابقة ذكرها.

Given that  $R = 6x - \frac{2y}{z^2}$  with  $x \pm \Delta x = 3 \pm 0.03$ ,  $y \pm \Delta y = 6 \pm 0.1$  and  $z \pm \Delta z = 9 \pm 0.05$  then  $\Delta R$  equals:

a) 0.81  
b) 0.18

b) 2.87

c) 3.22

\*  $\Delta R ??$  المطلوب

$$R = 6x - \frac{2y}{z^2}$$

مشتقة مع قوتها

على  $z$

\* : امنا في حالة  $\frac{y}{z^2}$  (حالة الدمج) :

\* دائماً في كل هذه النوع من المسائل نبدأ بالفرض بحيث اننا نرجع مسألتنا الى الحالة الاولى

$$R = 6x - \frac{2y}{z^2}$$

$$B = \frac{y}{z^2}$$

نأخذ  
بالمقام

هون نتوجد  $B \pm \Delta B$  (هي في الحالة الاولى)

$$\Rightarrow B = \frac{y}{z^2} \Rightarrow \text{هنا في الحالة الاولى}$$

$$B = \frac{6}{(9)^2} = \frac{6}{81} = 0.074$$

$$\Delta B = B \sqrt{\left(\frac{1 * \Delta y}{y}\right)^2 + \left(\frac{2 * \Delta z}{z}\right)^2}$$

$$\Delta B = 0.074 \sqrt{\left(\frac{0.1}{6}\right)^2 + \left(\frac{2 * 0.05}{9}\right)^2}$$

$$\Delta B = 0.001$$

$$B \pm \Delta B = 0.074 \pm 0.001$$

نتج

\* نضع للمعادلة الاصلية



$$*R = 6x - 2\frac{y}{z^2}$$

$$\Rightarrow R = 6x - 2\beta \Rightarrow \text{معدل دقة للبيان (2)}$$

$$R = 6 * (3) - 2 * (0.074)$$

$$R = 17.852$$

$$\Delta R = \sqrt{(6\Delta x)^2 + (2\Delta \beta)^2} = \sqrt{(6 * 0.03)^2 + (2 * 0.01)^2} = \underline{\underline{0.18}}$$

$$\boxed{\Delta R = 0.18} \rightarrow \text{الجواب C}$$

الحالة الرابعة : حالة حفظ القوانين

نستعمل طرق القوانين المطلوبة ومن ثم حل أسئلة عليها :

□ For a sphere:

$$\textcircled{1} V = \frac{4}{3} \pi r^3 \equiv V = \frac{4}{3} \pi \left(\frac{d}{2}\right)^3$$

•  $V$ : Volume (الحجم)

توضيح الرموز:

•  $r$ : Radius (نصف القطر)

•  $d$ : diameter (القطر)

$$\textcircled{2} \rho = \frac{m}{V} \equiv \rho = \frac{3m}{4\pi r^3} \equiv \rho = \frac{6m}{\pi d^3}$$

•  $\rho$ : density (الكثافة)

توضيح الرموز:

•  $m$ : mass (الكتلة)

•  $V$ : Volume (الجمع)

•  $r$ : Radius (نصف)

$$\textcircled{3} A = 4\pi r^2$$

Area radius

(مساحة)

□  $d$ : diameter (القطر)

$$\boxed{V = \pi h r^2 \equiv V = \pi h \left(\frac{d}{2}\right)^2}$$

$d$ : diameter

$$\boxed{2} \quad c = \pi \cdot d$$

والقصر عما علا

$$\boxed{3} \quad \rho = \frac{m}{V} = \frac{4m}{hT_d^2}$$

$$\boxed{4} A_t = 2\pi r (h + r)$$

انونا المسافة الكلية  
للاسلو اننا

3 momentum (

الزخم  $\Rightarrow$  momentum = Velocity \* mass  
الزخم = السرعة \* الكتلة .

4] Cube:  $V = A^3$   
Volume

## Volume

طوبى الفضل

حجج المكعب = (طول الضلع)<sup>3</sup>

6 circle / disk

$$c = \pi d$$

$$A = \pi \left( \frac{d}{2} \right)^2$$

$$V_{\text{disk}} = \pi h \left(\frac{d}{2}\right)^2$$

5 square:  $C = 4(A)$   
معطى الكرب

محبوبہ الکریمہ

طوبى للأفام

$$\left\{ \begin{array}{l} A = \frac{(R)^2}{(\text{معدل الفلج})^2} \\ \text{اعلاقة} \end{array} \right.$$

12) A student measures the length of a cube side to be  $3.4 \pm 0.1$  cm, then the volume of the cube  $V \pm \Delta V$  (in  $\text{cm}^3$ ) will be:

a)  $39.3 \pm 5.55$       b)  $79.5 \pm 5.55$       c)  $79.5 \pm 3.47$       d)  $39.3 \pm 3.47$

**Solution:**

الحالة الرابعة : لينة كعلاقة راضية :

Cube  $\rightarrow V = A^3 \Rightarrow V \pm \Delta V$

$$V = A^3$$

$$V = (3.4)^3$$

$$V = 39.3 \text{ cm}^3$$

$$\Delta V = V \sqrt{\left(\frac{F \Delta A}{A}\right)^2} = 39.3 \sqrt{\left(\frac{3 \times 0.1}{3.4}\right)^2} = \boxed{3.468}$$

Ex 13]

3. A student measures the following dimensions for a cylindrical rod. He found that the diameter and height of rod;  $(6.2 \pm 0.01 \text{ mm})$  and  $(15.3 \pm 0.01 \text{ cm})$ , respectively. If the mass of rod is  $(16.36 \pm 0.01 \text{ g})$ , then the value of  $\Delta \rho / \rho$  will be:

(a) 0.033  
(b) 0.003

(c)  $0.847 \times 10^{-3}$   
(d)  $9.347 \times 10^{-3}$

Solution:

هذا السؤال على الطريقة  $\Delta$  لأننا أعطينا علاقة  $\Delta$  بالخطأ النسبي

Cylinder

$$\frac{\Delta \rho}{\rho} \text{ والسائل}$$

$$\rho = \frac{4m}{\pi d^2 h}$$

$$\Delta \rho = \rho \sqrt{\left(\frac{1 \times \Delta m}{m}\right)^2 + \left(\frac{1 \times \Delta h}{h}\right)^2 + \left(\frac{2 \times \Delta d}{d}\right)^2}$$

$$\Rightarrow \frac{\Delta \rho}{\rho} = \sqrt{\left(\frac{1 \times 0.01}{16.36}\right)^2 + \left(\frac{1 \times 0.01}{15.3}\right)^2 + \left(\frac{2 \times 0.01}{6.2}\right)^2}$$

$$\Rightarrow \frac{\Delta \rho}{\rho} = 3.347 \times 10^{-3} = 0.00334 \approx \boxed{0.003}$$

الجواب

ملاحظة مهمة جداً:  $\Delta$  البان  $\pm$  3.14 يتم اعتبارها ثابتة كما في عدد اذا لم نعطها قيمة لها في السؤال على شكل error أما اذا أعطى  $\Delta$   $\pm$   $\Delta$  نحسب تغيره ونعطي في قايومه  $\Delta$   $\pm$   $\Delta$  ...

Ex 14]

3. The diameter, height and mass of a cylinder are  $d = (0.610 \pm 0.005) \text{ cm}$ ,  $h = (11.3 \pm 0.1) \text{ cm}$  and  $m = (16.83 \pm 0.01) \text{ g}$ , respectively. The density ( $\rho \pm \Delta \rho$ ) (in  $\text{g/cm}^3$ ) of the cylinder is:

a)  $5.099 \pm 0.061$   
b)  $5.099 \pm 0.095$

c)  $5.644 \pm 0.068$   
d)  $5.644 \pm 0.105$

Solution: cylinder  $\Rightarrow \rho \pm \Delta \rho$ ??

$$\rho = \frac{4m}{\pi d^2 h} = \frac{4 \times 16.83}{11.3 \times 3.14 \times (0.610)^2} = 5.0988 \approx 5.099$$

$$\Delta \rho = \rho \sqrt{\left(\frac{1 \times 0.01}{16.83}\right)^2 + \left(\frac{1 \times 0.1}{11.3}\right)^2 + \left(\frac{2 \times 0.005}{0.610}\right)^2} = 0.095$$

الجواب



15

In order to determine the area of circular disc, a student measured the diameter ( $d$ ) to be  $3.2 \pm 0.1 \text{ cm}$ . The value of  $A \pm \Delta A$  (in  $\text{cm}^2$ ) will be:

(a)  $8.04 \pm 0.50$   
(c)  $4.15 \pm 0.36$

(b)  $4.15 \pm 0.50$   
(d)  $8.04 \pm 0.36$

$$A_{\text{disk}} = A_{\text{circle}}$$

$$\Rightarrow A = \pi \left( \frac{d}{2} \right)^2 \Rightarrow A = \pi \left( \frac{3.2}{2} \right)^2 = 8.0384$$

$$\Rightarrow \Delta A = A \sqrt{\left( \frac{2 \Delta d}{d} \right)^2} \Rightarrow 8.0384 \sqrt{\left( \frac{2 \times 0.1}{3.2} \right)^2} = 0.5024$$

$$A \pm \Delta A \Rightarrow 8.0384 \pm 0.5$$

فرع ٩

الطريقة الثانية : الطريقة التجريبية :

إذا أنكل السؤال حدة تجريبية و  $R \pm \Delta R$

$$R \Rightarrow R = \left( \frac{\text{مجموع القيم}}{\text{عدد القيم}} \right) \quad * \text{خذ المتوسط الحسابي}$$

$$\Delta R \Rightarrow \sqrt{\frac{\sum_{n=1}^N (R - \bar{R})^2}{N(N-1)}}$$

$\bar{R}$  : المتوسط الحسابي

$R_0$  : أحد القيم من السؤال

$N_0$  : عدد مرات إيراد القيمة

$\sum$  : مجموع

14

Ex 16

7) A series of measurements made to determine  $\pi$ . The results were: 3.11, 3.12, 3.13, 3.14 and 3.15. The value of  $\pi \pm \Delta\pi$  will be:

- a)  $3.14 \pm 0.007$  b)  $3.13 \pm 0.006$  c)  $3.14 \pm 0.006$  d)  $3.13 \pm 0.007$

\* هذا السؤال على الحالة الخاصة لأنك أعطيت دقة خارج

$$\pi \pm \Delta\pi \quad ??$$

$$\Rightarrow \pi = \frac{\sum \text{القيم}}{N} = \frac{3.11 + 3.12 + 3.13 + 3.14 + 3.15}{5} = 3.13$$

$$\Rightarrow \Delta\pi = \sqrt{\frac{\sum_{n=1}^N (\pi - \bar{\pi})^2}{N(N-1)}}$$

$$\Rightarrow \Delta\pi = \sqrt{\frac{(3.11 - 3.13)^2 + (3.12 - 3.13)^2 + (3.13 - 3.13)^2 + (3.14 - 3.13)^2 + (3.15 - 3.13)^2}{5(5-1)}}$$

$$\Rightarrow \Delta\pi = 7.071 \times 10^{-3} = 0.007$$

$$\Rightarrow \pi \pm \Delta\pi = (3.13 \pm 0.007) \quad \underline{\underline{= \text{الجواب}}}$$

4- Five measurements of the volume of object are (3.15, 3.2, 3.16, 3.18, 3.15) the mean value of the volume (V) is:

d) 3.15

(c) 3.17

b) 3

a) 3.16

$$\text{Solution 8 } V = \frac{3.15 + 3.2 + 3.16 + 3.18 + 3.15}{5} = 3.168 \approx 3.17$$

A- Five measurements of the volume of a disk (diameter, d and thickness, t) were made. Let the fractional errors in d and t be A (i.e.  $A = \Delta d/d$ ) and B (i.e.  $B = \Delta t/t$ ) respectively. Then the fractional error in the volume is:

a-  $(4A+B)^{1/2}$

b-  $4A^2+B^2$

(c)  $(4A^2+B^2)^{1/2}$

d-  $(A^2+B^2)$

Ex 16

Solution 8  $\frac{\Delta d}{d} = A$  /  $\frac{\Delta t}{t} = B$

\* fractional error in  $V \Rightarrow \frac{\Delta V}{V} ??$   $V_{disk} = V_{السطح}$

$$V = \pi h \left(\frac{d}{2}\right)^2$$

(has t) في السؤال

$$\Rightarrow \frac{\Delta V}{V} = \sqrt{\left(\frac{\Delta h}{h}\right)^2 + \left(2 \frac{\Delta d}{d}\right)^2}$$

$$\frac{\Delta V}{V} = \sqrt{(B)^2 + 4(A)^2}$$

$$\frac{\Delta V}{V} = (4A^2 + B^2)^{1/2}$$

### 3 Personal error

دائماً يأتي على سؤال إما ميد أو فائيل #

\* هناك 3 حالات لا يحد Personal error

1. توجد قيمة حقيقية (accepted value) وقيمة من التجربة (experimental)

2. لا توجد قيمة حقيقية وتوجد قرأتين من التجربة

3. لا توجد قيمة حقيقية وتوجد أكثر من قراءة من التجربة

شرح الحالات :

1. قيمة حقيقية مع قوة من التجربة :

$$P.E = \left| \frac{\text{القيمة الحقيقية} - \text{التجربة}}{\text{القيمة الحقيقية}} \right| * 100\%$$

19)

- 3- A cylindrical object is measured to have a diameter  $d$  of 5.25 cm and a circumference  $c$  of 16.38 cm. If the accepted value of  $\pi$  is 3.14, the percent error in the experimental value of  $\pi$  is (2 marks)
- a) 6%    b) 0.06%    c) 0.02%    d) 0.6%    e) 0.02%

Solution:  $d = 5.25$

$$c = 16.38$$

$$\Rightarrow c = \pi \cdot d \Rightarrow \frac{c}{d} = \pi \Rightarrow \pi = \frac{16.38}{5.25}$$



$$\pi_{exp} = 3.12$$

$$\pi_{acce} = 3.14$$

$$P.E = \frac{| \text{أمتق - تجربة} |}{\text{مقيسة}} * 100\%$$

التي غير لهم لوجود  
اشارة القيمة المطلقة

$$\Rightarrow P.E = \frac{|3.12 - 3.14|}{3.14} * 100\% \Rightarrow 0.636\%$$

خرج (d)  
العبار.

2

لا توجد مقيسة حقيقية وتوجد قسرين فقط احد التجربة :

$$P.E = \frac{| \text{الاولى - الثانية} |}{\left( \frac{\text{مجموعهم}}{2} \right)} * 100\%$$

انضاً الترتيب غير لهم لوجود  
اشارة القيمة المطلقة لا

eg 22/  $\pi = 3.14$  و  $\pi = 3.12$  experimental Value و Find the Percen error

Solution :

نلاحظ أن القاسم ناتجان عن تجربة ولم يذكر أن

أحد القيمتين accepted \* إذن هي الحالة 2

$$P.E = \frac{|3.14 - 3.12|}{\left( \frac{3.14 + 3.12}{2} \right)} * 100\% = \frac{0.02}{3.13} * 100\% = 0.63$$

لا توجد مقيسة حقيقية وتوجد أكثر من قراءة

$$P.E = \frac{| \text{أكبر قراءة - أصغر قراءة} |}{\left( \frac{\text{مجموعهم كلهم}}{\text{عددهم}} \right)} * 100\%$$

Ex 23

$$\pi = 3.12$$

$$\pi = 3.13$$

$$\pi = 3.14$$

experimental Value و find the P.E

من أنظر القاسم قسرين إذن الحالة 3

$$P.E = \frac{|3.14 - 3.12|}{\left(\frac{3.12 + 3.13 + 3.14}{3}\right)} * 100\% = \frac{0.02}{3.13} * 100\% = 0.638\%$$

[x20]

A cylindrical object is measured to have a diameter  $d = 3.52 \text{ cm}$  and a circumference  $c = 12.19 \text{ cm}$ . If the accepted value of  $\pi$  is  $3.14$ , the percent error in this experimental value of  $\pi$  is:

- (a) 4.4%  
(c) 4.9%

- (b) 10.2%  
(d) 9.2%

نفس فارق مثال 21

### Example 0.8:

What is the percent difference between two measured values of 4.6 cm and 5.0 cm?

Solution: With  $E_1 = 4.6 \text{ cm}$  and  $E_2 = 5.0 \text{ cm}$ ,

$$\text{percent difference} = \frac{|E_2 - E_1|}{(E_2 + E_1)/2} \times 100\%$$

$$\text{percent difference} = \frac{5.0 - 4.6}{(5.0 + 4.6)/2} \times 100\%$$

$$= \frac{0.4}{4.8} \times 100\% = 8.3\%$$

لما ماينكر في السؤال انه احد القيم  
accepted

بالتاي نختار القيم وادارة التجربة  
\* اذن في هذا المثال احنا بالحالة  
نعم







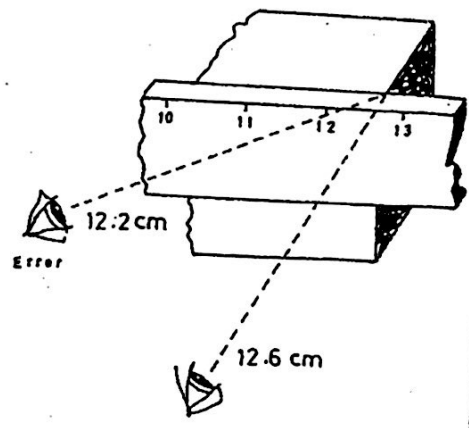
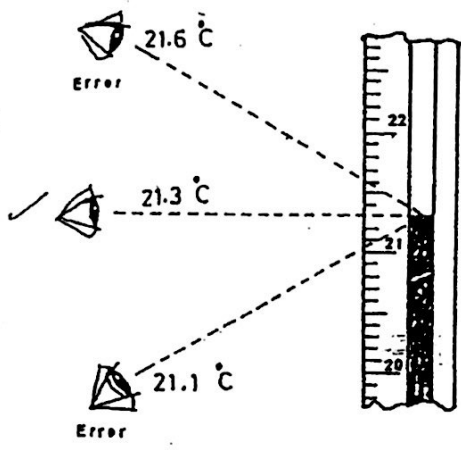


Fig (0.1) Examples of personal error in reading a scale due to parallax:

هو انظر لقراءة المسطرة بشكل غير افقي  
horizontal

بال عمودية

parallax  
personal error  
دعائه

## 2/ Systematic error:

هو الخطا الذي يكون بسبب  
الأداة نفسها

\* Systematic errors are errors associated with particular measurement instruments or techniques, such as an improperly calibrated instrument or bias on the part of the observer. Conditions from which systematic errors can result include:

1. An improperly "Zeroed" instrument (eg: a balance or ammeter)  
ان تكون الاداة غير موزونة على القراءة (صفر) بالبدائية مثلاً الميزان  
ان يقيس شيئاً موزوناً الصواب درجة الخطأ ان لا يكون صفر  
مثلاً
2. A thermometer that reads  $101^{\circ}\text{C}$  when immersed in boiling water at standard atmospheric pressure. The thermometer is improperly calibrated since the reading should be  $100^{\circ}\text{C}$ .  
(personal & systematic errors) هذه النقطة مثلاً  
ان يقيس شيئاً موزوناً الصواب درجة الخطأ ان لا يكون صفر
3. Personal bias of an observer, who, for example, always takes a low reading of a scale division. Thus, a personal error may be a systematic error.  
ان يقيس شيئاً موزوناً الصواب درجة الخطأ ان لا يكون صفر
4. A meter stick that has shrunk due to environmental conditions would always read higher  
تغير في قراءة أداة بسبب عوامل بيئية (بصيرت تقصراً أو طويلاً)

RANDOM error: ١٢: أي خطأ ناتج من البنية الميسرة ولا درجة الحرارة والأخطاء الجوية

3// Random errors result from unknown and unpredictable variations in experimental situations. Random errors are also referred to as accidental errors and are sometimes beyond the control of the observer. Conditions by which random errors can result include:

- 1: Unpredictable fluctuations in temperature or Line Voltage # صفقا الأمثلة على كى error ##
- 2: Mechanical Vibrations of the experimental setup اهتزازات
- 3: Unbiased estimates of measurement readings by the observer

له أنواع الأخطاء يأتي عليها سؤال واضع في الامتحان وسؤال في الفاصل - بيوتنا -

\* 2/ Physics Quantity: كميات فيزيائية (مقاييس)

- 1 Scalar quantity: time, distance, mass, speed, temperature, ..
- 2 Vector quantity: displacement, velocity, acceleration, .. كميات متجهة (مقاييس واداء)

\* 3/ Accuracy and Precision الدقة  
The Value error

\* في البداية ستم توضيح (Accuracy) و (precision)

وسوف 2 1 أمثلة على ذلك

Example 0.2: <sup>المثال</sup> <sup>المسألة</sup>

Two independent experiments give two sets of data with the expressed result and uncertainties of  $2.5 \pm 0.1$  cm and  $2.5 \pm 0.2$  cm, respectively. The first result is more precise than the second because the spread in the first measurements between 2.4 and 2.6 cm, whereas the spread in the second measurements between 2.3 and 2.7 cm. That is, the measurements of the first experiment are less uncertain than those of the second.

The accuracy of an experiment depends in general on systematic errors. The precision of an experiment depends on random errors.

\* إذا كان الخطأ العشوائي أكبر من الخطأ المنهجي

more accurate

هنا تقارب الأرقام المعطاة

بالقيمة الحقيقية

في نظريتي الخطأ قبل  $(\pm)$  فالتقارب إلى القيمة الحقيقية يكون الجواب

more precise

نظرية ما بعد  $(\pm)$  والاختلاف

الجواب الصحيح \* أي الاختلاف

سؤال عن أنواع الأخطاء :

- Which of the following is an example of a random error?
- a) Improperly zeroed instrument
  - b) Fluctuation in temperature
  - c) Using an old meter stick
  - d) None of the above

answer: b ✓✓

ملاحظة: كل تجربة لها نوع من الأخطاء وسنذكرها عند كل سؤال...  
وهناك أمثلة على الأخطاء المنهجية في الأمثلة في المقدمة



\*

- 7- Two independent experiments give two sets of data for earth acceleration "g" with the expressed results and uncertainties of  $9.8 \pm 0.5$  and  $9.7 \pm 0.1 \text{ m/s}^2$ . Respectively. (the accepted value of  $g = 9.8 \text{ ms}^{-2}$ )

(2 marks)

- The accuracy and the precision of the second experiment is better than the first.
- The accuracy and the precision of the first experiment is better than the second.
- ☒ The second experiment is more precise than the first.
- The first experiment is more precise than the second.
- The second experiment is more accurate than the first.

\* توضيح للسؤال وطريقة الحل :

First experiment  $\rightarrow 9.8 \pm 0.5$   
 second experiment  $\rightarrow 9.7 \pm 0.1$   
 له بعدوان نسبة الخطأ .

وهذه القيمة الحقيقية للمعيارية  $g = 9.8 \text{ m/s}^2$

Solution:

على الترتيب

وبعد هاتان علاقة

more accurate

- \*  $9.8 \pm 0.5$
  - \*  $9.7 \pm 0.1$
- \*  $g = 9.8$

كما وضعنا سابقاً بنقارنا الرقم الذي قبل (±) بالقيمة الحقيقية والاقرب لها هو الجواب

9.8  
9.8

الاقرب  
والاصغر

2B

more precise

- \*  $9.8 \pm 0.5$
  - \*  $9.7 \pm 0.1$
- \*  $g = 9.8$

كما وضعنا سابقاً بنقارنا الأرقام الذي بعد (±) والاقرب

0.5 > 0.1  
الاقرب

وهو هو الجواب

\* second exp more precise

لأنه الثاني

(2:

1. In order to obtain the value of gravitational acceleration ( $g$ ), two students computed the following results ( $g_1 = 10.0 \pm 0.02 \text{ m/s}^2$ ,  $g_2 = 9.7 \pm 0.2 \text{ m/s}^2$ ), if the accepted value is ( $g = 9.8 \text{ m/s}^2$ ) then:

- a) Two students have the same accuracy, but student one is more precise.
- b) Two students have the same precision, but student two is more accurate.
- c) Student one is more precise and less accurate than student two.
- d) Student two is more precise and more accurate than student one.

توضيح السؤال : نفس فكرة  $\{x_1$

$$g_1 = 10.0 \pm 0.02$$

$$g_2 = 9.7 \pm 0.2$$

$$g = 9.8 \text{ m/s}^2 \Rightarrow \text{accepted Value (القيمة الحقيقية)}$$

Solution:

more accurate

$$*g_1 = 10.0 \pm 0.02$$

$$*g_2 = 9.7 \pm 0.2 \rightarrow \text{more accurate}$$

$$g = 9.8$$

قابل  $\pm$

$$\begin{array}{|c|} \hline 10.0 \\ \hline 9.8 \\ \hline \end{array}$$

$$\begin{array}{|c|} \hline 9.7 \\ \hline 9.8 \\ \hline \end{array}$$

الأقرب للقيمة الحقيقية

$g_2$  more accurate than  $g_1$

more precise

$$g_1 = 10.0 \pm 0.02$$

$$g_2 = 9.7 \pm 0.2$$

$$g = 9.8$$

↓

قابل  $\pm$

$$0.02 \quad \boxed{<} \quad 0.2$$

الأصغر

$g_1$  more precise than  $g_2$

اذن الجواب  $\underline{\underline{c}}$

Student One is more precise and less accurate than Student two

(24)



ما هي الخطأ في كل تجربة ونوع الخطأ : (What's the major error of the exp)

error in calculations and measurements : سبب الخطأ

تجربة + collection and analysis of data : [1] تجربة  
Measurements and uncertainties

personal error : نوع

Frictional force : سبب الخطأ :  
systematic error : نوع الخطأ

Force + Force table : [2] تجربة  
and motion

changing in temperature

gas : سبب الخطأ : [3] تجربة  
Laws

Random error : نوع الخطأ

Lost heat to surrounding

Heat capacity : سبب الخطأ : [4] تجربة

Random error : نوع الخطأ

error in calculating the time period /  $\theta$  is very big

note

personal error : نوع الخطأ

Simple pendulum : [5] تجربة

the major error of

inaccuracy  
= systematic

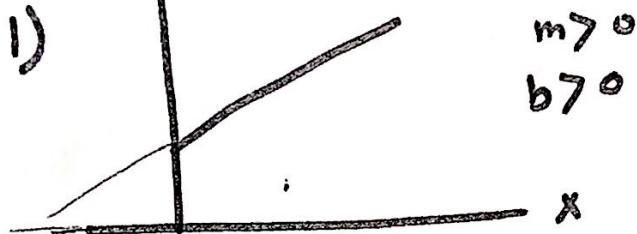
precision  
= Random

personal error : سبب الخطأ : Kinematic & Rectilinear motion : [6] تجربة  
نوع الخطأ : we must move the paper with an Avg speed not high or low

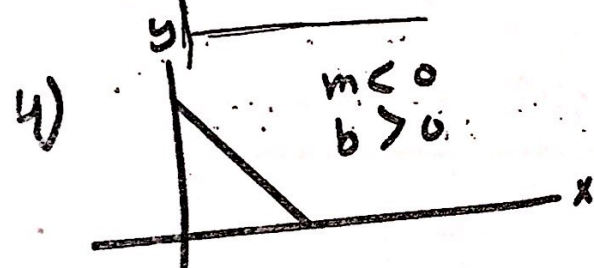
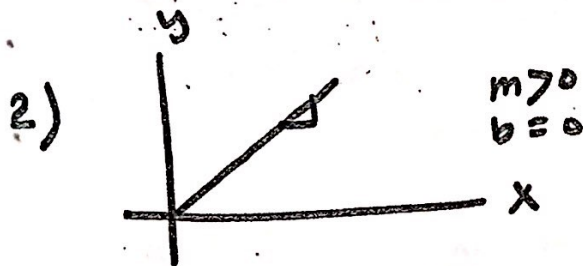
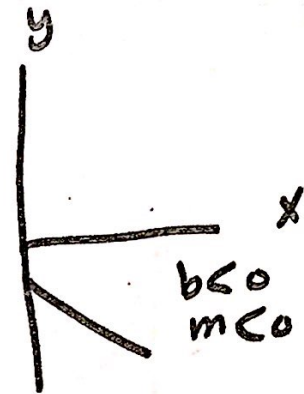


# الاختلاف الفعلي (اشكاله)

$$(y = mx + b)$$



7

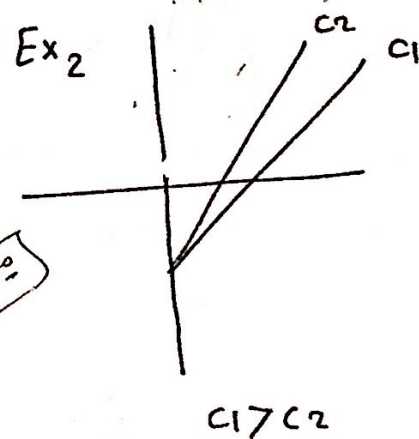
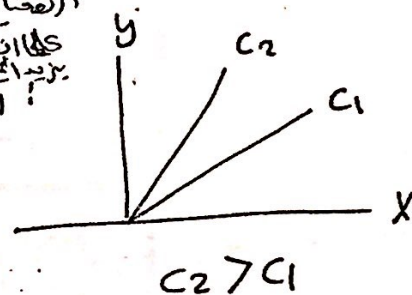


notes:

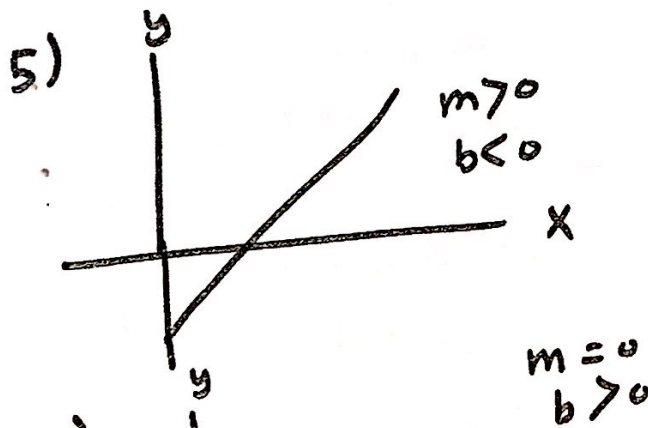
بالنسبة الميل في الربع الاول كلما ارتفعنا زداد .

اذا في الربع الرابع كلما ارتفعنا يقل

له كما فنزلنا للأسفل نزيد  
او بلا أخرى  
 $b > 0 \Rightarrow$  كلما ارتفعنا نزيد الميل  
 $b < 0 \Rightarrow$  كلما انخفضنا نزيد الميل  
Ex 1



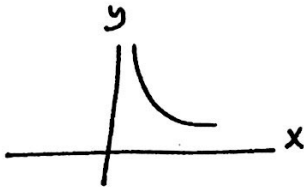
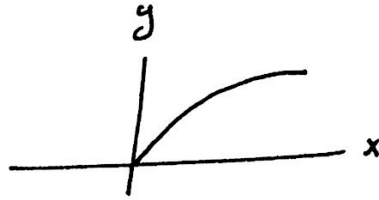
ميل  
 $C =$



لهذه الرسومات كلها جداً لجميع تجارب المارة فسوف نتابعهم  
لاستفاد رسومات جميع التجارب #

$$y = b\sqrt{x} \quad (\text{الصيغة العاقبة})$$

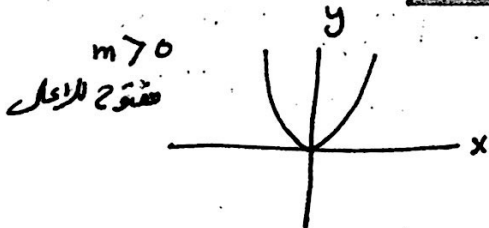
\* الاقتران العكسي :



$$y = \frac{m}{x^2} + b$$

الصيغة العاقبة :

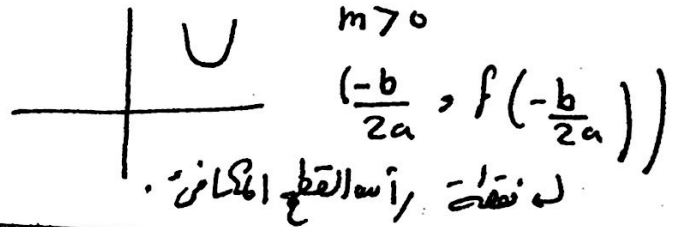
$$\text{OR} \quad y = \frac{m}{x} \quad \text{نفس الصيغة}$$



$m > 0$   
مفتوح للأعلى

$$y = mx^2 + b$$

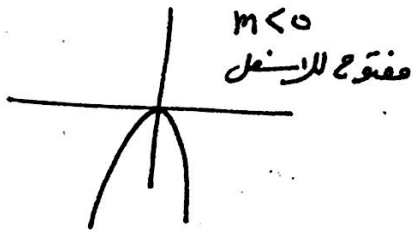
\* الاقتران التربيعي :



$m > 0$

$$\left( -\frac{b}{2a}, f\left(-\frac{b}{2a}\right) \right)$$

له نقطة رأس القطع المكافئ.



$m < 0$   
مفتوح للأسفل

رأى  
ال  
السؤال  
Introduction

Ex1. Given that  $R = \frac{x^3}{10yz}$  with  $x \pm \Delta x = 4 \pm 0.01$ ,  $y \pm \Delta y = 5 \pm 0.02$  and  $z \pm \Delta z = 10 \pm 0.1$ , then  $\Delta R$  equals: 2 Marks

(a)  $15.2 \times 10^{-5}$

(b)  $19 \times 10^{-5}$

(c)  $13 \times 10^{-4}$

(d)  $16.8 \times 10^{-4}$

$$\Delta R = R \sqrt{\left(\frac{3\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2 + \left(\frac{\Delta z}{z}\right)^2}$$

$$\Delta R = 0.128 \sqrt{0.000056 + 0.00016 + 0.0001} = 0.00167 = 16.8 \times 10^{-4}$$

Ex2. Error Analysis:

12) If  $X \pm \Delta X = 10 \pm 0.1$ ,  $Y \pm \Delta Y = 30 \pm 0.5$  and  $Z \pm \Delta Z = 15 \pm 0.2$ , then the magnitude of error in R for the following relation is;

$$R = Y \cdot X / Z^2$$

$$30 \cdot 10 / 15^2$$

b) 0.004

a) 0.017

c) 0.510

(d) None of the above

$$\Delta R = \sqrt{(\Delta Y)^2 + (\Delta B)^2}$$

$$= \sqrt{(0.5)^2 + (0.0012)^2}$$

$$= 0.500001$$

none

$$B = \frac{Y}{Z^2}$$

لنفرض

$$\Delta B = B \sqrt{\left(\frac{\Delta X}{X}\right)^2 + \left(\frac{2\Delta Z}{Z}\right)^2}$$

$$= 0.044 \sqrt{0.0001 + 0.00071}$$

$$= 0.00125$$

EX  $R = y - 3x^2$

Find  $\Delta R$

$$x \pm \Delta x = 2.32 \pm 0.01$$

$$y \pm \Delta y = 1.16 \pm 0.02$$

$$\Delta R = \sqrt{(\Delta y)^2 + (3\Delta B)^2}$$

$$= \sqrt{(1.16)^2 + (3 \times 0.046)^2}$$

$$= 0.139$$

$$B = x^2$$

$$\Delta B = B \sqrt{\left(\frac{2\Delta x}{x}\right)^2}$$

$$= 2.32 \times (2 \times 0.01)$$

$$= 0.046$$

1081



Ex 3) The correct empirical relation that describes the plotted curve in graph is:

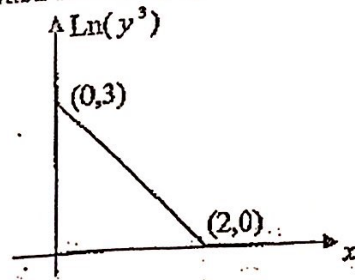
2 Marks

(a)  $y = e^{1-x^2}$

(b)  $y^2 = e^{1-x^2}$

(c)  $y^3 = e^{3-3x}$

(d)  $y = e^{1-x/2}$



$$y = mx + b$$

$$\ln y^3 = \frac{3}{-2}x + 3$$

منه  $\Rightarrow y^3 = e^{-\frac{3}{2}x+3}$

~~$y = e^{-\frac{3}{2}x+3}$~~   $(y = \frac{-x}{2} + 1)^2$  ?  
 $y = e^{-\frac{3}{2}x+2}$

Ex 2) Given the function  $y = c10^{2mx}$ , where  $c$  and  $m$  are constants. The value of  $m$  may be determined from a graph of:

2 Marks

(a)  $y$  versus  $x$

(c)  $\log(y)$  versus  $\log(mx)$

(b)  $\log(y)$  versus  $x$

(d)  $\log(y)$  versus  $\log(x)$

لايجاد  $m$  من خلال ال slope و y-intercept

$\log y = \log c 10^{2mx}$  نستخدم Log للتبسيط

$$\log y = \log c + \log 10^{2mx}$$

$$\log y = \log c + \frac{2mx}{\cancel{x}}$$

slope

ب) لذلك الإجابة الصحيحة

Ex<sub>1</sub> given that  $R = (3x+2y)/(y-x)$  then  $\Delta R$  is given by:

$R = \frac{A}{B}$

$A = 3x+2y$

$B = y-x$

$\Delta R = R \sqrt{\left(\frac{\Delta A}{A}\right)^2 + \left(\frac{\Delta B}{B}\right)^2} = R \sqrt{\left(\frac{(3\Delta x)^2 + (2\Delta y)^2}{(3x+y)^2}\right) + \left(\frac{(\Delta y)^2 + (\Delta x)^2}{(y-x)^2}\right)}$

none of the above

Ex<sub>2</sub> the diameter of a sphere was measured four times the measurements are 2.40 cm, 2.35 cm, 2.44 cm, 2.38 cm Find the area of the sphere surface ( $A \pm \Delta A$ ) in  $\text{cm}^2$

$d = \frac{2.44 + 2.4 + 2.35 + 2.38}{4} = 2.3925$

$A_{\text{sphere}} = \pi \left(\frac{d}{2}\right)^2 = 3.14 \times \left(\frac{2.38}{2}\right)^2 = 4.48 \text{ cm}^2$

$\Delta A = A \sqrt{\left(\frac{2\Delta d}{d}\right)^2} = A \times \frac{2\Delta d}{d}$

$= 4.48 \times 2 \times 0.0005 = 0.00448$

$= 1.8 \times 10^{-3} = 0.0018$

none of the above

$4.48 \pm 0.0018$

Ex<sub>3</sub> In force table experiment the error caused by the friction force between pulley (ofu) and strings is considered as:

- (a) personal error
- (b) systematic error
- (c) Random error
- (d) analytical error

Ex<sub>4</sub> Two experiments were done to find the value of the acceleration due to gravity. The results are  $g_1 = 9.7 \pm 0.52 \text{ m/s}^2$

$g_2 = 9.3 \pm 0.21 \text{ m/s}^2$

(a)  $g_1$  is more accurate but  $g_2$  is more precise

then:

(20)



EX 5  
2016

Which of the following is not systematic error?

Random errors  
(عشوائية)

- (a) Improperly zeroed instrument
- (b) Vibration in the experimental setup
- (c) The Thermometer is improperly calibrated since the reading should be 100°C
- (d) A student always takes a low reading of a scale division

EX 6  
2016

A room whose length is measured to be  $12.75 \pm 0.005$  m and whose width is measured to be  $3.64 \pm 0.001$  m. Find the area and the error in the area of the room ( $A \pm \Delta A$ ) in  $m^2$ .

$$A = \text{Length} \times \text{width}$$

$$= 12.75 \times 3.64$$

$$= 46.41 \text{ m}^2$$

$$\Delta A = A \sqrt{\left(\frac{\Delta L}{L}\right)^2 + \left(\frac{\Delta W}{W}\right)^2}$$

$$= 46.41 \sqrt{\left(\frac{0.005}{12.75}\right)^2 + \left(\frac{0.001}{3.64}\right)^2} = 0.022$$

$$(46.41 \pm 0.022) \text{ m}^2$$

EX 7  
2016

Given that function  $y = c 10^{mx}$ , where  $m$  and  $c$  are constants, the value of  $m$  may be determined from the graph of:

- (a)  $y$  versus  $x$
- (b)  $\log y$  versus  $x$
- (c)  $\log y$  versus  $\log(mx)$
- (d)  $\log y$  versus  $\log x$

EX 8  
2016

Two students made an experiment to measure the gravitation acceleration, The first one had  $g = 10.0 \pm 0.5 \text{ m/s}^2$  and  $g_2 = 9.7 \pm 0.2 \text{ m/s}^2$

which of the following statements best describes these results:

Student two is more precise and more accurate than student one.



EX<sub>9</sub>  $R = y - 3x$

$x \pm \Delta x = 2.32 \pm 0.01$

$y \pm \Delta y = 1.16 \pm 0.02$

Find  $\Delta R$

2016

الحل  $\Rightarrow$   
المطلوب

$$\begin{aligned}\Delta R &= \sqrt{(\Delta y)^2 + (3\Delta x)^2} \\ &= \sqrt{(0.02)^2 + (3 \times 0.01)^2} \\ &= \underline{0.139} \\ &\quad \# \end{aligned}$$

$$\begin{aligned}B &= x^2 \cdot x^2 \\ \Delta B &= B \sqrt{\left(\frac{2\Delta x}{x}\right)^2} \\ &= 2 \times \Delta x \\ &= 2 \times 2.32 \times 0.01 \\ &= 0.046 \end{aligned}$$

EX<sub>10</sub>  
ميدان  
الثاني  
2016

A student measured the following values of the radius (R) of a circle in cm. They were  $r = 1.08, 1.18$  and  $1.04$  cm. the error in the measured radius in (cm)

$$\begin{aligned}\bar{r} &= \frac{1.08 + 1.18 + 1.04}{3} \\ &= 1.08\end{aligned}$$

$$\begin{aligned}\Delta r &= \sqrt{\frac{\sum_{i=1}^n (r_i - \bar{r})^2}{N(N-1)}} \\ &= \sqrt{\frac{(1.08 - 1.08)^2 + (1.18 - 1.08)^2 + (1.04 - 1.08)^2}{3(2)}} \\ &= \dots \dots \dots \# \\ &= 0.0281\end{aligned}$$

EX<sub>11</sub>

$R = \frac{x^2}{2yz}$

$x \pm \Delta x = 2.32 \pm 0.02$

$y \pm \Delta y = 2.45 \pm 0.01$

$z \pm \Delta z = 3.65 \pm 0.05$

then  $\Delta R/R = ?$

$$\begin{aligned}\frac{\Delta R}{R} &= \sqrt{\left(\frac{2\Delta x}{x}\right)^2 + \left(\frac{\Delta y}{y}\right)^2 + \left(\frac{\Delta z}{z}\right)^2} \\ &= \underline{0.335} \\ &\quad \# \end{aligned}$$

في صحته

EX<sub>12</sub>

The independent variable in an experiment is:

- (a) the variable you hope to observe
- (b) the variable you change in an experiment
- (c) The variable that isn't changed in an experiment
- (d) none of these is correct

(32)

EX<sub>13</sub> A student obtained the following values of the radius (r) of a circle in cm. He obtained  $r = 2.13, 2.14, 2.15, 2.16$  and  $2.17$   
 the error in the measured radius  $\Delta r$  (in cm) is :

$$\bar{r} = \frac{2.13 + 2.14 + 2.15 + 2.16 + 2.17}{5} = 2.15$$

$$\Delta r = \sqrt{\frac{\sum_{n=1}^N (r - \bar{r})^2}{N(N-1)}}$$

$$= \sqrt{\frac{(2.13 - 2.15)^2 + (2.14 - 2.15)^2 + (2.15 - 2.15)^2 + (2.16 - 2.15)^2 + (2.17 - 2.15)^2}{5(4)}}$$

$$= \sqrt{5 \times 10^{-5}} = 7.071 \times 10^{-3} = 0.007071$$

$$\approx \underline{\underline{0.0071}}$$

جواب 0.0071

EX<sub>14</sub> Depending on the previous question, If the true value of radius is 2.11 cm, the percent error in the radius of the circle in (cm) is:

$$P.E = \left| \frac{\bar{r} - r_{\text{accepted}}}{r_{\text{accepted}}} \right| \times 100\% = \left| \frac{2.15 - 2.11}{2.11} \right| \times 100\%$$

$$= 1.896\%$$

جواب 1.896%

Experiment (1)

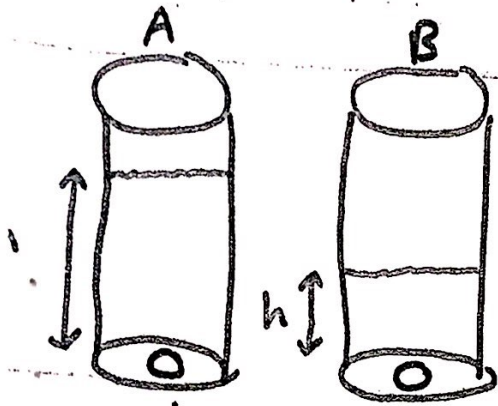
Collection and Analysis  
of Data

engine\_team



# Exp: Collection and analysis of data :

توضيح :



\* نفس القطر  $\underline{d}$

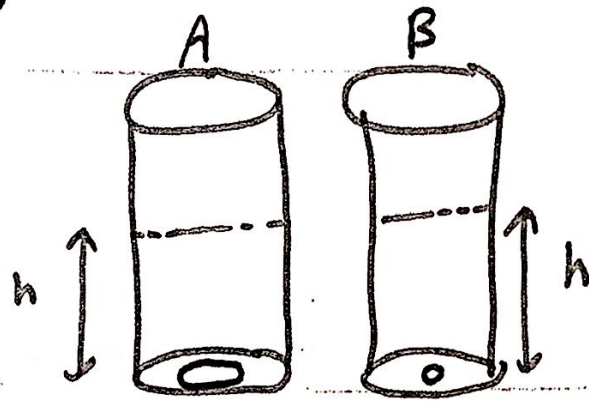
\* الوعاء A ارتفاع الماء  $h$  فيه  
أكثر من الوعاء B

\* سلاحظنا أننا في الوعاء A سنحتاج  
إلى زمن أكبر لإفراغه

\* إذن كلما زاد ارتفاع الماء زاد  
الزمن المستغرق لتفريغ الوعاء

$$t \propto h$$

(العلاقة طردية)



→ نفس ارتفاع الماء  $h_A = h_B$

و الوعاء A القطر أكبر من الوعاء B

$$d_A > d_B$$

و الوعاء A القطر أكبر من الوعاء B بالتالي سيقل  
الزمن اللازم لتفريغ الوعاء ..

$$t \propto \frac{1}{d} \quad \text{(العلاقة عكسية)}$$

ملحوظة :

d: diameter:	القطر
h: height:	الارتفاع

$$\boxed{1} \quad t = 10^b h^m$$

\* قوانين حفظ :

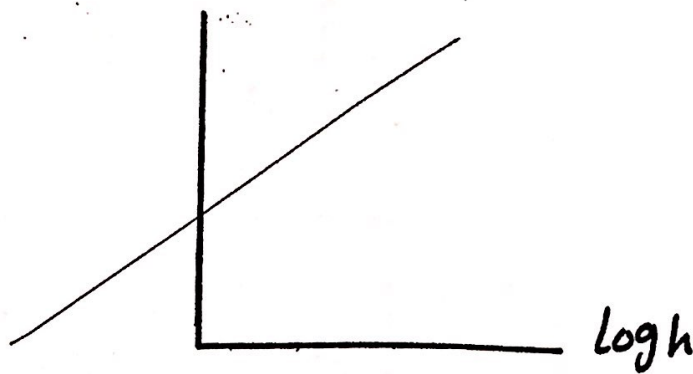
t: time: الزمن (sec) الوحدة

b: y-int  $\Rightarrow$  التقاطع مع محور الصادات

h: height  $\Rightarrow$  الارتفاع  $\Rightarrow$  cm

III

\* الرسمة التي نستخدم فيها القانون الأول 8



وأيضا  $\underline{h}$

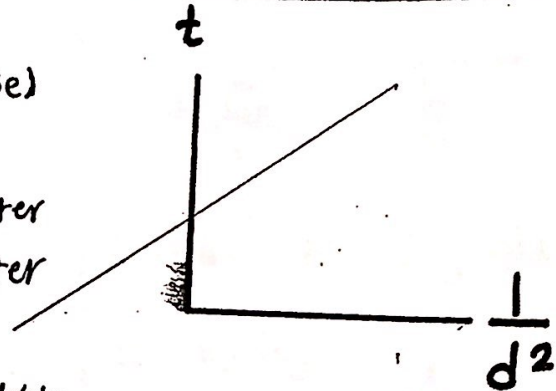
[2]  $t = \frac{m}{d^2} + b$

8 t: time (se)

8 m slope

8 d diameter

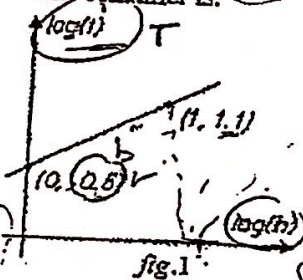
8 b y-inter



Ex 26]

2. The time needed to empty a container filled with water depends on its height for a certain hole diameter as shown in fig. 1 below. According to that, if the height of water was 70m, then the time needed to empty the same container is:

- 10.53sec
- 7.96sec
- 1.02sec
- 0.90sec



Solution :

log t

log h

مما أنت اعطانه رسمه

$t = 10^b h^m$

نستخدم القانون

$t = 10^{0.6} (7)^{0.5} = 10.532 \text{ sec}$

الاجواب فرج

$x_1, y_1$   
 $(0.6, 0.9)$   
 $x_2, y_2$   
 $(1.1, 1.1)$

$m \rightarrow \text{slope: } \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1.1 - 0.9}{1.1 - 0.6} = 0.5$

[2]



Ex 27]

## Collection and Analysis of Data:

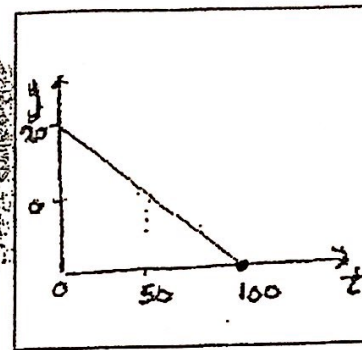
1- For the figure shown, (y) as a function of (t) is given by:

b)  $20 - 0.2t$

a)  $5t + 20$

d)  $100 - t$

c)  $20 - 5t$



Solution 8  $y = mx + b$

$y = \text{slope} \times t + 20$

$y = -0.2t + 20$

$y = 20 - 0.2t$

slope:  $(0, 20)$   
 $(100, 0)$

$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{0 - 20}{100 - 0} = \frac{-20}{100} = -0.2$

Ex 28]

Which of the following statements is correct for the time required to empty the cylindrical container:

(a) If  $d$  is constant, the time is directly proportional to the height of water.

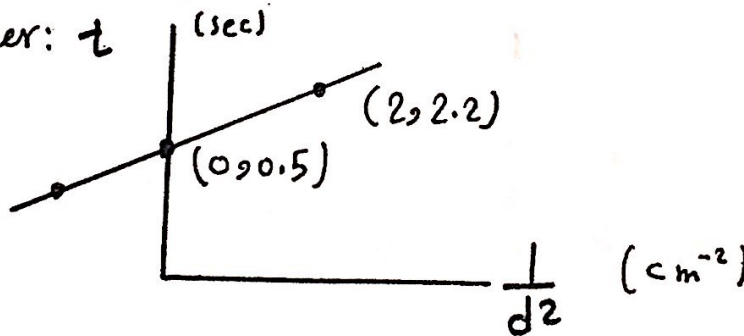
(b) If  $h$  is constant, the time is directly proportional to the diameter of the hole.

(c) If  $d$  is constant, the time is inversely proportional to the height of water.

(d) If  $h$  is constant, the time is directly proportional to the area of the hole.

الجواب فيج  $a$  كما ذكرنا سابقاً  $t \propto h$  (طردى) بثبت  $d$  لا يقل.

Ex 29] IF the diameter  $\Rightarrow d = 5 \text{ cm}$  find the time needed to empty the container:  $t$



Solution:

نطبق على القانون التالي

$\Rightarrow t = \frac{m}{d^2} + b$

$\Rightarrow t = \frac{0.85}{(5)^2} + 0.5 = 0.534 \text{ s}$

slope  $= \frac{y_2 - y_1}{x_2 - x_1} =$

$\frac{2.2 - 0.5}{2 - 0} = 0.85$



2- The relation between the time needed to empty container and the depth of the water is given by  $t = c\sqrt{h}$  where  $c$  is constant. For a certain depth the time needed is 8 sec, if the depth is halved then the time in (sec) needed to empty the container is: (2 marks)

- a) 3.45    b) 1.73    c) 4.2    d) 5.6    e) 2.6

$$t = c\sqrt{h}$$

\*  $t_1 = 8 \text{ sec}$      $t_2 ??$   
 $h_1 \uparrow$      $h_2 = \frac{1}{2} h_1 \rightarrow$

فصل سوال  
 \* نفسم المهادلينة :

halved :  $\Rightarrow h_2 = \frac{1}{2} h_1$   
 trippled :  $\Rightarrow h_2 = 3 h_1$   
 one-fourth :  $\Rightarrow h_2 = \frac{h_1}{4}$   
 one-fifth :  $\Rightarrow h_2 = \frac{h_1}{5}$

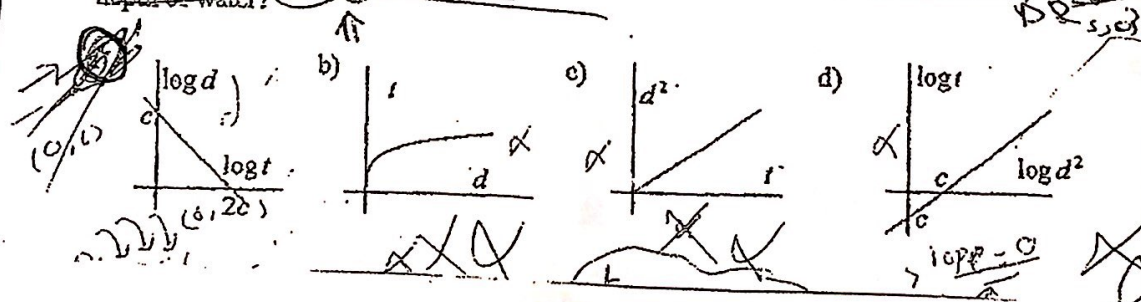
$$\frac{t_2 = c\sqrt{h_2}}{t_1 = c\sqrt{h_1}} \Rightarrow \frac{t_2}{8} = \frac{\sqrt{0.5} \sqrt{h_1}}{\sqrt{h_1}} \Rightarrow \frac{t_2}{8} = \sqrt{0.5} \Rightarrow t_2 = 5.65$$

جوابه

Ex 31]  $t = c\sqrt{h}$ , when  $t_1 = 6 \text{ sec} \rightarrow h_1$  \*  $c$  is constant و  $t_2 ??$   
 \*  $h_2 = 0.5 h_1 ??$     نفس فارق سوال 30

$t_2 = 4.24 \text{ sec}$     الجواب النهائي

3. Which of the following graphs is correct to represent the relation between the time ( $t$ ) and the diameter of the hole ( $d$ ) on the bottom of the container at constant depth of water?



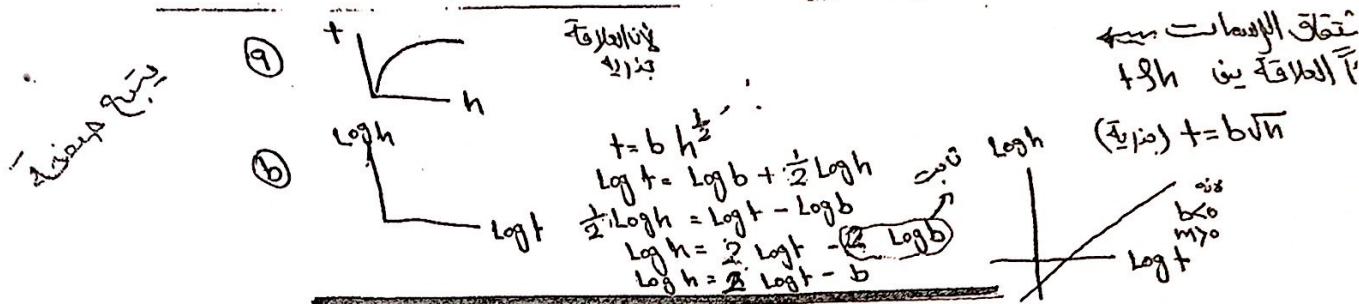
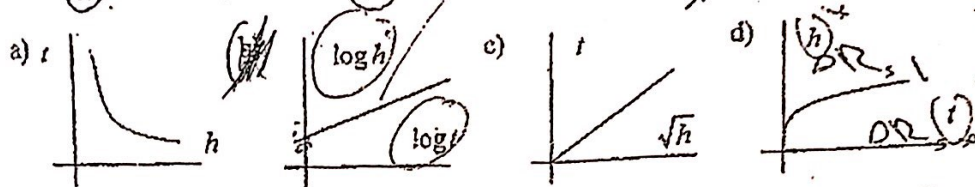
note

33 / 32 سوال  
 8/7

14

Ex 33]

2. Which of the following graphs is correct to represent the relation between the time ( $t$ ) and the depth of water ( $h$ ) in the container at constant area of the hole?



Ex 34]

5-It is found that the relationship between the time  $t$  (in sec) of water emptying and height of water level  $h$  (in cm), for containers with hole diameter  $d$  (in cm) is given by  $\log_{10} t + 2 \log_{10} d = 0.25$ . At what diameter of the hole is the emptying time 7 sec?

0.504 cm.

$$\log t + 2 \log d = 0.25$$

$$t = 7$$

$$d = ?$$

$$\Rightarrow \log 7 + 2 \log d = 0.25$$

$$\log d = \frac{0.25 - \log 7}{2} \Rightarrow \log d = -0.297 \Rightarrow d = 0.504 \text{ cm}$$

Ex 35]

5- COLLECTION AND ANALYSIS OF DATA:

For the corresponding figure (3),

which shows A log relation,

find in clear mathematical steps

The relation between  $y$  and  $x$

Such as  $y =$

$$y = mx + b$$

$$y = K x^m$$

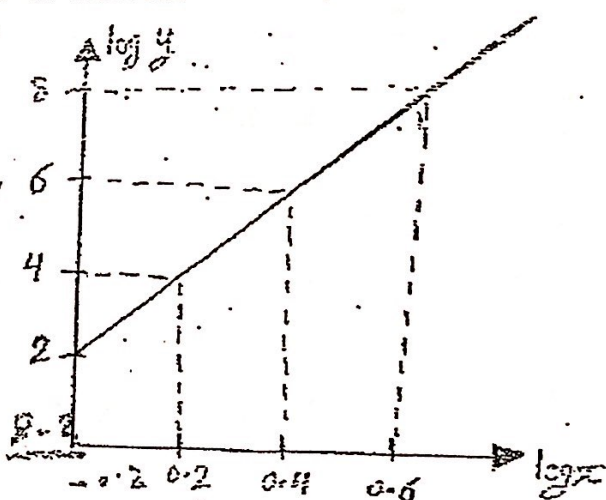
$$\log y = \log K + m \log x$$

$$y = mx + b$$

$$y = K x^m$$

$$m =$$

(الميل المستقيم)



127



Solution :

$$y = mx + b$$

$$\log y = m \log x + 2$$

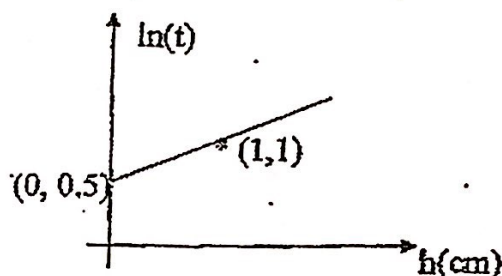
$$\frac{\log y}{10} = \frac{10 \log x + 2}{10} \Rightarrow y = x^{10} \times 100$$

$$m = \frac{6-4}{0.4-0.2} = 10$$

36

8) In an experiment, a student measures the variation between the height of water (h) in a container and the time needed to empty water from a hole with diameter (d). The correct relation that represents the following figure is:

- a)  $t = 1.65 e^{h/2}$
- b)  $t = 1.65 e^{2h}$
- c)  $t = 7.4 e^{2h}$
- d)  $t = 7.4 e^{h/2}$



Solution :

$$\Rightarrow y = mx + b$$

$$\Rightarrow \ln t = m h + 0.5$$

$$\Rightarrow \ln t = 0.5 h + 0.5$$

$$\Rightarrow \frac{\ln t}{e} = \frac{0.5 h + 0.5}{e}$$

$$\Rightarrow t = 1.643 e^{h/2} \quad \text{الخيار } \underline{a} \quad \text{الجواب الصحيح}$$

هذا الخط مستقيم

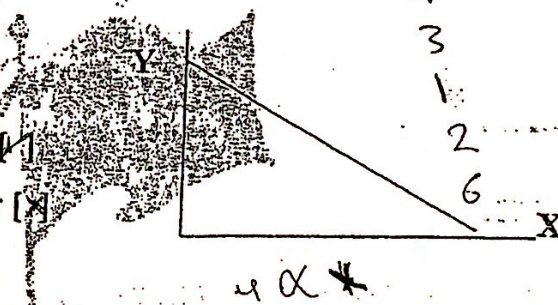
$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 0.5}{1 - 0} = 0.5$$

### 1- Collection and Data Analysis

Refer to figure beside

⊗ The relation between y and x is linear [✓]

⊗ The relation between y and x<sup>3</sup> is linear [✗]



$$y = mx + b$$

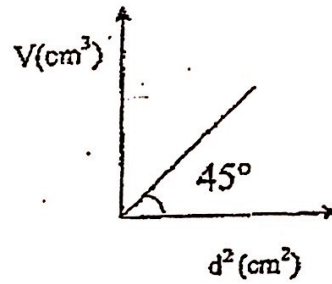
Linear

البيانات من المخطط أن العلاقة خطية بين x و y لأن تكون خطية

161



4-In an experiment... to measure the variation of the volume  $V$  versus the square of the diameter  $d^2$  of a cylindrical object of constant height  $h$ , the graph below is obtain. The height  $h$  of the cylinders is: 1.27 cm.



$\tan \theta$  slope  $\frac{\Delta y}{\Delta x}$

\*  $V_{\text{cylinder}} = h \pi \left(\frac{d}{2}\right)^2$

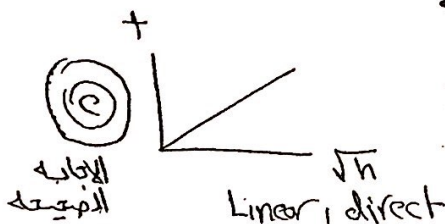
$V = \frac{h \pi d^2}{4} + 0$

$\Rightarrow \text{slope} = \frac{h \pi}{4}$

$\Rightarrow \text{slope} = \tan 45$

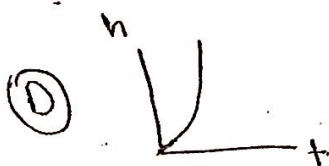
$\frac{h \pi}{4} = \tan 45$

$\frac{h \pi}{4} = 1 \Rightarrow \frac{4}{\pi} = h \pi \Rightarrow \left(h = \frac{4}{\pi}\right) \text{ cm} \Rightarrow h = 1.27 \text{ cm}.$



$t = b \sqrt{h}$

33

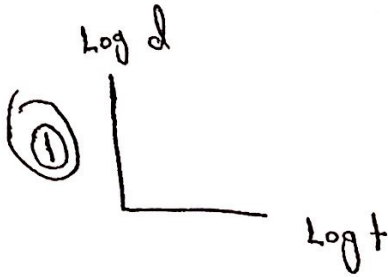


$t = b \sqrt{h}$   
 $t^2 = b^2 h$   
 $h = \frac{1}{b^2} t^2$   
 $h = m t^2$

هذا هو الشكل المتوقع للبيانات

Ex 32

الاجابة الصحيحة



نبدأ من هنا

العلاقة بين  $t$  و  $d$

$$t = \frac{m}{d^2}$$

$$t = \frac{m}{d^2} \Rightarrow t \cdot d^2 = m \Rightarrow d^2 = \frac{m}{t} \Rightarrow$$

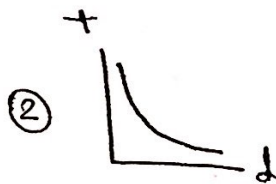
$$d^2 = m(t)^{-1} \xrightarrow{\text{Log}} 2 \log d = \log m + 1 \log t$$

$$\log d = \frac{\log m}{2} - \frac{1}{2} \log t \Rightarrow \log d = \frac{\log m}{2} - \frac{1}{2} \log t$$

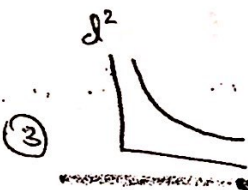
y-intercept slope



الاجابة الصحيحة

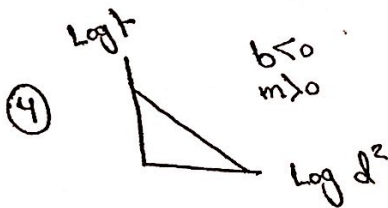


خط اقتران عكسي



$$t = \frac{m}{d^2} \Rightarrow d^2 = \frac{m}{t}$$

خط اقتران عكسي



$$t = \frac{m}{d^2} \Rightarrow \log t = \log m - 2 \log d^2$$

y-intercept slope

8

EX<sub>1</sub> Which of the following statement is correct for the time required to empty the cylindrical container:

(a) If  $h$  is constant, the time is directly proportional to the area of the hole

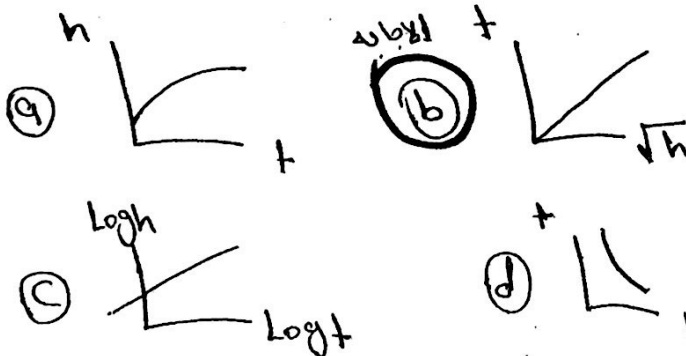
(b) If  $h$  is constant, the time is directly proportional to the diameter of the hole

(c) If  $d$  is constant, the time is inversely proportional to the height of the water

(d) If  $h$  is constant, the time is inversely proportional to the area of the hole

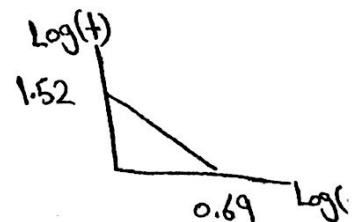
الإجابة الصحيحة  
والتي هي (d) هي الصحيحة  
بالتجربة

EX<sub>2</sub> Which of the following graphs is correct to represent the relation between the time ( $t$ ) and the depth of water ( $h$ ) in the container at constant area of the hole!



السؤال الصحيح  
وضوح الاختيار  
السابق

EX<sub>3</sub> In collection and analysis of data exp the height of the water is 1cm, the relation between  $\text{Log}(t)$  and  $\text{Log}(d)$  is plotted in the figure below, If the diameter of the hole  $d=2\text{mm}$ , what's the time needed to empty the container?



الاجابة هي (a)

(a)



$$\text{Log } t = m \text{Log } d + b$$

$$\text{Log } t = \text{Log } d^m + b$$

$$t = 10^{\text{Log } d^m + b}$$

$$t = d^m \times 10^b$$

$$t = 2^{-2.202} \times 10^{1.52}$$

$$= 7.18 \text{ sec}$$

##

EX<sub>2</sub> is  
Empirical relation

$$m = \frac{\Delta y}{\Delta x} = \frac{1.52}{-0.69} = -2.202$$

$$b = 1.52$$

EX<sub>4</sub> For the previous question; the empirical relation between  $t$  &  $d$  is:

$$t = \frac{10^{1.52}}{d^{2.202}} = \frac{33}{d^{2.2}}$$

$$\# \quad t = \frac{33}{d^{2.2}}$$

← Empirical relation

EX<sub>5</sub> The time needed to empty a container filled with water depends on its height for a certain hole diameter as shown in fig. below. According to that, If the height of the water was 10 cm, then the time (in sec) needed to empty the container is;

empirical relation

$$\text{Log } t = m \text{Log } h + b$$

$$\text{Log } t = 0.52 \text{Log } h + 0.8$$

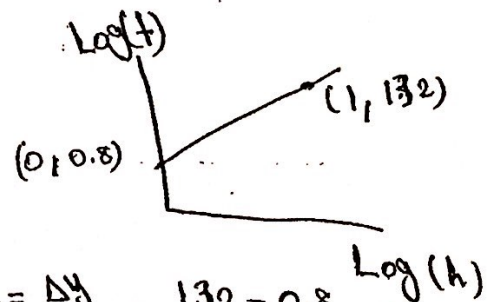
$$\text{Log } t = \text{Log } h^{0.52} + 0.8$$

$$\text{Log } h^{0.52} + 0.8$$

$$t = 10^{\text{Log } h^{0.52} + 0.8}$$

$$= 10^{\text{Log } h^{0.52}} \times 10^{0.8}$$

$$t = h^{0.52} \times 10^{0.8} = 10^{0.52} \times 10^{0.8} = 20.893 \quad (10)$$



$$m = \frac{\Delta y}{\Delta x} = \frac{1.32 - 0.8}{1 - 0} = 0.52$$

$$b = 0.8$$

$$t = 20.893 \quad (10)$$

Experiment ((2))

Measurements

and

Uncertainties

engine\_team

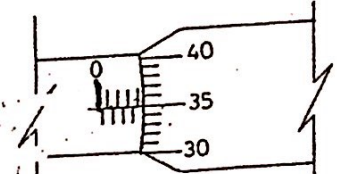
## Exp2: Measurements and uncertainties

\* هذه التجربة - دقة قوسية  $d$  (القطر)  $\rightarrow$  وسيت إبعادهم من خلال جهازين .  
 $h$  الارتفاع

الجهاز الأول **Micrometer (الميكرومتر)**

\* يتم من خلال جهاز الميكرومتر حساب الـ diameter  $(d)$   $d \pm \Delta d$

\* توضيح طريقة إبعاد  $d \pm \Delta d$



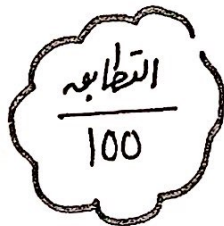
micrometer ↑  
(شكل الجهاز)

0.005 mm  
0.0005 cm

الافتقار  
نظرا الى المسطرة المدرجة (الرقعة من  
(و) ونقرأ عادي

نقرأ الى المسطرة غير المدرجة  
إذنا أن تكون (إذا لم يغير الترتيب  
0.5 (إذا استمر الترتيب  
بعد المسطرة المدرجة)

العامودي



ملاحظة :  $mm \rightarrow cm$   $\times 10^{-1}$

$\leftarrow$   
 $\times 10$

\* متى نضج جهاز micrometer كونه على شكل حرف (T) (أ) قلوباً



## [2] Vernier caliper

(الورنية)

العهاز الثاني

$$h \pm \Delta h$$

من خلال هذا الجهاز نحسب (height)

\* توضيح لمقاييس الأبعاد:

$$h \pm \Delta h$$

$$0.025 \text{ mm}$$

$$0.0025 \text{ cm}$$

$$* \left( \frac{\text{أول تطابقه}}{10} \right) + \text{نظرا إلى الصفر ونأخذ الرقم الذي}$$

قبله في غير المبرمج \*

ملاحظة: القراءة الناتجة بوحدة mm

وإذا طاب قول

$$\text{mm} \xrightarrow{10^{-1}} \text{cm}$$

ملاحظة مهمة جداً

عند إبعاد  $h$  بالتحديد إبعاد  
أو تطابقه دائماً تأخذ الرقم الذي  
يكون من جهة التدرج

\* ملاحظة: متى نقيس جهاز الورنية يكون على شكل مسطرة ( — ) فقط مستقيم

Ex 37]

### ⊗ Measurements and Uncertainties:

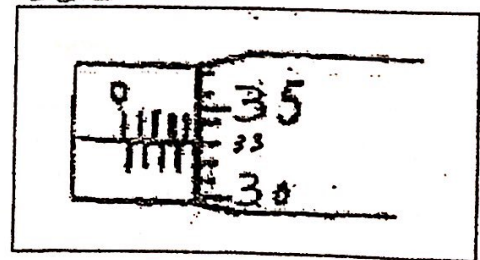
3- The diameter of a sphere was measured by the micrometer shown in the figure, the reading (in mm) is:

b) 5.33

(a) 4.33

d) 4.48

c) 4.44



ذكر في السؤال أن الجهاز (micro) ما يقا

Solution 8

$$4 + 0 + \frac{33}{100} = 4.33$$

قراءة المسطرة المبرمج + قراءة المسطرة عند المبرمج = قراءة المسطرة

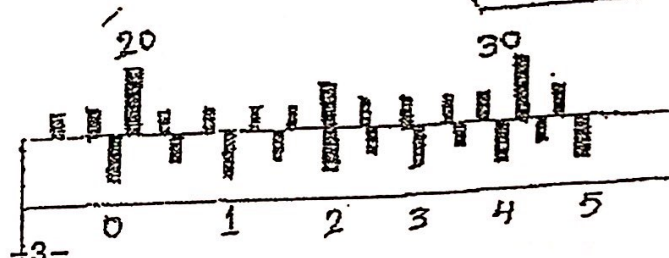
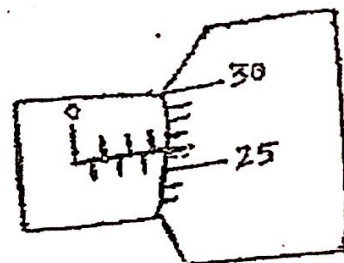
الفرقة الجواب

\* ملاحظة السؤال قبل ذلك d فقط

# Ex 38] MEASUREMENTS AND UNCERTAINTIES :

Give the reading for the following instruments

Mikrometer



a)  $\Rightarrow 3 + 0 + \frac{26}{100} = 3.26 \text{ mm}$

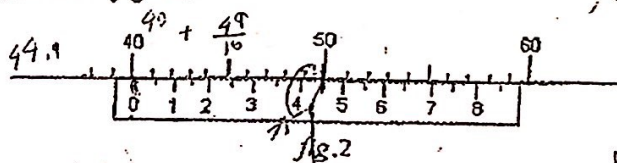
b)  $\Rightarrow \frac{2}{10} + 19 = 19.2 \text{ mm}$

نتبع الخطوات المذكورة و نقرأ أن نَحْسِنَ سَفِيًّا

The reading of the Vernier Caliper as shown in fig. 2 is:

Ex 39]

- (a)  $(4.020 \pm 0.0025) \text{ cm}$
- (b)  $(3.902 \pm 0.0025) \text{ cm}$
- (c)  $(4.045 \pm 0.0025) \text{ cm}$
- (d)  $(3.945 \pm 0.0025) \text{ cm}$



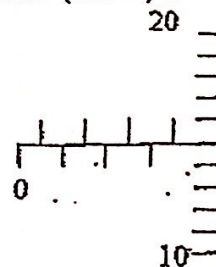
Solution:  $\frac{4.5}{10} + 40 = 40.45 \text{ mm} \Rightarrow \text{السؤال يطلب بـ cm} \Rightarrow 4.045$

$\Delta h \Rightarrow 0.0025 \text{ cm}$   $\Rightarrow h + \Delta h = (4.045 \pm 0.0025) \text{ cm}$

Ex 40]

7) In the figure, which of the following readings of micrometer (in mm) is correct?

- a)  $3.15 \pm 0.005$
- b)  $3.65 \pm 0.050$
- c)  $3.65 \pm 0.005$  ✓
- d)  $3.50 \pm 0.010$

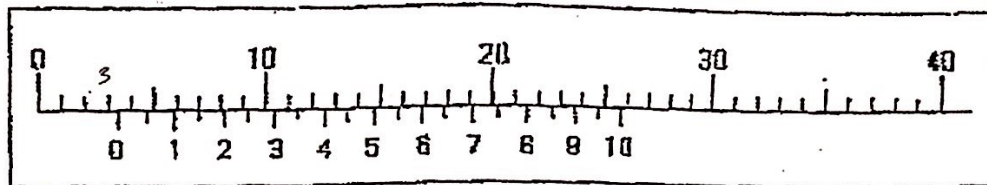


\*  $d \pm \Delta d \Rightarrow 3 + 0.5 + \frac{15}{100} = 3.65 \text{ mm}$   $\Rightarrow (3.65 \pm 0.005)$

$\Delta d \Rightarrow 0.005 \text{ mm}$



Ex 41] 3- The reading of the vernier caliper shown below is:  $0.315 \pm 0.0025 \text{ cm}$



\*  $h??$   $h = 3 + \frac{1.5}{10} = 3.15 \text{ mm} = 3.15 \times 10^{-1} = 0.315 \text{ cm}$

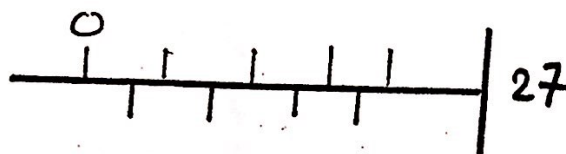
\*  $\Delta h \Rightarrow 0.0025 \text{ cm}$

Ex 42] The uncertainty in reading a micrometer in (cm) is:  
 a) 0.01 ☒ b) 0.005 ☒ c) 0.0005 ☒ d) None of the above.

# من الحفظ جواب فرغ

Ex 43]   
 \* The error in the Micrometer reading for a single measurement is:  $0.0005 \text{ mm}$   
 \* The error in the Vernier caliper is:  $0.025 \text{ mm} / 0.0025 \text{ cm} / 0.0005 \text{ cm}$

Ex 44] The diameter of a sphere is measured by micrometer  
 find the Volume of the sphere :



Solution:

$V \pm \Delta V$  المطلوب

$V = \frac{4}{3} \pi \left(\frac{d}{2}\right)^3$

$V = \frac{4}{3} \pi \left(\frac{4.27}{2}\right)^3$

$V = 40.7$

\*  $\Delta V = V \sqrt{\left(\frac{3\Delta d}{d}\right)^2 + (0)}$

$\Delta V = 40.7 \sqrt{\left(\frac{3 \times 0.0005}{4.27}\right)^2}$

$\Delta V = 0.142$

$d \pm \Delta d$

$\rightarrow 0.001 \text{ mm}$

$d = 4 + 0 + \frac{27}{100}$

$d = 4.27 \text{ mm}$

$V \pm \Delta V = 40.7 \pm 0.142$  ❌ "



Smallest deviation

\* تم سطر عجز الورنية والاعيار وسير \* بدنا نتحدث من

للحفظ:

[1] Ruler: Analytical : <sup>أقل قدر</sup>smallest deviation : 1mm  
وسية الخطأ دائماً 0.05cm حفظ #

[2] Caliper: Analytical : smallest deviation : 0.05mm  
وسية الخطأ : 0.025mm

micrometer: Analytical : smallest deviation: 0.01mm

[3] Digital balance & Digital : 0.01g  
نفسية الخطأ للميزان حفظ #

\*  $\frac{\text{أقل قدر}}{2} = \text{ملاحظة نسبة الخطأ}$

في جميع الأدوات الميزان نسبة الخطأ = أقل قدر

2-In an experiment to obtain the density of a cylinder, a student measures its diameter, height and mass that are: 10.0cm, 39.0cm, and 210.01g, respectively. The student uses measuring instrument: ruler and digital balance. If the length of ruler is, 20cm then the uncertainty in the density ( $\Delta\rho$ ) is: 0.6049 mg/cm<sup>3</sup>.

$$\rho_{\text{cylinder}} = \frac{4m}{\pi d^2 h} = \frac{4 \times 210.01}{39 \times 3.14 \times (10)^2} = 0.06 \text{ g/cm}^3$$

-  $\Delta m = 0.01 \text{ g}$  (لأنه استخدم digital Balance)  
 $\Delta \rho = \rho \sqrt{\left(\frac{\Delta h}{h}\right)^2 + \left(\frac{2\Delta d}{d}\right)^2 + \left(\frac{\Delta m}{m}\right)^2}$

-  $\Delta h = \Delta d = 0.5 \text{ mm} = 0.05 \text{ cm}$  (لأنه استخدم مسطرة)

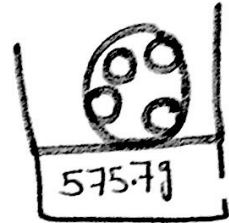
$$= 0.06 \sqrt{\left(\frac{0.05}{39}\right)^2 + \left(\frac{0.05 \times 2}{10}\right)^2 + \left(\frac{0.01}{210.01}\right)^2}$$

$$= 0.000604 \text{ g/cm}^3 \xrightarrow{\times 10^3} \text{mg/cm}^3 = 0.6049 \text{ mg/cm}^3$$

Ex\* If the ball shown on the digital scale moves with a velocity  
 $(10 \pm 1 \text{ m/s})$  the uncertainty in momentum in  $\text{kg m/s}$  is :  
 $* p = \text{mass} * v$

$$* \Delta p = m \Delta v \sqrt{\left(\frac{\Delta \text{mass}}{\text{mass}}\right)^2 + \left(\frac{\Delta v}{v}\right)^2}$$

$$\Delta m = 0.01 \text{ g}$$



digital balance

$$\Delta p = 10 \times 0.5757 \sqrt{\left(\frac{0.01}{575.7}\right)^2 + \left(\frac{1}{10}\right)^2}$$

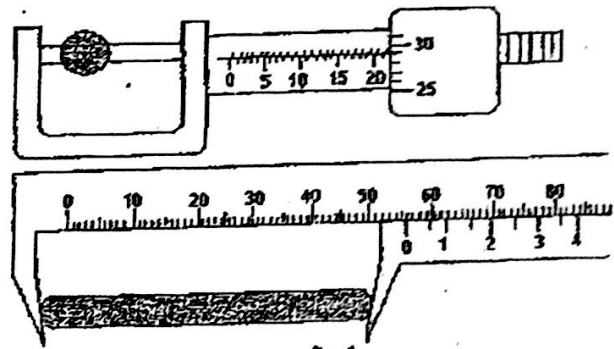
$$\Delta p = 0.5257 \text{ kg} \cdot \text{m/s}$$

الاجاب

هذا السؤال  
 يسأل عن  
 اختيار الجواب  
 الصحيح من بين  
 الخيارات

4. The diameter and height of a cylinder are given in fig.1. Find the volume (V) of the cylinder ( $\text{cm}^3$ ) if its mass is  $m \pm \Delta m = (26.33 \pm 0.02) \text{ g}$

- a) 1.44
- b) 18.3
- c) 20.6
- d) 1.3



$$V_{\text{cylinder}} = \pi h \frac{d^2}{4}$$

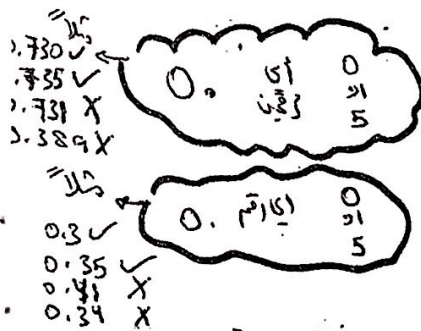
$$= \frac{3.14 \times (5.51) \times (2.179)^2}{4}$$

$$= 20.58 \approx 20.6 \text{ cm}^3$$

$$h = 55 + \frac{1}{10} = 55.1 \text{ mm} = 5.51 \text{ cm}$$

$$d = \frac{29}{100} + 21 + 0.5 = 21.79 \text{ mm} = 2.179 \text{ cm}$$

Which of the following represents a reading of micrometer  
 وأعطى بالقياسات هذه القراءات؟ Vernier caliper



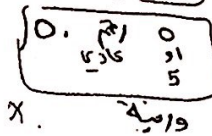
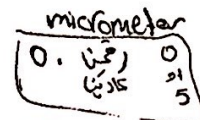
ملاحظات الحل:  
 قبول القراءات جميعها الى mm  
 في حال طلب في السؤال لا micrometer يجب ويبدو القياس التالى بالرقم  
 في حال طلب في السؤال لا Vernier caliper يجب ويبدو القياس التالى بالرقم

Ex: Which of the following represents a micrometer reading  
 (a)  $1 \times 10^{-3} \text{ m}$  (b)  $1.21 \times 10^{-1} \text{ mm}$  (c)  $1.21 \times 10^{-4} \text{ cm}$  (d) None of the above

(a)  $1 \times 10^{-3} \text{ m} = 1 \times 10^{-2} = 0.01 \text{ mm} \checkmark$

(b)  $1.21 \times 10^{-1} \text{ mm} = 0.121 \text{ mm} \times$

(c)  $1.21 \times 10^{-3} \text{ mm} = 0.00121 \text{ mm} \times$



في حال الى mm 2 في

لا جواب (a)

The sides of a rectangular plate measured by a vernier caliper were found to be 12.04 and 10.12 cm. The calculated error in the value of the plate's area in  $\text{cm}^2$  is:

- (a) 0.039 (b) 0.014 (c) 0.029 (d) None of the above

$$\Delta A = A \sqrt{\left(\frac{\Delta B}{B}\right)^2 + \left(\frac{\Delta C}{C}\right)^2}$$

$$= 121.84 \sqrt{\left(\frac{0.0025}{12.04}\right)^2 + \left(\frac{0.0025}{10.12}\right)^2}$$

$$= 0.0389 \approx 0.039 \text{ cm}^2$$

لا جواب (a)  $\checkmark$

$A = B * C$   
 A = المساحة  
 B = الطول  
 C = العرض

$A = 12.04 * 10.12 = 121.844$

$\Delta B = \Delta C = 0.0025 \text{ cm}$   
 لا تتغير  
 Vernier caliper





نأسف لتعذر كتابة الأسئلة بالسنوات عليها خلال سنة 2015 - 2016  
بسبب تعذر قيادة الرسات وخصوصية ذلك ولكن ...

للاستدلال على هذه التجربة فقام

وضع رسمه  
micrometer  
وطلب  $d \pm \Delta d$   
vernier caliper  
وطلب  $h \pm \Delta h$

في كل ... سؤال رسمه لجهاز ثم طلب  
Volume / لآلة او الاسطوانة  
لآلة الاسطوانة

او اي قواني  
قد اعطيتكم اياها / لآلة او الاسطوانة

\* في بعضنا للاستدلال بالسنوات قم وضع micrometer داخله  $d \pm \Delta d$  وطلب مساحة السطح فنقول مساحة السطح  $A \pm \Delta A$  ونجد  $d \pm \Delta d$  كما عرفنا

\* او في بعضنا الأفكار وضع ميزان في مثال سابقه

$C \pm \Delta C$   
او طلب متجه السطح =  $d \pm \Delta d$   
ونجد  $d \pm \Delta d$  كما نعرف

او سؤال: اكمنا لآلة تمثل قراءة ماكيروميتري ورنية  
كما في امثله سابقة

② او وضع بداخله دائرة وطلب مساحة الدائرة  $A \pm \Delta A$   
 $\pi d^2 / 4$

مساحة الدائرة =  $\pi d$   
ونجد  $d \pm \Delta d$

Experiment (3)

Vectors //

Force table

## Exp 3: Vectors, force Table

\* قوتون معطى (Forces)  $\left\{ \begin{array}{l} \text{مقدار : magnitude} \\ \text{اتجاه : direction} \end{array} \right.$   $\Rightarrow$  وطين قوتا القوة للحلقة : Resultant force

Equilibrium force (حين أن شهاتين القوتين متساويتان في المقدار ومعاكسان اتجاهًا).

\* ملاحظت: قوتی که Resultant force - مقدار - تحت الیه

لأما الخامس في حسب الربع

180 + 0R : الربع الاول : أما الربع ٤ فمبطل الربع

⇒ (مفظ)  $\boxed{\begin{array}{l} \text{الدرجة الأولى} \\ \text{الدرجة الثانية} \end{array}} \quad 0R + 180$

$R \pm 180^\circ$  ————— :  $On \pm 180^\circ$

عازال direction : (علافة الزاورة)

الإصلية:

$$x + \frac{1}{x^2} = y$$

هذه الزاوية  $\Rightarrow \theta' = \theta_R = \tan^{-1} \left| \frac{y}{x} \right| =$

11/11/1917

$$\phi' = f \cdot q_n^{-1} \mid y \mid$$
$$\textcircled{7} = 2^{-n} \left| \frac{1}{x} \right|$$

١٠ هي المرجعية == لاعاد الزمنية ==

DR

1. The first group of people who are likely to be affected by the proposed project are the local residents who live in the vicinity of the project site. These residents may be affected by the project in a number of ways, including increased traffic, noise, and air pollution. The project may also affect the local economy by creating jobs and increasing the demand for goods and services. The project may also affect the local environment by increasing the demand for water and electricity, and by increasing the amount of waste generated.

$1141$

$$\theta' = \tan^{-1} \left| \frac{y}{x} \right|$$
$$\theta = 180 + \alpha \approx 940^\circ 81'$$
$$V_R = 100 + 0 = 100$$

---

OR  $\theta' = \tan^{-1} \left| \frac{y}{x} \right|$

1.  $\frac{1}{x^2} = x^{-2}$

$$\Rightarrow \theta_R = 360 - \theta' = (0)^\circ \text{ or } 360^\circ$$

1. *Chlorophyll a* and *Chlorophyll b* were determined by the method of Arar and Collins (1971) using a Shimadzu 1601 UV-Visible Spectrophotometer. The concentration of chlorophylls was expressed in  $\mu\text{g mL}^{-1}$ .

---

مفاتيح الحيا - السعدان :

المجلس المشوري

[illegible]

# خيال و

0. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22. 23. 24. 25. 26. 27. 28. 29. 30. 31. 32. 33. 34. 35. 36. 37. 38. 39. 40. 41. 42. 43. 44. 45. 46. 47. 48. 49. 50. 51. 52. 53. 54. 55. 56. 57. 58. 59. 60. 61. 62. 63. 64. 65. 66. 67. 68. 69. 70. 71. 72. 73. 74. 75. 76. 77. 78. 79. 80. 81. 82. 83. 84. 85. 86. 87. 88. 89. 90. 91. 92. 93. 94. 95. 96. 97. 98. 99. 100. 101. 102. 103. 104. 105. 106. 107. 108. 109. 110. 111. 112. 113. 114. 115. 116. 117. 118. 119. 120. 121. 122. 123. 124. 125. 126. 127. 128. 129. 130. 131. 132. 133. 134. 135. 136. 137. 138. 139. 140. 141. 142. 143. 144. 145. 146. 147. 148. 149. 150. 151. 152. 153. 154. 155. 156. 157. 158. 159. 160. 161. 162. 163. 164. 165. 166. 167. 168. 169. 170. 171. 172. 173. 174. 175. 176. 177. 178. 179. 180. 181. 182. 183. 184. 185. 186. 187. 188. 189. 190. 191. 192. 193. 194. 195. 196. 197. 198. 199. 200. 201. 202. 203. 204. 205. 206. 207. 208. 209. 210. 211. 212. 213. 214. 215. 216. 217. 218. 219. 220. 221. 222. 223. 224. 225. 226. 227. 228. 229. 230. 231. 232. 233. 234. 235. 236. 237. 238. 239. 240. 241. 242. 243. 244. 245. 246. 247. 248. 249. 250. 251. 252. 253. 254. 255. 256. 257. 258. 259. 260. 261. 262. 263. 264. 265. 266. 267. 268. 269. 270. 271. 272. 273. 274. 275. 276. 277. 278. 279. 280. 281. 282. 283. 284. 285. 286. 287. 288. 289. 290. 291. 292. 293. 294. 295. 296. 297. 298. 299. 300. 301. 302. 303. 304. 305. 306. 307. 308. 309. 310. 311. 312. 313. 314. 315. 316. 317. 318. 319. 320. 321. 322. 323. 324. 325. 326. 327. 328. 329. 330. 331. 332. 333. 334. 335. 336. 337. 338. 339. 340. 341. 342. 343. 344. 345. 346. 347. 348. 349. 350. 351. 352. 353. 354. 355. 356. 357. 358. 359. 360. 361. 362. 363. 364. 365. 366. 367. 368. 369. 370. 371. 372. 373. 374. 375. 376. 377. 378. 379. 380. 381. 382. 383. 384. 385. 386. 387. 388. 389. 390. 391. 392. 393. 394. 395. 396. 397. 398. 399. 400. 401. 402. 403. 404. 405. 406. 407. 408. 409. 410. 411. 412. 413. 414. 415. 416. 417. 418. 419. 420. 421. 422. 423. 424. 425. 426. 427. 428. 429. 430. 431. 432. 433. 434. 435. 436. 437. 438. 439. 440. 441. 442. 443. 444. 445. 446. 447. 448. 449. 450. 451. 452. 453. 454. 455. 456. 457. 458. 459. 460. 461. 462. 463. 464. 465. 466. 467. 468. 469. 470. 471. 472. 473. 474. 475. 476. 477. 478. 479. 480. 481. 482. 483. 484. 485. 486. 487. 488. 489. 490. 491. 492. 493. 494. 495. 496. 497. 498. 499. 500. 501. 502. 503. 504. 505. 506. 507. 508. 509. 510. 511. 512. 513. 514. 515. 516. 517. 518. 519. 520. 521. 522. 523. 524. 525. 526. 527. 528. 529. 530. 531. 532. 533. 534. 535. 536. 537. 538. 539. 540. 541. 542. 543. 544. 545. 546. 547. 548. 549. 550. 551. 552. 553. 554. 555. 556. 557. 558. 559. 560. 561. 562. 563. 564. 565. 566. 567. 568. 569. 570. 571. 572. 573. 574. 575. 576. 577. 578. 579. 580. 581. 582. 583. 584. 585. 586. 587. 588. 589. 590. 591. 592. 593. 594. 595. 596. 597. 598. 599. 600. 601. 602. 603. 604. 605. 606. 607. 608. 609. 610. 611. 612. 613. 614. 615. 616. 617. 618. 619. 620. 621. 622. 623. 624. 625. 626. 627. 628. 629. 630. 631. 632. 633. 634. 635. 636. 637. 638. 639. 640. 641. 642. 643. 644. 645. 646. 647. 648. 649. 650. 651. 652. 653. 654. 655. 656. 657. 658. 659. 660. 661. 662. 663. 664. 665. 666. 667. 668. 669. 670. 671. 672. 673. 674. 675. 676. 677. 678. 679. 680. 681. 682. 683. 684. 685. 686. 687. 688. 689. 690. 691. 692. 693. 694. 695. 696. 697. 698. 699. 700. 701. 702. 703. 704. 705. 706. 707. 708. 709. 710. 711. 712. 713. 714. 715. 716. 717. 718. 719. 720. 721. 722. 723. 724. 725. 726. 727. 728. 729. 730. 731. 732. 733. 734. 735. 736. 737. 738. 739. 740. 741. 742. 743. 744. 745. 746. 747. 748. 749. 750. 751. 752. 753. 754. 755. 756. 757. 758. 759. 760. 761. 762. 763. 764. 765. 766. 767. 768. 769. 770. 771. 772. 773. 774. 775. 776. 777. 778. 779. 780. 781. 782. 783. 784. 785. 786. 787. 788. 789. 790. 791. 792. 793. 794. 795. 796. 797. 798. 799. 800. 801. 802. 803. 804. 805. 806. 807. 808. 809. 810. 811. 812. 813. 814. 815. 816. 817. 818. 819. 820. 821. 822. 823. 824. 825. 826. 827. 828. 829. 830. 831. 832. 833. 834. 835. 836. 837. 838. 839. 840. 84

Scanned by

Scanned by

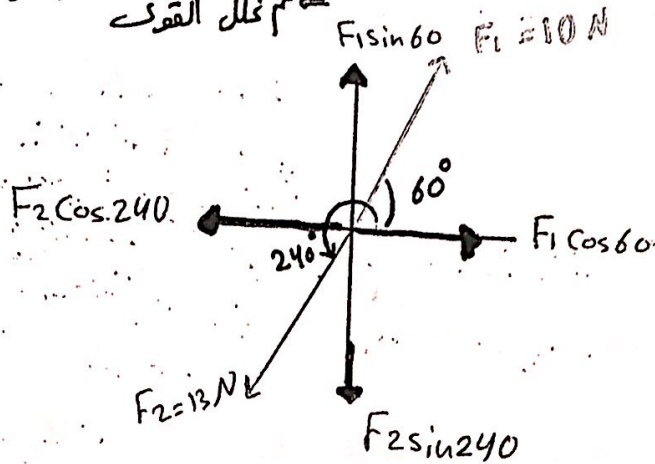


2) In force table experiment. The magnitude and direction of equilibrant force (قوة موازنة) for a system consist of two forces;  $[F_1] = 10 \text{ N}$ ,  $\theta_1 = 60^\circ$  and  $[F_2] = 13 \text{ N}$ ;  $\theta_2 = 240^\circ$  will be:

- a)  $3 \text{ N}$ ,  $240^\circ$     **b)  $3 \text{ N}$ ,  $60^\circ$**     c)  $2 \text{ N}$ ,  $60^\circ$     d)  $2 \text{ N}$ ,  $240^\circ$

Solution:

مبنى فل السؤال بنمثل القوى على المحاور  
ثم نحلل القوى



$\sum F_x$  (مجموع القوى على x)

$$\Rightarrow (F_1 \cos 60) + (F_2 \cos 240)$$

$$\Rightarrow (10 \cos 60) + (13 \cos 240)$$

$$\Rightarrow 5 + -6.5$$

$$F_x \Rightarrow -1.5 \text{ N } (-\hat{i})$$

ملاحظة صدنا الاتجاه حسب القوة الاكبر

$$6.5 > 5$$

نغير الإشارة

$$\vec{F} = -1.5\hat{i} - 2.6\hat{j}$$

$\sum F_y$  (مجموع القوى على y)

$$\Rightarrow (F_1 \sin 60) + (F_2 \sin 240)$$

$$\Rightarrow (10 \sin 60) + (13 \sin 240)$$

$$\Rightarrow 8.66 + -11.258$$

$$\Rightarrow \sum F_y = -2.59 \approx -2.6 (-\hat{j})$$

له صدنا الاتجاه لان 11.258 > 8.66

نغير الإشارة

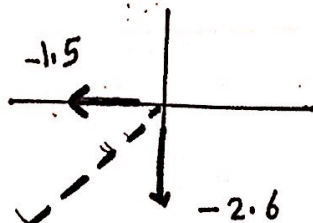
$$\text{mag} = \sqrt{(\sum F_x)^2 + (\sum F_y)^2}$$

$$= \sqrt{(-1.5)^2 + (-2.6)^2}$$

$$F_{eq} = 3 \text{ N}$$

(ملاحظة)

(الربع الثاني)



$$\theta' = \tan^{-1} \left| \frac{y}{x} \right| = \tan^{-1} \left| \frac{-2.6}{-1.5} \right| = 60^\circ$$

$$\theta' = 60^\circ \Rightarrow \text{الربع الثالث} = 180 + 60 = 240^\circ$$

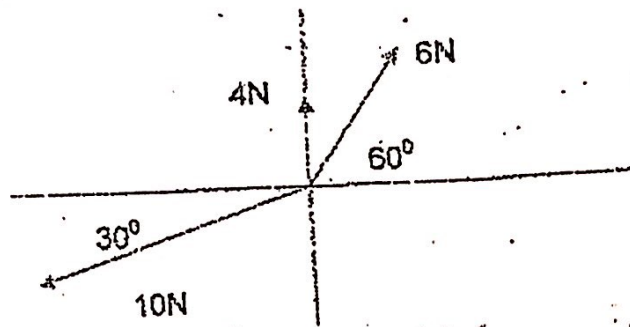
below -x -axis

$$2 \text{ N}, 60^\circ$$

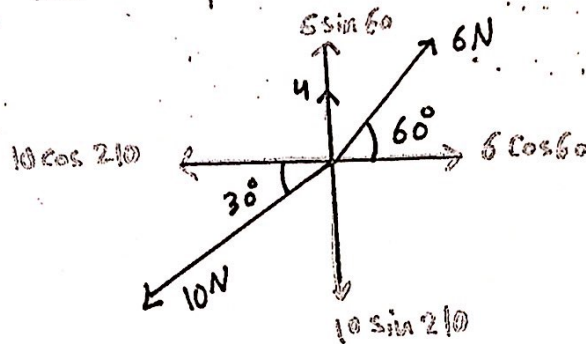
$$\text{equilibrant} = 180^\circ + 60^\circ = 240^\circ$$

5- In the figure shown, the magnitude of the additional force that should be added to get the system in equilibrium is: (2 marks)

- a) 7.7N    **b) 7.1N**    c) 6.6N    d) 5.7N    e) 2.3N



Solution:



$$\Rightarrow \sum F_x$$

$$\Rightarrow 6 \cos 60 + 10 \cos 30$$

$$\Rightarrow 3 + -8.7$$

$$\Rightarrow -5.7 \text{ N} (-)$$

$$\sum F_y \Rightarrow 4 + 6 \sin 60 + 10 \sin 30$$

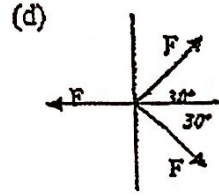
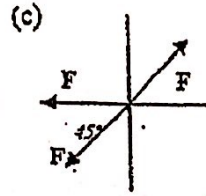
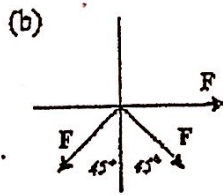
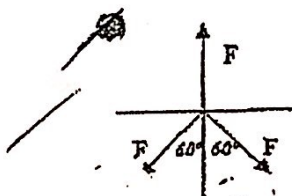
$$\Rightarrow 9.196 + -5$$

$$\Rightarrow 4.196 \text{ N } (+)$$

$$|\vec{F}|_{\text{equ}} \Rightarrow \sqrt{(-5.7)^2 + (4.196)^2} = 7.077 \approx 7.1 \text{ N}$$

النتيجة النهائية هي 7.1N

10. The system that is under equilibrium is:



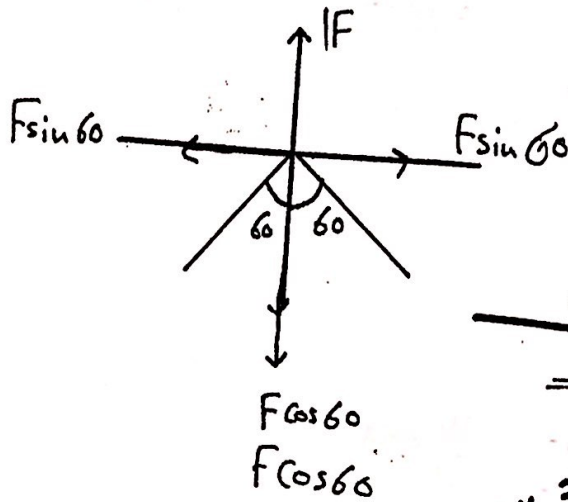
\* البواب خرجي A

توضيح طريقة الحل في الملف



\* في هذا السؤال نطلب منا النظام الذي هو في اتزان  $\parallel$  equilibrium  $\parallel$  ؟

مقدار يكون في اتزان إذا  $\Sigma F_x = \text{zero}$   
 $\Sigma F_y = \text{zero}$



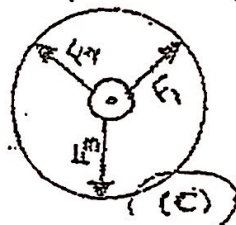
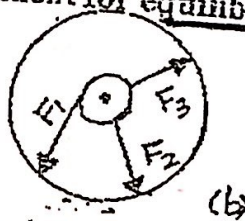
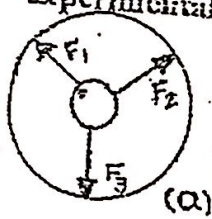
$\Rightarrow \Sigma F_x = 0$

$\Rightarrow F \cos 60 + F \cos 60 \Rightarrow \underline{\underline{1F}}$  مع  $\underline{\underline{1F}}$

$\Sigma F_y = 0$

\* القوى متساوية مقداراً متعاكسة اتجاهاتاً  $\parallel$

18. which of the following figures represents the correct experimental arrangement for equilibrium:



الاجابة هي (c)  $\parallel$  الامتحان ١٩٩١

University of...

في هذا السؤال قيم القوى واتجاهاتها ناقصة لذلك من الصعب التوصل الى خيار  $\parallel$  الامتحان ١٩٩١

1. VECTORS:

a- According to the corresponding figure (1)

$\vec{A} + \vec{B} + \vec{C} + \vec{D} = \underline{\underline{0}}$  (2, 0)

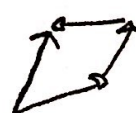
$\vec{A} + \vec{B} + \vec{C} = \underline{\underline{-\vec{D}}}$

$\vec{A} + \vec{B} + \vec{C} + \vec{D} = \text{zero}$

$\vec{A} + \vec{B} + \vec{C} = -\vec{D} \Rightarrow$

السبب محصلة  $\vec{A}$  و  $\vec{B}$  و  $\vec{C}$

رسم ذلك الاول الى رأس الارض  $\rho$  واذن  $\underline{\underline{\rho}}$  ولكن في الرسمة معكوسة بـ  $-\vec{D}$



3) The major source of inaccuracy in force table experiment is:

- a) personal error
- b) random error
- c) systematic error
- d) none of the above

الإجابة هي (c) لأن البب الوثيقي هو ال friction وهو بب (systematic) الأداة



Ex: In the force Table experiment, suppose that you were told to put 100g at  $45^\circ$  and 150g at  $135^\circ$ . A third force that is needed to have the system of all three forces in equilibrium has magnitude and direction that are given by: (Acceleration due to gravity  $g \approx 10 \text{ m/s}^2$ )

$$F = 1.8 \text{ N}, \theta = 281^\circ$$

Solution:  $m_1 = 100\text{g}$

$$\theta = 45^\circ$$

$$F_1 = m_1 g$$

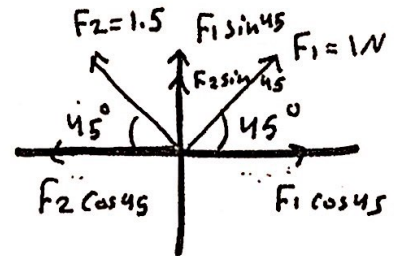
$$F_1 = \frac{100}{1000} * 10 = 1\text{N}$$

$m_2 = 150\text{g}$

$$\theta = 135^\circ$$

$$F_2 = m_2 g$$

$$= \frac{150}{1000} * 10 = 1.5\text{N}$$



$$\Rightarrow \Sigma F_x = (F_2 \cos 45) - (F_1 \cos 45)$$

$$\Sigma F_x = 0.35 \text{ (-)}$$

$$\Rightarrow \Sigma F_y = (F_1 \sin 45) + (F_2 \sin 45)$$

$$\Sigma F_y \approx 1.8 \text{ N}$$

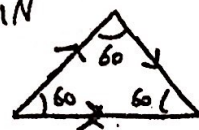
$$\Rightarrow |F| = \sqrt{(0.35)^2 + (1.8)^2} \approx 1.8\text{N}$$

$$\star \text{ direction: } \theta' = \tan^{-1} \left| \frac{1.8}{0.35} \right| \Rightarrow 78.9 \approx 79^\circ \Rightarrow 180 - 79^\circ = 101^\circ$$

$$180 + 101 = 281 \text{ } \Leftarrow \text{ equilibrium}$$

Ex: The resultant force in the figure show:

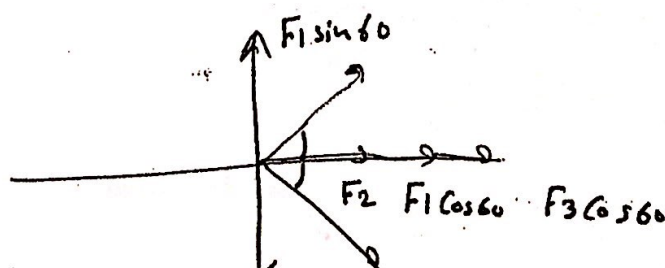
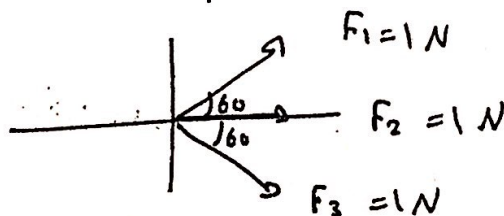
$$F_1 = 1\text{N}$$



$$F_3 = 1\text{N}$$

$$F_2 = 1\text{N}$$

Solution:



بنظام القوى

7

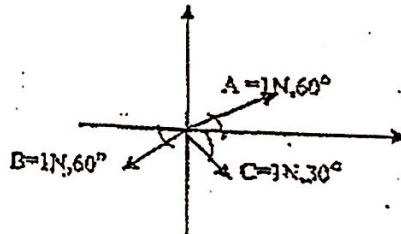
$$\Sigma F_x = (F_2) + (F_1 \cos 60) + (F_3 \cos 60) = 2N$$

$$\Sigma F_y = F_1 \sin 60 - F_3 \sin 60 = 0$$

$$|\vec{F}| = \sqrt{(\Sigma F_x)^2 + (\Sigma F_y)^2} = \sqrt{(2)^2 + (0)^2} = \sqrt{4} = 2N$$

3) In the force table experiment, three forces A, B, C with magnitudes and directions are shown in the figure. The magnitude and direction of equilibrium force:

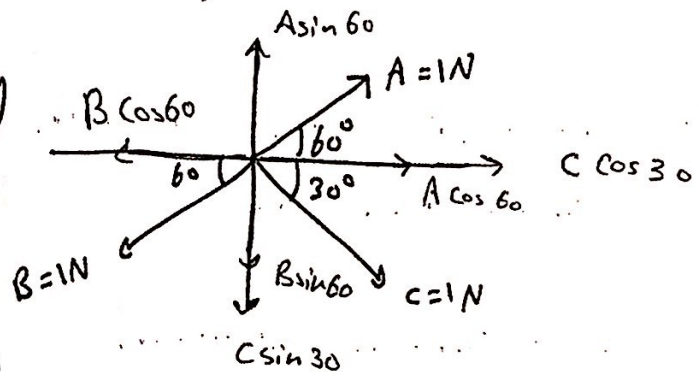
- a) 2,  $15^\circ$       b) 1,  $330^\circ$   
c) 1.7,  $330^\circ$       d) 1,  $150^\circ$



Solution:

$$\Sigma F_x = (1 \cos 60 + 1 \cos 30) - (1 \cos 60)$$

$$\Sigma F_x = 0.87 N (\hat{i})$$



$$\Sigma F_y = (\sin 60 + \sin 30) - (\sin 60)$$

$$\Sigma F_y = 0.5 N (-\hat{j})$$

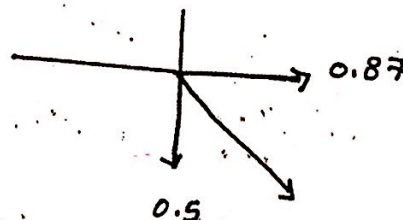
$$|\vec{F}| = \sqrt{(0.5)^2 + (0.87)^2} = 1N$$

$$\theta = \tan^{-1} \left( \frac{0.5}{0.87} \right) = 29.88^\circ \approx 30^\circ$$

$$\theta = 360^\circ - 30^\circ = 330^\circ$$

$$= 330^\circ - 180^\circ = 150^\circ$$

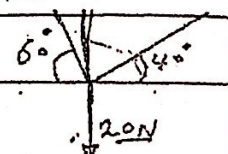
له زاوية الاتزان.



الربع الرابع

اذل الجواب  $150^\circ$

Ex: ~~For Table force: A body is said to be in equilibrium if~~  
~~a) it has acceleration.~~ ~~b) The resultant force equal to zero.~~  
~~c) all the applied forces are along the same line~~  
~~d) all the applied forces are equal.~~



b) The resultant force equal to zero.



## 2- Vector

Ex

- ① ⊗ The major error in this experiment is that due to frictional forces [ ] ~~yes~~
- ② ⊗ Using force table, one can directly measure the resultant [ ] ~~yes~~ No
- ③ ⊗ The method of components to find a resultant is not as accurate as the force table [ ] No

①

Frictional  
forces

المب (الرئيس) للتأ في تجريبه  
vectors  
(force table)

②

\* لأن في التجريب القوة التي نتجها  
على إيجابتها هي Equ force  
مباشرة

③

خطأ: لأن التحليل نظرياً أدق من استخدام Force Table

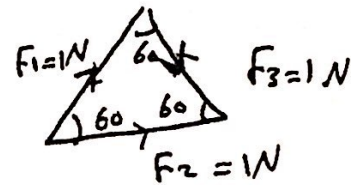
Ex: The resultant force of the three forces shown in fig shown below:

a 2 N in the -ve x - axis

ⓑ 2 N in the +ve x - axis

c 1 N in the -ve x - axis

d 1 N in the +ve x - axis



\* في كل السؤال نفس الفكرة \*  
ولكن في direction



7. A system consists from two forces  $\vec{F}_1 = (7\hat{i} + 8\hat{j})N$  and  $\vec{F}_2 = (3\hat{i} - 5\hat{j})N$ . The equilibrant force (القوة الموازنة) for the two forces is:

a)  $(-10\hat{i} - 3\hat{j})N$

b)  $(4\hat{i} - 13\hat{j})N$

c)  $(10\hat{i} + 3\hat{j})N$

d)  $(-4\hat{i} + 13\hat{j})N$

Solution:  $|\vec{F}| = \Sigma F_x + \Sigma F_y$   
 $= (7\hat{i} + 3\hat{i}) + (8\hat{j} + -5\hat{j})$   
 $= (10\hat{i} + 3\hat{j})N$

6. The magnitude of the resultant force of the system shown in fig. 2 is:

a)  $3.0mg$

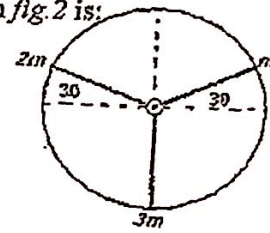
b)  $2.2mg$

c)  $1.7mg$

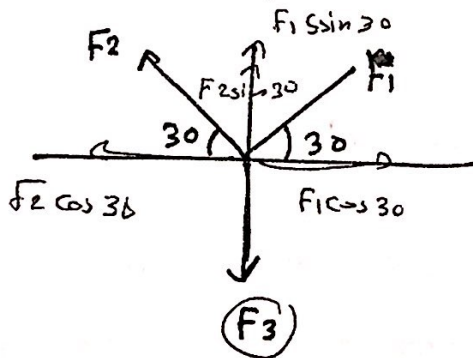
d)  $6.0mg$

~~e) can not be determine~~

نوع  
الاجواب



$2m \sin 30$



$(m) \rightarrow F_1 = mg$

$(2m) \rightarrow F_2 = 2mg$

$(3m) \rightarrow F_3 = 3mg$

$$\Rightarrow \Sigma F_x = (2mg \cos 30 - mg \cos 30)$$

$$\Sigma F_x = \cos 30 g m (2 - 1)$$

$$\Sigma F_x = 0.87 g m$$

$$\Rightarrow \Sigma F_y = (3mg - (mg \sin 30 + 2mg \sin 30))$$

$$\Sigma F_y = (3mg - 3mg \sin 30)$$

$$\Sigma F_y = 3mg (1 - \sin 30)$$

$$\Sigma F_y = 1.5mg$$

$$\Rightarrow |\vec{F}| = \sqrt{(0.87 mg)^2 + (1.5 mg)^2} = 1.7mg$$

(الاجابه هـ)

11m

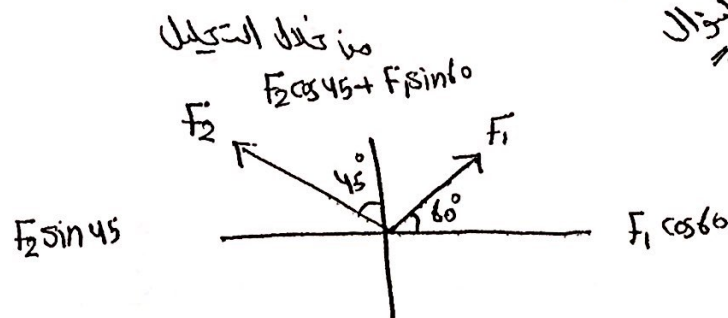
- i) Two forces are applied to the ring of force table. If  $\vec{F}_1$  at an angle  $60^\circ$ , and  $\vec{F}_2$  at  $135^\circ$ , the equilibrium force will be on the negative y-axis when; 2 Marks

(a)  $m_1 = \frac{1}{2} m_2$

(b)  $m_1 = \frac{1}{\sqrt{2}} m_2$

(c)  $m_1 = 2m_2$

(d)  $m_1 = \sqrt{2} m_2$



equilibrium :  $\sum F_x = 0$

$\sum F_x = 0 \Rightarrow$

$F_1 \cos 60 = F_2 \sin 45$

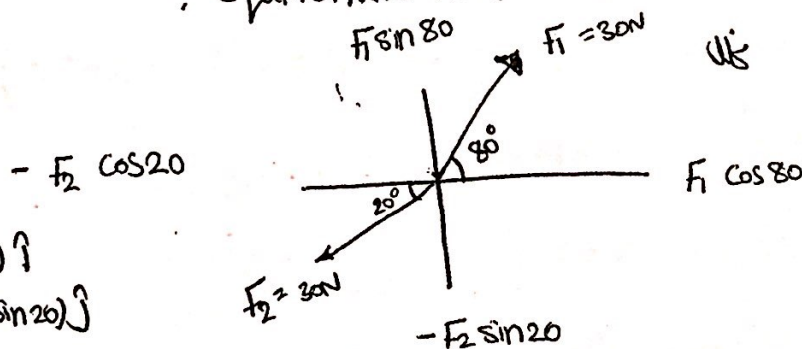
$m_1 g \cos 60 = m_2 g \sin 45$

$m_1 = \frac{\sin 45}{\cos 60} m_2$

$m_1 = \sqrt{2} m_2$

EX<sub>1</sub> In the force table experiment  $|\vec{F}_1| = |\vec{F}_2| = 30\text{N}$  are directed as  $80^\circ$  and  $200^\circ$  respectively. The direction of the third force  $\vec{F}_3$  in (N) which balances the two forces  $\vec{F}_1$  and  $\vec{F}_2$  is:

: equilibrium force



$\vec{F}_R = (F_1 \cos 80 - F_2 \cos 20) \hat{i} + (F_1 \sin 80 - F_2 \sin 20) \hat{j}$

$= -22.98 \hat{i} + 19.28 \hat{j}$

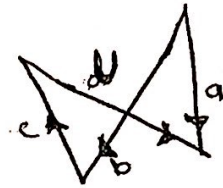
$\theta = \tan^{-1} \left| \frac{19.28}{-22.98} \right| = 39.99^\circ$

$\theta_R = 180 - 39.9 = 140.1^\circ$

$\theta_{eq} = 140.01 + 180 = 320^\circ$

EX<sub>2</sub>  
فایل  
الاجابة  
2016

Find the vector  $U$  in the figure in terms of vectors  $a, b, c$

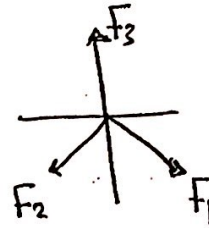


EX<sub>4</sub> Find the Resultant force for the three forces in the figure

$F_1 = F_2 = 30\text{ N}$  ,  $F_3 = 10\text{ N}$  ,  $\theta_1 = 315^\circ$  ,  $\theta_2 = 225^\circ$

ميدان  
الاجابة  
2016

32.4 N : الاجابة  
بالمتكامل  
في  
ميدان  
الاجابة



EX<sub>5</sub> In the previous questions what's the direction of the equilibrium force?

الاجابة :  $90^\circ$   
بالمتكامل في الميدان

EX<sub>6</sub> one student found the resultant direction of two vectors in second quarter the direction of equilibrium force vector equal  $\Rightarrow$

ميدان  
الاجابة  
2016

(a)  $\theta_{eq} = \theta_R$  (b)  $\theta_{eq} = 180 - \theta_R$

الخيار

(c)  $\theta_{eq} = \theta_R + 180$  (d)  $\theta_{eq} = -\theta_R$

الاجابة  
في  
ميدان

EX<sub>6</sub> In an experiment, one student found the resultant direction of two vectors in first quarter, the direction of equilibrium force vector equal;

فایل  
الاجابة  
2015

$\theta_{eq} = \theta_R + 180$  : الاجابة

(12)



EX7 Which of the following diagrams represents

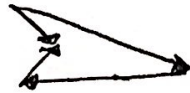
$$\vec{U} - \vec{a} = -\vec{b} - \vec{c}$$

فاينال الصغ  
التي  
سنة  
2015

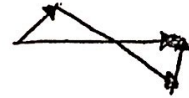
9



10



11



12



EX8 generally speaking, If the balance force makes an angle  $\theta$  relative to x-axis, then the resultant force will be:

سنة  
2016

(a)  $\theta + 180$

(c)  $\theta + 180$

(b)  $\theta + 360$

(d) both (a) and (c) are correct

الاجابة

$$\theta_R + 180 = \theta_1 + \theta_2 \quad \text{و} \quad \theta_R \pm 180 = \theta_1 + \theta_2$$

$$\theta_R - 180 = \theta_1 + \theta_2$$

EX9 two forces, one of magnitude 2N and the other of magnitude 3N, are applied to the ring of a force table. the directions of both forces are unknown, which best direction the Limitations in R the resultant?

R من 2N إلى 3N

(a)  $R \leq 5N$

(b)  $5N \leq R \leq 11N$

(c)  $R > 3N$

(d)  $1N \leq R \leq 5N$

(e)  $R \leq 2N$

الاجابة

الاجابات

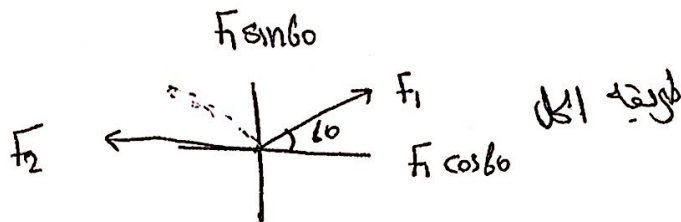
نتيجة التوقيت

نتيجة التوقيت

13

EX<sub>10</sub> Two forces are applied to the ring of force table  
 If  $\vec{F}_1$  at an angle  $60^\circ$  and  $\vec{F}_2$  at  $180^\circ$ , the equilibrium force will be in the negative y-axis when

- (a)  $m_1 = 2m_2$  (b)  $m_1 = \sqrt{2}m_2$  (c)  $m_1 = \frac{1}{2}m_2$   
 (d)  $m_1 = \frac{1}{\sqrt{2}}m_2$



equilibrium  $\Rightarrow F_1 \cos 60 = F_2$   
 $m_1 g \cos 60 = m_2 g$   
 $m_1 \times \frac{1}{2} = m_2$   
 $\Rightarrow m_1 = 2m_2$

EX<sub>11</sub>  $F_1 = F_2 = 30\text{N}$  are directed at  $90^\circ$  and  $210^\circ$  respectively  
 the direction of the third force  $F_3$  which balance the two forces  $F_1$  &  $F_2$  is :

$330^\circ$

موازاة المتجهين الآخرين

EX<sub>12</sub> A system of forces consists of  $\vec{F}_1$  (7N with  $75^\circ$ )  
 and  $\vec{F}_2$  (5N with  $255^\circ$ )

then the magnitude of the third force  $F_3$  which balance  $F_1$  /  $F_2$  is :

2N with  $255^\circ$

بالتضاد

(14)

Experiment (4)

# Kinematics of Rectilinear Motion



# Exp 4: Kinematics of Rectilinear Motion:

٣٢٣

\* ١. لعاطِلِبِ فِى السَّوَالِ (Total distance) : المسافة هي نصفها المسافة تحت المنحنى حسب السرعة في المستوي (المركبات) بنمى  
علاقت: مسافة المثلث:  $\frac{1}{2} \times \text{طول القاعدة} \times \text{الارتفاع}$   
مسافة المربع = (طول الضلع)  $\times$  (عدد المثلثات)

التحليل الأول

\* مسافة المستطيل = (الطول  $\times$  العرض)  
\* وحدة المسافة: إما (cm أو m) حسب المسألة  
\* المطلوب في السؤال: Velocity (السرعة) في السؤال أو حسب الوحدة

\* ٢. لعاطِلِبِ ٨

instantaneous velocity

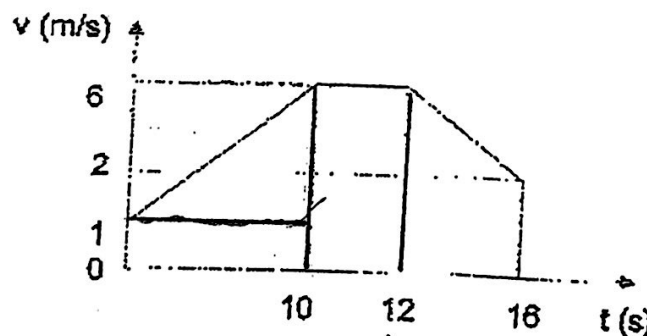
\* السرعة اللحظية  
\* نشتق الزمن المطلوب عند السرعة ونوصل خطاً مع هذا الزمن حتى يتم التقاطع مع الرسم.

\* ٣. إذا طُلب: Average acceleration

$$\bar{a} = \frac{\Delta V}{\Delta t} = \frac{\text{التغير في السرعة}}{\text{التغير في الزمن}} = \frac{V_f - V_i}{t_f - t_i} \quad (\text{m/s}^2)$$

Ex:

6- In the experiment on the Kinematics of Rectilinear Motion, the following velocity versus time graph was obtained as below. Use this figure to answer the following questions:



a) The total distance traveled in the first 12 seconds is: (2 marks)  
a) 35m b) 25m c) 47m d) 35m<sup>2</sup> e) 47m<sup>2</sup>

b) The average acceleration in the time interval  $t = 0$  to  $t = 12$  second is (2 marks)  
a) 1.5ms<sup>-2</sup> b) 0.75 ms<sup>-2</sup> c) 0.51 ms<sup>-2</sup> d) 0.06 ms<sup>-2</sup>  
e) 0.42 ms<sup>-2</sup>

c) the instantaneous velocity at time = 10 sec

Solution; a Total distance?? in the first 12 sec

كما ذكرنا المسافة هي المسافة تحت المنحنى وحسب السؤال المسافة أول 12 ثانية  
بالتالي بنجز المسافة من 0 إلى 10 ومن 10 إلى 12

نلاحظ أننا سنجز المسافة من 0 إلى 10 في شكلين: مستطيل و مثلث

مساحة = الطول × العرض

مساحة =  $\frac{1}{2} \times \text{طول القاعدة} \times \text{الارتفاع}$

مساحة =  $10 \times 1 = 10 \text{ m}$

مساحة =  $\frac{1}{2} \times 10 \times (6 - 1) = \frac{1}{2} \times 10 \times 5 = 25 \text{ m}$

(10 إلى 12)

مساحة المستطيل = الطول × العرض

=  $6 \times (12 - 10)$

=  $6 \times 2$

=  $12 \text{ m}$

\* نجمع المسافات التي يقربها المسافة :

$25 + 10 + 12 = 47 \text{ m}$

∴ Total distance = 47 m

b  $a = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i} = \frac{6 - 1}{12 - 0} = \frac{5}{12} \approx 0.42 \text{ m/s}^2$

ملاحظة: مثلًا عند الزمن 12 بفرضنا حتى نقطه الرسم وبالتالي نقطة التقاطع هي السرعة للرد وهي 6 على بسبب المثال

c  $6 \text{ m/s}$

النكاح الثاني: مستطيلات

\* الفكرة الثانية: شبيهة بالفكر الأول يكون معطى إلى المستوى الدينامي رسمه اعده بين (v-t) السرعة والزمن

نفس الطريقة الأولى (مساحة المستطيلات)

Total distance =

instantaneous Velocity

Avg velocity

عن نقطة معينة

إذا كانت السرعة المطلوبة عند زمن بين المستطيلات

إذا كانت السرعة المطلوبة زمن موجود عند الأطراف

في حال كان instant : يعمل بين نقطتين المستطيلات



2. تاج شرح هذا الشكل عند لحظة معينة (الاسترخاء)

1. لو طلبنا Avg Velocity عند لحظة معينة ← نرى هذه النسبة (ممكن وجودها بالنسبة المثلث)

بأنفسها

على الحافة. نأخذ الحافة اليمنى ونؤخذها

1. لو طلبنا Inst velocity عند لحظة معينة ← نرى هذه النسبة (ممكن وجودها)

بأنفسها

على الحافة. نعمل بين انصاف المستطيلات

Find Avg velocity at  $t = 3 \text{ sec}$

Find inst velocity at  $t = 3 \text{ sec}$

$$\text{Avg } a = \frac{b - a}{b - a}$$

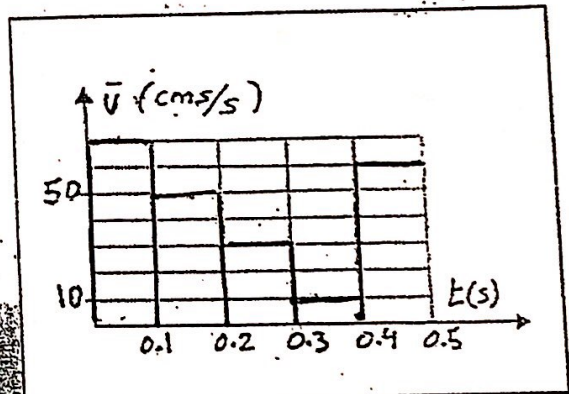
$$\text{Avg } a = \frac{v(t=b) - v(t=a)}{b - a}$$

هنا طريقة الحل تختلف تب موقع النانبة بالنسبة للمستطيلات ... في هذا الشكل ذلك

# x: Kinematics of Rectilinear Motion:

5- In the experiment of one dimensional rectilinear motion, the figure shows a histogram plot of  $\bar{v}$  versus  $t$ . then the instantaneous velocity at  $t = 0.3 \text{ s}$  is:

- b) 30 cms/s
- a) 10 cms/s
- d) 35 cms/s
- c) 20 cms/s



\* چون طلب السرعة اللحظية عند الزمن 0.3 وجاءت عند الاطراف  
instant

20 ← بنعمل سلم من نصف المستطيل الاول الى نصف المستطيل الثاني  
0.2 0.3 0.4 ← ومدة 0.3 بنمدها من 0.2 حتى يتقاطع مع السلم

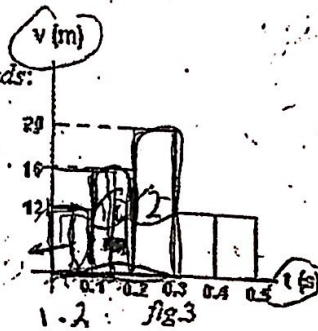
← نبشوف السرعة المقابلة لهذه التقاطع وهي 20



In the "Kinematics of Rectilinear Motion" experiment; depending on fig.3; answer questions 6 and 7.

6. The distance (in m) traveled in the first 0.3 seconds:

- (a) 4.8  
(b) 6.0  
(c) 1.2  
(d) 1.6



(0 → 0.3) sec

\* طلب في السؤال distance في نفس المساحة

0 → 0.1  
مساحة المستطيل = الطول × العرض

$$0.1 \times 12 = 1.2$$

0.1 → 0.2  
مساحة المستطيل = الطول × العرض

$$0.1 \times 16 = 1.6$$

0.2 → 0.3

الطول × العرض =

$$0.1 \times 20 = 2$$

$$\text{distance} = 1.2 + 1.6 + 2 = 4.8 \text{ m}$$

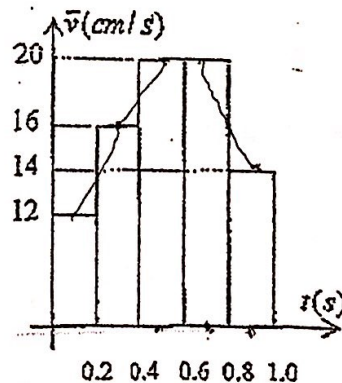
ج ٤

In the Kinematics of Rectilinear Motion experiment, the following velocity versus time graph was obtained as below. Use this figure to answer questions from 6 to 9.

4 Marks

6) The total distance travelled in the first 0.3 seconds is:

- (a) 7.6 cm  
(b) 7.6 cm<sup>2</sup>  
(c) 4 cm  
(d) 4 cm<sup>2</sup>



7) The instantaneous velocity at t=0.9sec is:

- (a) 20 cm/s  
(b) 14 cm/s  
(c) 16 cm/s  
(d) can not be determined

8) The average acceleration of the object on the time interval (0.5sec - 0.7sec) is:

- (a) 0 cm/s<sup>2</sup>  
(b) -30 cm/s<sup>2</sup>  
(c) 20 cm/s<sup>2</sup>  
(d) 30 cm/s<sup>2</sup>

9) The average velocity at t=0.8sec is:

- (a) 14 cm/s  
(b) 16 cm/s  
(c) 12 cm/s  
(d) can not be determined

solution: 6) Total distance  $\Rightarrow 0.2 \rightarrow 0.3$   
 مسافة المسير = الطول \* العرض  
 $0.2 * 12 = 2.4$   
 $0.2 \rightarrow 0.3$   
 الطول \* العرض  
 $= 0.1 * 16 = 1.6$   
 $2.4 + 1.6 = 4 \text{ cm}$   
 خرج  $\underline{4}$

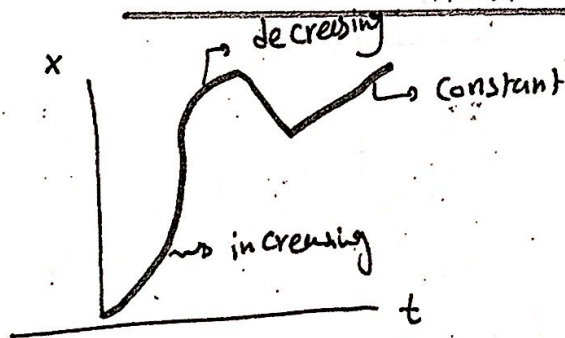
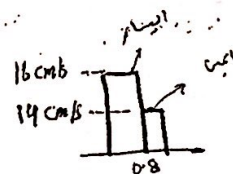
7)  $0.9 \Rightarrow$  هذا الزمن جاد بالمتوسط بالتاي :  
 نبطل هيك وينطلع السرعة

البيان :  $14 \text{ cm/s}$  خرج (b)

8)  $\bar{a} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i} = \frac{20 - 20}{0.7 - 0.5} = \frac{0}{0.2} = \text{Zero}$

9)  $14 \text{ cm/s} \Rightarrow$  average velocity

كل انفا على الحواف نري  
 Inst v : نضل بين انصاف المستطيلات  
 Avg v : ايمى  
 هنا Avg لذلك ايمى :  $14 \text{ cm/s}$



\* الفقرة الثالثة :

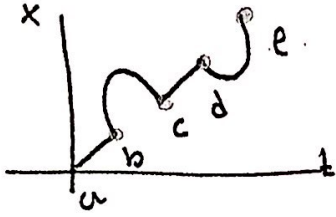
ملاحظة :  
 decreasing :  $\searrow$   
 increasing :  $\nearrow$   
 constant : ثابت

بجانب معطيات على المستوى الكهربائي بيه  
 $\underline{x}$  (distance) و  $\underline{t}$  (time) مسافات  
 لخصت سرعة الجسم (Velocity)  
 Partick

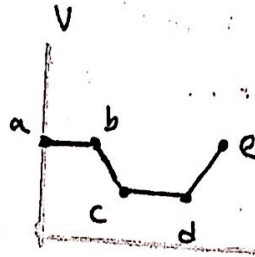
constant — increase U { (decrease)  $\cap$



Ex: Plot graph represent speed versus time and show all points on graph



Solution:



الشكل التالي

\* الفكرة الرابع: بدون معطيات سرية ورق

ومسافات بين كل نقطة وأخرى والزمن ويطالب بمجموعة من الخطأين يتم توضيح هذا المثال  
مع فلان مثال ومن ثم طرح أسئلة السؤال:

Ex:

|      |   |   |   |      |   |    |   |      |
|------|---|---|---|------|---|----|---|------|
| 0.5x | * | x | * | 1.5x | * | 2x | * | 2.5x |
|------|---|---|---|------|---|----|---|------|

Consider the time between two consecutive points is 0.1 sec and  $x = 1 \text{ cm}$

\* دائماً لها شئوف هذا النوع من الأسئلة ↑ بنوع 3 جداول :-

| t (sec) | X (cm)                    |
|---------|---------------------------|
| 0       | 0                         |
| 0.1     | 0.5                       |
| 0.2     | (0.5 + 1)                 |
| 0.3     | (0.5 + 1 + 1.5)           |
| 0.4     | (0.5 + 1 + 1.5 + 2)       |
| 0.5     | (0.5 + 1 + 1.5 + 2 + 2.5) |

\* دائماً تبدأ من 0  
وتنزل حسب الزمن

| time interval | V ( $\frac{\Delta x}{\Delta t}$ ) |
|---------------|-----------------------------------|
| 0 → 0.1       | 5                                 |
| 0.1 → 0.2     | 10                                |
| 0.2 → 0.3     | 15                                |
| 0.3 → 0.4     | 20                                |
| 0.4 → 0.5     | 25                                |

بنظرة  
كل القاطعة

| t mid | V mid | a = $\frac{\Delta V}{\Delta t}$ |
|-------|-------|---------------------------------|
| 0.05  | 5     | 50                              |
| 0.15  | 10    | 50                              |
| 0.25  | 15    | 50                              |
| 0.35  | 20    | 50                              |
| 0.45  | 25    | 50                              |

نقل V  
في المبدل  
أثنين  
كما هي

و هكذا  
أشهر  
أبدأ من 0.05  
ثم زيادة 0.1

أيضاً في  
القانون  
 $a = \frac{\Delta V}{\Delta t}$   
فلا فائدة :  
ليس في الفروقات  
آن يكون  
a ثابت  
50 سرعة

أما هنا  
المسافة x أيضاً تبدأ من 0  
ومن ثم نضع المسافة الأولى ومن  
كل مرة نزيد المسافة التي قبلها



\* الاستنتاج من هذبا الفكرة :

\* Find the displacement of the motion

\* من العبدل الاول :

دائما نأخذ المسافة النهائية وهي ٥

$$(0.5 + 1 + 1.5 + 2 + 2.5) = 7.5 \text{ cm}$$

\* Find the smallest or largest average velocity :



\* Find time interval have smallest or largest average Velocity

$$(0 \rightarrow 0.1)$$

$$(0.4 \rightarrow 0.5)$$

\* Find the instantan velocity at  $t = 0.05$  ?? 5

\* Find the acceleration of the motion ??  $50 \text{ m/s}^2$

\* اذا كان التسارع متغير بحد الزمان او بغيره

largest or smallest

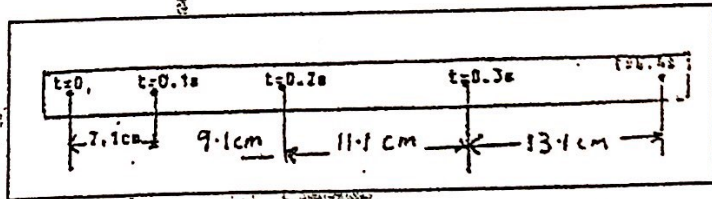
[X] The ticker tape shown below was recorded for a certain uniformly accelerated motion. the average acceleration in  $(\text{cm/s}^2)$  is

b) 200

a) 293

d) 132

c) 260



solution:

| t   | x    |
|-----|------|
| 0   | 0    |
| 0.1 | 7.1  |
| 0.2 | 16.2 |
| 0.3 | 27.3 |
| 0.4 | 40.4 |

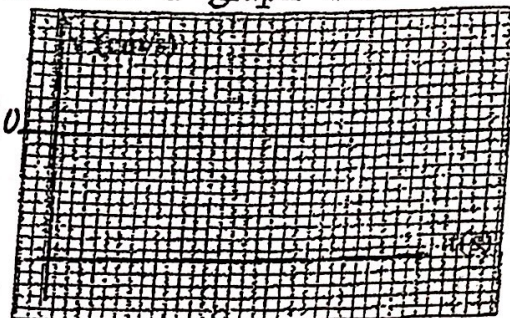
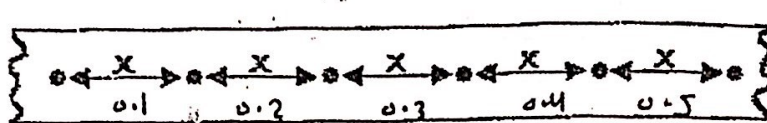
| t <sub>int</sub> | V    |
|------------------|------|
| 0 → 0.1          | 7.1  |
| 0.1 → 0.2        | 9.1  |
| 0.2 → 0.3        | 11.1 |
| 0.3 → 0.4        | 13.1 |

$$\frac{\Delta x}{\Delta t}$$

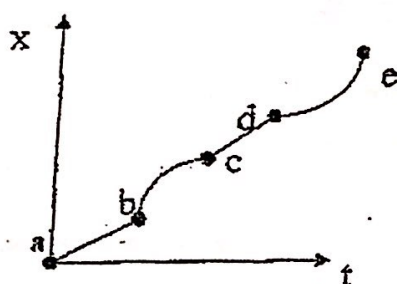
| t <sub>mid</sub> | V <sub>mid</sub> | a   |
|------------------|------------------|-----|
| 0.05             | 7.1              | 200 |
| 0.15             | 9.1              | 200 |
| 0.25             | 11.1             | 200 |
| 0.35             | 13.1             | 200 |

لهذا  $a$  ثابت لان  $\Delta x$  و  $\Delta t$  ثابتان

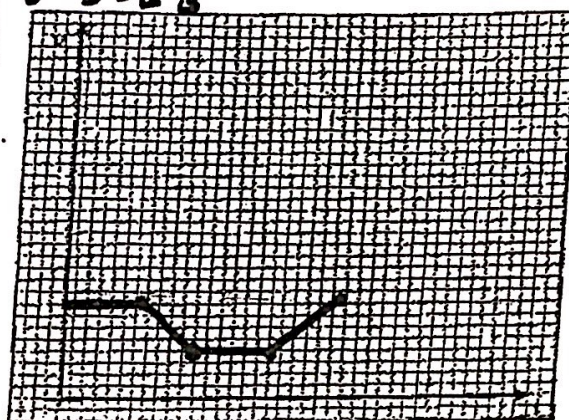
9-For the ticker tape shown below, if the time between two consecutive points is 0.1sec and  $x = 1\text{cm}$ . Plot a graph that represents the velocity versus time?



Ex 10-In the experiment of rectilinear motion, use the graph below to plot graph represent speed versus time and show all points on graph.



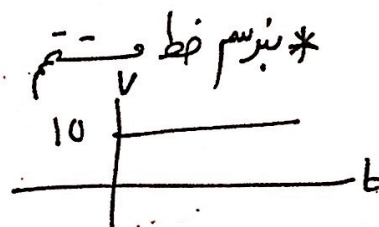
حلول | رسم منحنى السرعة



Ex 9:

| t   | x |
|-----|---|
| 0   | 0 |
| 0.1 | 1 |
| 0.2 | 2 |
| 0.3 | 3 |
| 0.4 | 4 |
| 0.5 | 5 |

| t       | V  |
|---------|----|
| 0-0.1   | 10 |
| 0.1-0.2 | 10 |
| 0.2-0.3 | 10 |
| 0.3-0.4 | 10 |
| 0.4-0.5 | 10 |



6- The position in (m) of a particle as a function of time in (sec) is given by:  $x=2t^3+5t-6$ . The average acceleration in ( $\text{m/sec}^2$ ) between 3 and 5 sec, is:

- a) 24      ~~b) 18~~      c) 35      d) None of the above

7- Using the previous question, the acceleration in ( $\text{m/sec}^2$ ) at  $t=1\text{sec}$  is:

- a) 24      ~~b) 12~~      c) 11      d) None of the above

$$x = 2t^3 + 5t - 6$$

$$v = 6t^2 + 5$$

$$a = 12$$

④ Avg a =  $\frac{v(5) - v(3)}{5 - 3} = \frac{155 - 59}{2} = 48 \text{ m/sec}^2$

⑤ a(1) =  $12 \times 1 = 12 \text{ m/sec}^2$

④ 48



### 3- Kinematics of Rectilinear Motion:

Note: Time interval between two successive points equal 0.1 s

- ⊗ In the first two intervals, the speed is almost equal ☐
- ⊗ The acceleration at 0.2 s is negative [ ]
- ⊗ The largest acceleration occurs at 0.4 s [ ]
- ⊗ The speed is slowest at 0.25 s. [ ]

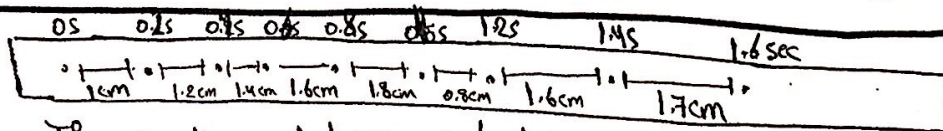
السؤال  
غير كامل يجب وجود  
رسم، وقتياً كانوا  
يزيدوا ورق عليه الرسا

EX<sub>1</sub> In kinematic experiment, the tape represents the distance only (X)

the tape represents : المسافة  
distance & time

EX<sub>2</sub> In kinematic experiment, the distance between taps represents velocity and acceleration (✓)

EX<sub>3</sub>  
استكمال المسألة  
التي كانت  
2016  
(م)



If the time between each two consecutive points is 0.2sec:

- ① Find the distance traveled in the time interval (0.6s & 1.0sec).
- (a) 3.0 cm (b) 2.6 cm (c) 3.4 cm (d) 4.2 cm

- ② Find the instantaneous velocity at  $t = 0.7$  sec:
- (a) 9 cm/s (b) 7 cm/s (c) 8 cm/s (d) 6 cm/s

- ③ Find the Avg Acceleration of the object on the time interval (1.1 to 1.5) sec:
- (a) -0.25 cm/s<sup>2</sup> (b) 26 cm/s<sup>2</sup> (c) 60 cm/s<sup>2</sup> (d) 2.5 cm/s<sup>2</sup>

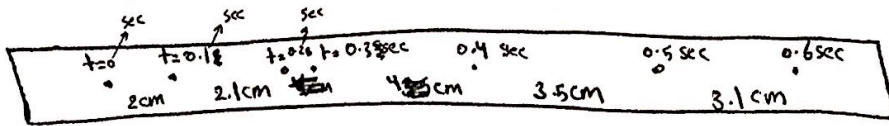
(11)



Ex 21

the following tape was obtained, answer the questions using this tape

فایل  
المعيار الأول  
ف  
الثنائي  
لسته  
2016



فایل  
الثنائي  
لسته  
2016

① If the Avg acceleration in the interval (0.15 - 0.25)s is  $-1.60 \text{ m/s}^2$  then the distance (in cm) moving the interval (0.2 - 0.3)s is:

- الجابات (a) 0.5 (b) 0.6 (c) 0.7 (d) 0.8 (e) 0.9

② The velocity was highest at time:

- الجابات (a) 0.15 sec (b) 0.55 sec (c) 0.4 sec (d) 0.35 sec (e) 0.25 sec

③ The smallest magnitude of acceleration occurs at time:

- الجابات (a) 0.1 sec (b) 0.2 sec (c) 0.5 sec (d) 0.4 sec (e) 0.3 sec



لحل الأمثلة نقوم بملء الجدول

①  $a = \frac{\Delta v}{\Delta t}$   
 $-1.60 = \frac{v(0.25) - v(0.15)}{0.25 - 0.15}$   
 $-160 \times \frac{v(0.25) - 21}{0.1}$

$v(0.25) = 5 \text{ cm/s}$

$v(0.25) = \frac{\Delta x}{\Delta t}$

$v(0.25) = \frac{\Delta x}{0.3 - 0.2}$

$5 = \frac{\Delta x}{0.1}$

الجابات  $\Delta x = 0.5 \text{ cm}$

| t(sec) | X(cm) |
|--------|-------|
| 0      | 0     |
| 0.1    | 2     |
| 0.2    | 4.1   |
| 0.3    | 4.6   |
| 0.4    | 8.6   |
| 0.5    | 12.1  |
| 0.6    | 15.2  |

ملاحظة: تم ملء الجدول

| Time interval | $\Delta v = \frac{\Delta x}{\Delta t}$ |
|---------------|--|
| 0 → 0.1       | 20                                     |
| 0.1 → 0.2     | 21                                     |
| 0.2 → 0.3     | 50                                     |
| 0.3 → 0.4     | 40                                     |
| 0.4 → 0.5     | 35                                     |
| 0.5 → 0.6     | 31                                     |

تم ملء الجدول  
بأكمله

| t mid (s) | v mid (cm/s) | Avg a |
|-----------|--------------|-------|
| 0.05      | 20           | 10    |
| 0.15      | 21           | 290   |
| 0.25      | 50           | -100  |
| 0.35      | 40           | -500  |
| 0.45      | 35           | -40   |
| 0.55      | 31           |       |

② نقوم بملء الجدول: ملاحظة: قبل السؤال الأول فقط استمعنا أن نبقى فقط أول 2 صفوف في الجدول الأول

والآن سوف انزل الجدول كامل بعد أن نعرفنا جميع الجوابات

و نرى في الجدول الثالث ان اعلى سرعة كانت عند 0.25

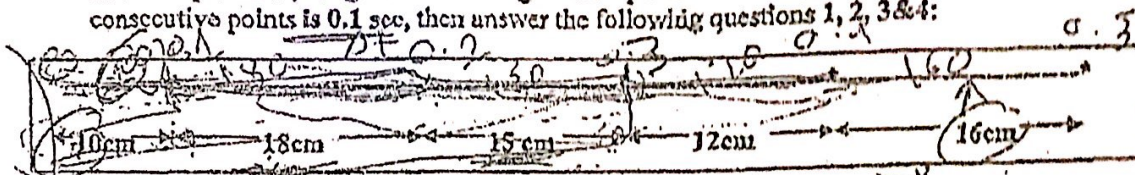
من الجدول الثالث اول سرعة كان عند 0.35

1/2

EX<sub>5</sub>

❖ Kinematics of rectilinear motion experiment:

In this experiment, we get the following ticker tape. If the time between two consecutive points is 0.1 sec, then answer the following questions 1, 2, 3 & 4:



1) The smallest average velocity (in cm/sec) is:

- a) 100  
b) 120  
c) 180  
d) 80

2) The smallest average acceleration (in cm/s<sup>2</sup>):

- a) 400  
b) 800  
c) 800  
d) 300

3) The velocity (in cm/sec) at t=0.45 sec is:

- a) 100  
b) 120  
c) 150  
d) 160

4) The area under the curve of (V and t) from (0.1-0.3) sec will be:

- a) 18 cm  
b) 27 cm  
c) 28 cm  
d) 33 cm

| t (s) | X (cm) |
|-------|--------|
| 0     | 0      |
| 0.1   | 10     |
| 0.2   | 28     |
| 0.3   | 43     |
| 0.4   | 55     |
| 0.5   | 71     |

| Time interval | Avg V (cm/sec) |
|---------------|----------------|
| 0 → 0.1       | 100            |
| 0.1 → 0.2     | 180            |
| 0.2 → 0.3     | 150            |
| 0.3 → 0.4     | 120            |
| 0.4 → 0.5     | 160            |

| t mid | V mid | Avg a |
|-------|-------|-------|
| 0.05  | 100   | 800   |
| 0.15  | 180   | -300  |
| 0.25  | 150   | -300  |
| 0.35  | 120   | 400   |
| 0.45  | 160   |       |

$\Delta x = x_2 - x_1$   
 $= 43 - 10$   
 $= 33$

11

9 80

12

13

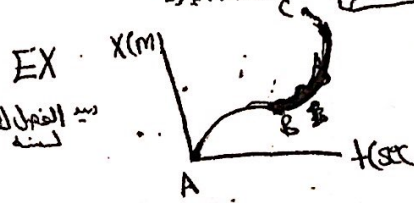
14

Fig. 1

5. In kinematics of rectilinear motion experiment, which of the following statements is correct?

- a) The dots on the tapes represent position and time.  
 b) The instantaneous velocity can be found directly from the tape.  
 c) The maximum and minimum average velocity can be found directly from the tape.  
 d) Both (a) and (c) are correct.

Q14) Kinematics of rectilinear motion: The dots on the tape represent  
 a) position b) position and time c) acceleration d) time



In the figure → decreasing from A to B, increasing from B to C

13



EX/6 ① The distance (in m) traveled by the object in the time interval (0.45 - 0.35) sec is:

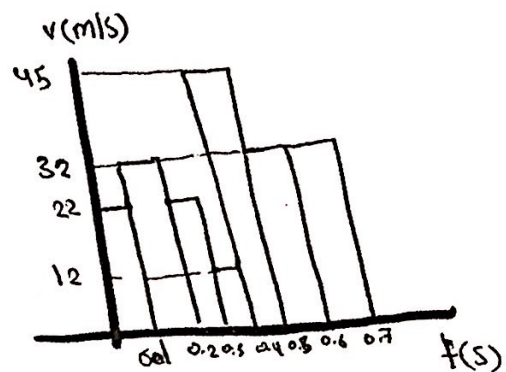
مسافة  
الاجابة  
20/6

المسافة = المسافة الاولى + المسافة الثانية  
 $\frac{1}{2}(0.1 \times 32) + \frac{1}{2}(0.1 \times 45) = 3.85 \text{ m}$  #

② the instantaneous velocity in (m/s) at  $t = 0.35 \text{ sec}$  is:

12 m/s

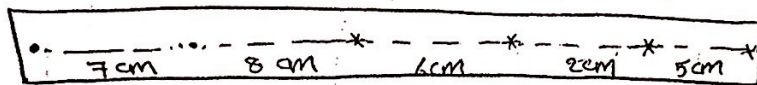
الاجابة: ← كالتالي في المنحنى



③ the Avg acceleration in ( $\text{m/s}^2$ ) of the object on the time interval (0.35 - 0.45) sec is:

Avg  $a = \frac{\Delta v}{\Delta t}$  : لكي  
 $= \frac{v(0.45) - v(0.35)}{0.45 - 0.35} = \frac{45 - 12}{0.1} = 330 \text{ m/s}^2$  #

Ex IF the time between two consecutive (2.520) points is 0.1 sec answer the Questions.



① The velocity in (cm/s) at 0.4 second is:

الاجابة

Ⓐ 80

Ⓑ 60

Ⓒ 70

Ⓓ 50

Ⓔ 20

الاجابة  
في التوقيت  
الاول

② The smallest Avg acceleration in ( $\text{cm/s}^2$ ) is:

الاجابة

Ⓐ 300

Ⓑ 400

Ⓒ 200

Ⓓ 100

③ The Largest Avg velocity in (cm/s) is:

الاجابة

Ⓐ 20

Ⓑ 50

Ⓒ 60

Ⓓ 20

EX From the graph below, answer the Questions:

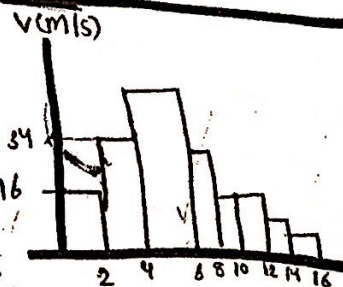
مسافة  
الاجابة

① the distance moved (in m) by the object in the interval (1/3) is:

#  $150 \text{ m} = 1 \times 34 + 16 \times 1$  : كالتالي

② the Avg acceleration in ( $\text{m/s}^2$ ) in the interval (1/3) is:

Avg  $a = \frac{v(3) - v(1)}{3 - 1} = \frac{34 - 16}{2} = 9$  #



(14)



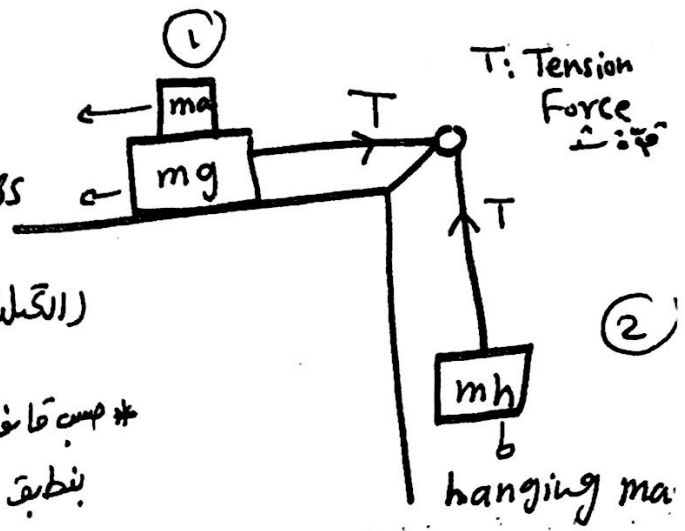
# Experiment 5

## Force And Motion

## Ex5: Force and motion:

$m_a$ : added mass

$m_g$ : glider mass



\* ملاحظة  $M_{cart} = m_a + m_g$  (الكتلتين معاً)

$$F = ma$$

\* حسب قانون نيوتن الثاني  
بنطبق على الجسمين

$$(1) T - 0 = m_{cart} a$$

$$(2) m_h g - T = m_h a \quad + \quad \text{نجمع المعادلتين}$$

$$\Rightarrow m_h g = m_{cart} a + m_h a$$

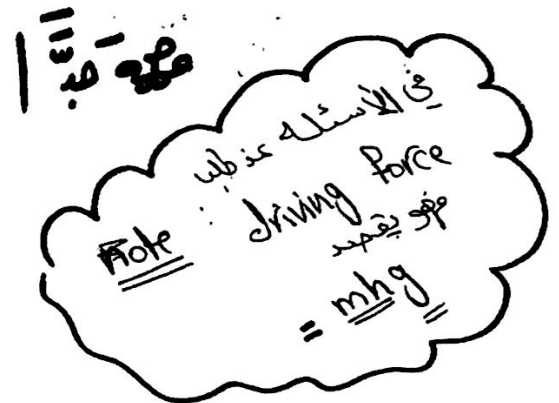
$$\Rightarrow m_h g = (m_{cart} + m_h) a$$

$m_h$ : hanging mass

$g$ : gravity

$a$ : acceleration

$$m_h g = (m_h + m_a + m_g) a$$



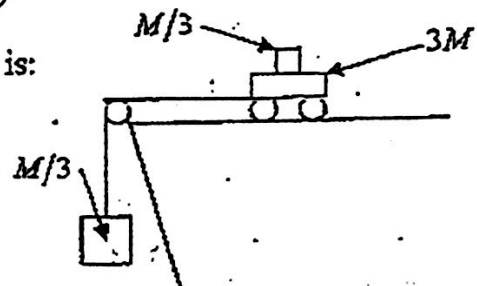
هذا القانون هو  
الوحيد في التجربة

Ex:

If you have the following setup for force and motion experiment, answer questions 12 and 13. (NOTE: the friction force is neglected)

12) The force acting on the system (driving force) is:

- (a)  $Mg/3$
- (b)  $11 Mg/3$
- (c)  $Mg/4$
- (d)  $9Mg/2$



13) The acceleration of the group is:

- (a)  $g/18$
- (b)  $g/4$
- (c)  $g/11$
- (d)  $3g/4$

Solution: 12) driving force =  $m_h g$   

$$= \frac{M}{3} g$$

②

13)  $m_h g = (m_a + m_h + m_g) a$   

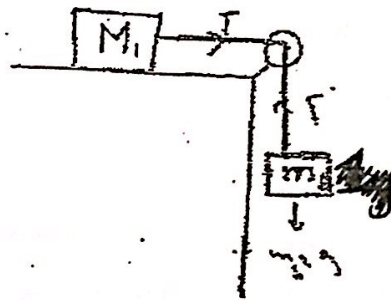
$$\frac{M}{3} g = (3M + \frac{M}{3} + \frac{M}{3}) a$$
  

$$\frac{M}{3} g = \frac{11}{3} M a$$
  

$$a = \frac{g}{11} \text{ m/s}^2$$

#### 4- FORCE AND MOTION:

a- According to the corresponding figure (2)  
 If  $M=2m$ , then the tension in the string (T)



consider  $g = 9.8 \text{ m/s}^2$

- ②
- (a) 6.5 m
  - (b) 3.5 m
  - (c) 3.3 m
  - (d) 9.8 m

b- In force and motion experiment we changed the inclination of the track to eliminate what force ~~friction~~

a-)  $T = Ma \dots (1)$

$mg - T = ma \dots (2)$

$\Rightarrow mg = Ma + ma$

$\Rightarrow mg = 2ma + ma$

$\Rightarrow \cancel{m}g = 3\cancel{m}a$

$\Rightarrow a = \frac{g}{3} \text{ m/s}^2$

نحوه حذف اصطکاک

$\Rightarrow T = Ma$

$\Rightarrow T = 2m a$

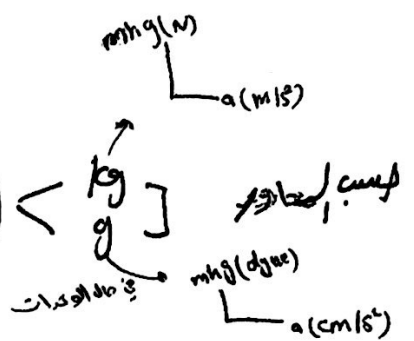
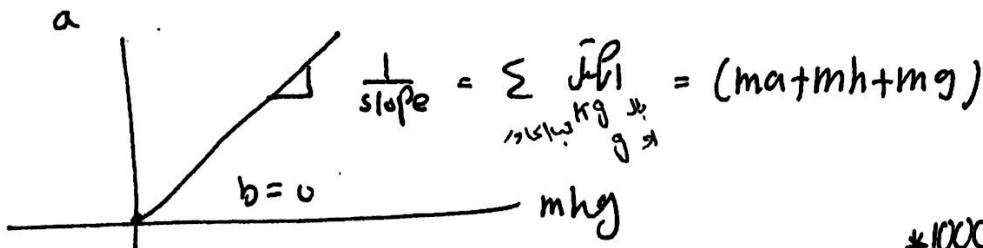
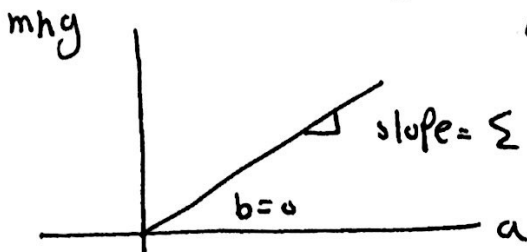
$$= 2 * 2 * \frac{9.8}{3} = 6.53 \text{ m/s}^2 \quad (6.5 \text{ m/s}^2) \text{ N}$$

الطريقه الاولى:

(مقابل قوتها)



$$m_h g = (m_a + m_h + m_g) a$$



عند القلي:  $a$

$$kg \xrightarrow{\times 1000} g$$

ملاحظة

$$1N \rightarrow 10^5 \text{ dyne} \quad \text{و } g \frac{cm}{s^2}$$

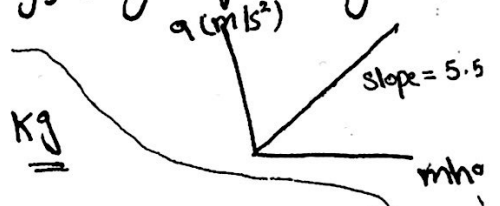
$$1kg \frac{m}{s^2}$$

مثال

**Ex:** The added and hanging mass are 70g, 60g respectively the glider mass is:

$$\text{Sol: } \frac{1}{\text{slope}} = m_h + m_g + m_a \quad * \text{slope} = 5.55 \text{ kg}$$

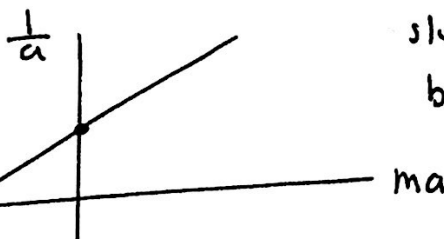
$$\Rightarrow \frac{1}{5.55} = 70 + 60 + m_g \Rightarrow 0.18 \times 1000 = 130 + m_g \Rightarrow m_g = 50g$$



الافتتاح

2

$$m_h g = (m_c + m_a + m_h) a$$



$$\text{slope} = \frac{m_h g}{m_c + m_a + m_h}$$

$$\frac{m_h g}{m_c + m_a + m_h} = a$$

$$\frac{1}{a} = \frac{m_c + m_a + m_h}{m_h g}$$

$$\frac{1}{a} = \frac{m_c + m_a}{m_h g} + \frac{m_h}{m_h g}$$

y-intercept slope

$$\text{slope} = m_h g$$

$$b = (m_h + m_g)$$



الافتتاح

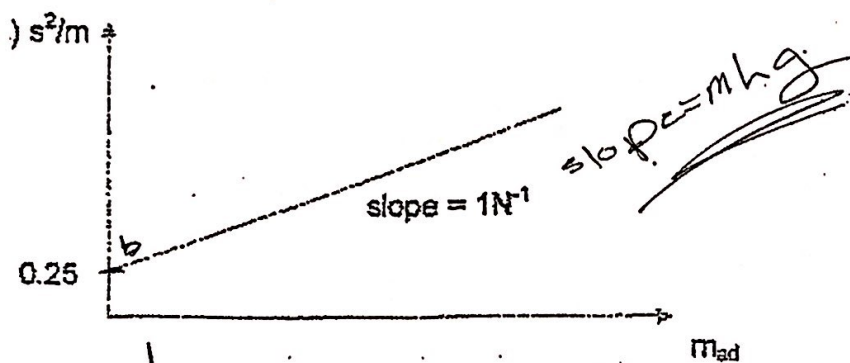
$$m_h g = (m_c + m_a + m_h) a$$

$$m_g = \frac{m_h g}{a} - m_h - m_g$$

y-intercept

In the "Force and Motion" experiment, if the following figure was obtained. The hanging mass & the mass of the cart (in kg) respectively are: (use  $g=10\text{ms}^{-2}$ ) (4 marks)

- a) 0.15, 0.1    b) 0.05, 0.06    c) 0.1, 0.06    d) 0.06, 0.05  
 e) 0.1, 0.15



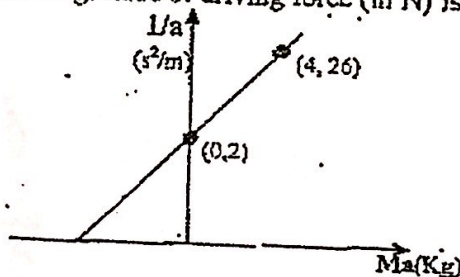
\* slope =  $mhg$

$1 = mh \times 10 \Rightarrow mh = 0.1 \text{ kg}$

$b = \frac{mh + mc}{mhg} \Rightarrow 0.25 = \frac{0.1 + mc}{0.1 \times 10}$   
 $mc = 0.15 \text{ kg}$

\*\* In the force and motion experiment :

- 8) For a constant driving force and changing added mass. A relation between  $(1/a)$  and  $(M_a)$  plotted in the graph. The magnitude of driving force (in N) is:  
 a) 8.0    b) 6.0  
 c) 0.16    d) 0.13



- 9) The plot of the acceleration (a) of a cart of mass  $M_c$  versus the hanging mass m is:  
 a) linear    b) non-linear    c) linear if  $M \gg m$  for all values.

Solu: driving force =  $mhg$

slope =  $mhg$

slope =  $\frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{26 - 2}{4 - 0} = 6$

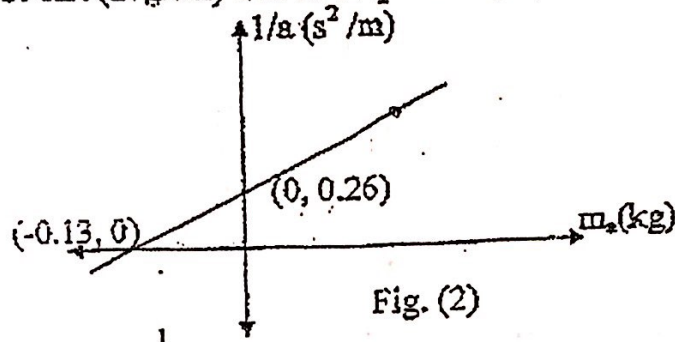
driving force =  $mhg$

slope =  $mhg \Rightarrow \frac{1}{6} = 0.166 \text{ N}$

(14)

5) The relation between  $1/a$  (in  $s^2/m$ ) and added mass  $m_a$  (in kg) is shown in figure (2) for a system consist of a cart that carry a mass and connected to a hanger with constant mass ( $m_h$ ). The magnitude of driving force (in N) and the mass of cart (in gram) will be respectively: (consider  $g = 10 \text{ m/s}^2$ )

- a) 0.5, 90
- b) 0.5, 80
- c) 0.1, 80
- d) 0.1, 90



solu:  $\text{slope} = \frac{1}{mhg}$

$$* \text{slope} = \frac{\Delta y}{\Delta x} = \frac{0.26 - 0}{0 - (-0.13)} = \frac{0.26}{0.13} = 1.923$$

$$\Rightarrow \frac{1}{1.923} \approx \frac{1}{1.9} = mh * 10 \Rightarrow mh = 0.0526 \text{ kg}$$

$\Rightarrow$

$\Rightarrow$

1) \* driving force =  $m_h g \Rightarrow 0.0526 * 10 = 0.526 \approx 0.5 \text{ N}$

2)  $\Rightarrow m_{\text{cart}} = \dots$  y-intercept =  $\frac{m_{\text{cart}} + m_h}{mhg}$

$$0.26 = \frac{m_{\text{cart}} + 0.0526}{0.0526 * 10}$$

$$m_{\text{cart}} = 0.084 \text{ kg} \approx 80 \text{ g}$$

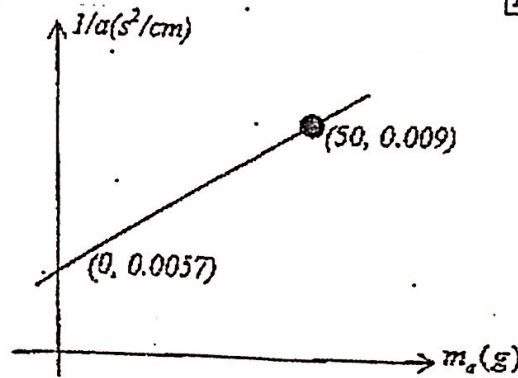


In the force and motion experiment; a student obtained the following graph, answer questions 10 and 11 depending on the graph.

2

10) If the hanging mass ( $m_h = 35g$ ), the value of  $g$  (gravitational acceleration) is:

- (a)  $980.0 \text{ cm/s}^2$
- (b)  $432.9 \text{ cm/s}^2$
- (c)  $606.1 \text{ cm/s}^2$
- (d)  $1000 \text{ cm/s}^2$



11) From the previous graph, the mass of the car ( $m_c$ ) is:

- (a)  $51.4 \text{ kg}$
- (c)  $51.4 \text{ g}$

- (b)  $61.4 \text{ kg}$
- (d)  $61.4 \text{ g}$

$$b = m + m_h$$

$$0.0057 = m + 35$$

$$\frac{1}{1.1 \times 10^{-5}}$$

solut: 10)  $m_h = 35g$

$$\text{slope} = \frac{g}{m_h}$$

$$\text{slope} = \frac{0.009 - 0.0057}{50 - 0} = 6.6 \times 10^{-5}$$

$$\Rightarrow \frac{1}{6.6 \times 10^{-5}} = 35 \times g \Rightarrow \frac{15151.515}{35} = 35 \times g$$

$$\Rightarrow g = 432.9 \text{ cm/s}^2$$

$$\frac{m_h g}{m_c + m + m_h} = g$$

$$\frac{1}{g} = \frac{m_c + m + m_h}{m_h g}$$

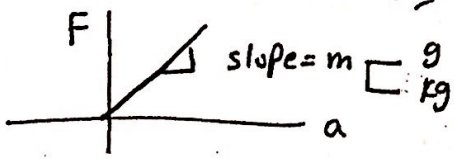
$$= \frac{m_c + m_h}{m_h g} + \frac{1}{m_h g} m$$

$$\text{y-intercept} = \frac{m_c + m_h}{m_h g}$$

$$0.0057 = \frac{m_c + 35}{35 \times 432.9}$$

$$m_c = 51.86 \text{ g} \approx 51.4 \text{ g}$$

$$F = ma \rightarrow$$



قانون نيوتن الثاني

المطابق مع رسومات

7- Find the mass of the cart from the graph of force vs acceleration for a constant mass system of mass = mass of the cart + 100g.

\* مقدار ثابت

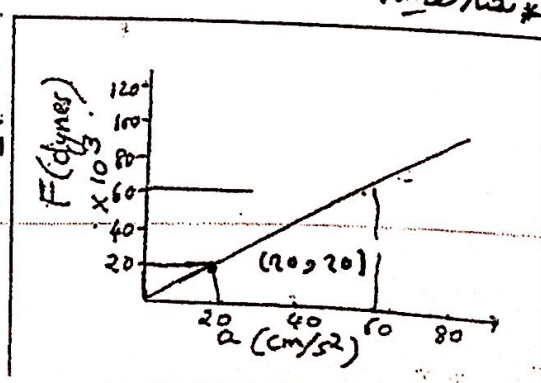
$$m = m_{\text{cart}} + 100$$

$$F = ma \Rightarrow \text{slope} = m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

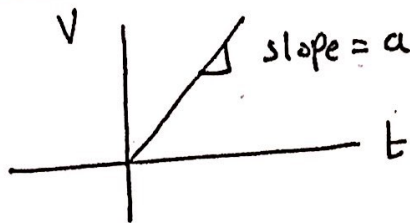
$$\frac{20 \times 10^3}{20 - 0} = 1000$$

$$\Rightarrow 1000 = m + 100$$

$$m_{\text{cart}} = 900 \text{ g}$$

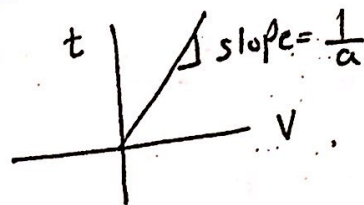


2]



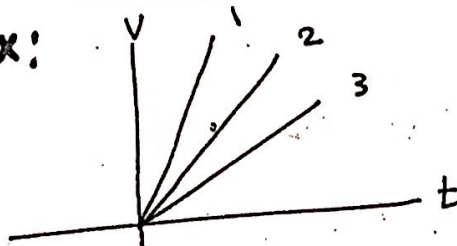
\* ملاحظة: دائماً اذكر ميل - اذكر ا - اقل

$F = m_b \uparrow a$   
علاقة بالسرعة



\* اذكر ميل - اقل - ا - اقل

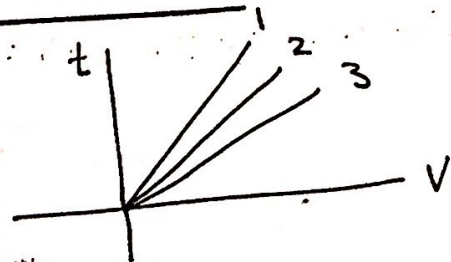
Ex:



$a_1 > a_2 > a_3$

$m_1 < m_2 < m_3$

Ex:



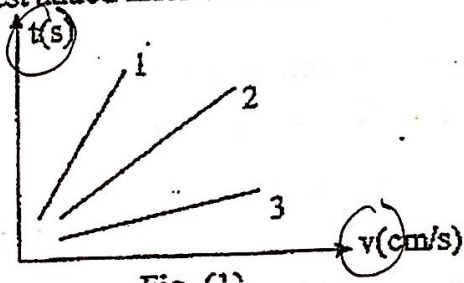
$a_1 < a_2 < a_3$

$m_1 > m_2 > m_3$

\* In Force and Motion Experiment: answer questions (4 and 5).

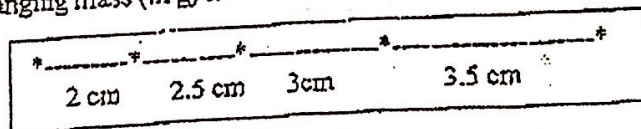
4) The relation between time (in sec) and velocity (in cm/s) is shown in figure (1) for a constant driving force ( $m_b g$ ) and different added masses on the cart. The line that represents largest added mass will be:

- a) line 1
- b) line 2
- c) line 3
- d) we can't judge from fig. (1)



تأمل تجربة Kinematic Force and motion

10) The ticker tape shown below is for a 800 g cart pulled by a hanging mass  $m_h$ . The time interval between any two consecutive points is 0.1s and  $g = 980 \text{ cm/s}^2$ . The hanging mass (in g) is:



a) 43

b) 853

c) 53

d) 753

$m_{\text{cart}} = 800 \text{ g}$

$g = 980 \text{ cm/s}^2$

$m_h ??$

g solution:

$m_h g = (m_{\text{cart}} + m_h) a$   
 $?? \cdot 980 = (800 + ??) a$

نستعمل المعادلة



| t   | x   |
|-----|-----|
| 0   | 0   |
| 0.1 | 2   |
| 0.2 | 4.5 |

| time    | V  |
|---------|----|
| 0-0.1   | 20 |
| 0.1-0.2 | 25 |

| V | t    | a        |
|---|------|----------|
|   | 0.05 | a = 50 ✓ |
|   | 0.15 |          |

$$m_h = 43g$$

نحوه ثبت اعداد و العواب النتائج :

2] If the  $m_h = 5g$ ,  $g = 1000 \text{ cm/s}^2$  and the cart acceleration is: Find the mass of the cart?

| Time (sec)      | 0.05 | 0.15 | 0.25 | 0.35 | 0.45 |
|-----------------|------|------|------|------|------|
| Velocity (cm/s) | 10   | 12   | 14   | 16   | 18   |

solu:  $m_h g = (m_{\text{cart}} + m_h) a \rightarrow a = \frac{\Delta v}{\Delta t} = \frac{12 - 10}{0.15 - 0.05} = 20 \text{ cm/s}^2$

$$5 * 1000 = (m_{\text{cart}} + 5) * 20$$

$$* m_{\text{cart}} = 245 \text{ g}$$

## 6- Force & Motion

A- in this experiment, two taps were obtained. The time interval between two successive points equals = 0.1 sec.

- If the total hanging mass is the same for both tapes, then the added mass to the cart for
- Tape B is larger than that for Tape A (✓)
- The acceleration is constant in Tape A and is negative (✓)
- If the cart is empty in both cases, then the total hanging weight for Tape B is larger than that for Tape A (✓)

Ex<sub>1</sub> In force and motion experiment (تجربة القوة والحركة) we increase the inclination of track to illuminate the normal force that acts on cart (X).  
بزيادة ميلان المسار لتوضيح القوة الطبيعية التي تؤثر على العربة (X).

Ex<sub>2</sub> In force and motion when we increase the load on the cart and driving force is constant, the acceleration of the cart will be constant (X).  
عند زيادة الحمل على العربة والقوة الدافعة ثابتة، فإن تسارع العربة سيكون ثابتاً (X).



8. In the case of the constant total mass of the force and motion experiment; fig.3 shows the relation between  $m_h(g)$  and  $a/g$ . The total mass of the system is (in kg):

- (a) 1  
b) 0.5  
c) 1000  
d) 500  
e) can not be determine

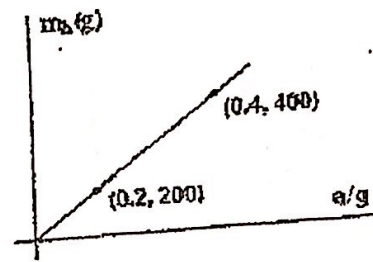


fig.3

2

$$m_h g = (m_a + m_h + m_g) a$$

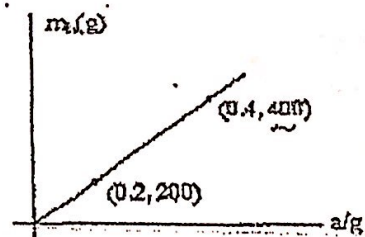
$$m_h = \underbrace{(m_a + m_h + m_g)}_{\text{total mass}} \frac{a}{g}$$

$$\text{total mass} = \text{slope} = \frac{\Delta y}{\Delta x} = \frac{200}{0.2} = 1000 \text{ g} = 1 \text{ kg}$$

ⓐ

9. In the case of the constant total mass of the force and motion experiment; fig.2 shows the relation between  $m_h$  (in g) and  $a/g$ . The total mass of the system is (in kg):

- (a) 10  
~~(b) 1~~  
(c) 0.5  
(d) 5  
e) can not be determine



نفس السؤال

- Q15) The slope of the graph plotted between  $mg$  and acceleration represent  
a) velocity    b) displacement    c) mass    d) weight

$$F = ma$$

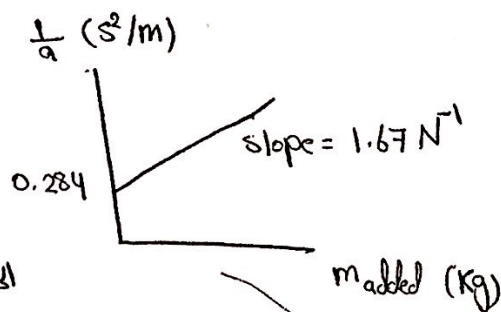
$$mg = \underbrace{m}_{\text{slope}} a$$



EX, 111  
ميد الفيزياء  
2014

force and motion exp, a student obtained  $mg$  + the gravitational acceleration  $g = 10 \text{ m/s}^2$ . the hanging mass and the mass of the glider (in g) respectively are:

- الخيارات  
 (a) 60, 110  
 (b) 50, 120  
 (c) 80, 100  
 (d) 70, 100



من  
 ①  $\frac{1}{\text{slope}} = m_h g$   
 $\frac{1}{1.67} = m_h \times 10$   
 $m_h = 0.0598 \text{ kg} \approx 0.06 \text{ kg} = 60 \text{ g}$

mg ②  $b = \frac{m_h + m_c}{m_h g} \Rightarrow 0.284 = \frac{0.06 + m_c}{0.6}$   
 $m_c = 0.104 \text{ kg} \approx 110 \text{ g}$

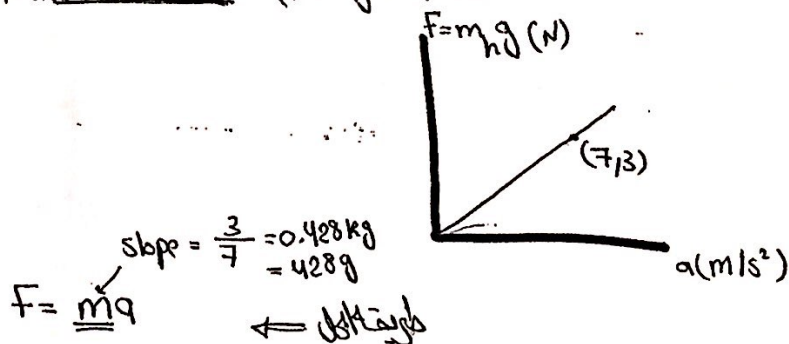
$m_c = m_g$   $m_{\text{added}} = m_c + m_h$

EX  
ميد الفيزياء  
2016

For the fixed total mass and changing driving force. the relation between  $m_h g$  (in Newton) and the acceleration is presented in the figure below. the total mass (in gram) is:

الخيارات

- (a) 428  
 (b) 333  
 (c) 267  
 (d) 227



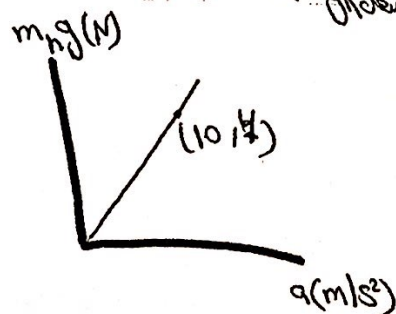
$\text{slope} = \frac{3}{7} = 0.428 \text{ kg} = 428 \text{ g}$

$F = m_h g$

الخيار

EX II  $m_h = 210 \text{ g}$  and the added mass =  $150 \text{ g}$  then the mass of the glider is: (in g)

- (a) 40 (b) 80 (c) 60 (d) 140 (e) 100



$F = m a$   
 $m_h g = m a$

$\text{slope} = \frac{4}{10} = 0.4 \text{ kg}$

mass of the system =  $0.4 \text{ kg}$

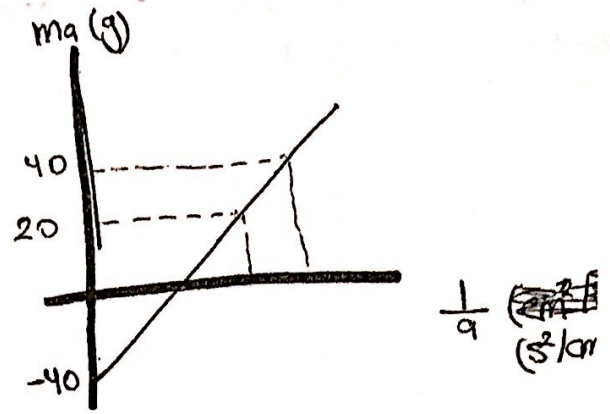
$150 + 210 + m_g = 400 \text{ g} \Rightarrow m_g = 40 \text{ g}$

الخيار

EX - From  $(m_a - \frac{1}{a})$  graph in figure the hanging mass and the glider mass respectively are:

قابل المصنوع  
الأداة + الترخيص  
سنة 2016

قابل المصنوع  
الترخيص  
سنة 2016



- according to  $(m_a - \frac{1}{a})$  graph  
If the Added mass is 250g  
then the acceleration in  $(m/s^2)$  is:

ملاحظة: ← الأرقام على محور X غير واضحة من النموذج  
ولكن سأكتب لطيفة الحد (السؤال رقم ٢١)

اولاً نضع

$$\begin{cases} \textcircled{1} m_h \Rightarrow \text{slope} = \bar{m}_h g \\ \textcircled{2} m_g \Rightarrow b = -(\bar{m}_h + \bar{m}_g) \end{cases}$$

ثم اشتقاقهم في صلب  
مفصلة في التلخيص

نحولها في المعادلة

$$(\bar{m}_h + \bar{m}_g + \bar{m}_a) a = \bar{m}_h g$$



EX In the force and motion exp, which of the following statements is correct:

الفيضان

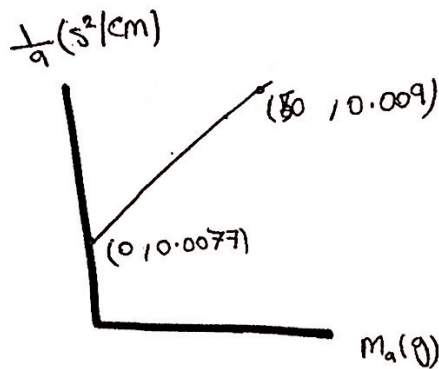
- ① The acceleration is inversely proportional with the hanging mass at constant driving force
- ② The acceleration is directly proportional with the glider mass at constant driving force
- ③ The acceleration is inversely proportional with the driving force at constant total mass
- ④ The acceleration is directly proportional with the driving force at constant total mass.

ف = م ا  
 $F = m a$   
 constant

EX A student obtained the following graph, Find the mass of the glider (M) in g:

الفيضان

- (a) 70.90      (b) 123.47  
 (c) 256.90      (d) 42.79



$$\textcircled{1} b = \frac{m_h + m_c}{m_h g} \Rightarrow 0.0077 = \frac{3846.1 + m_c}{3846.1}$$

$$m_c = 257.6g \approx 256.90g$$

$$\textcircled{2} m_h \Rightarrow \frac{1}{\text{slope}} = m_h g$$

$$\frac{50}{0.009 - 0.0077} = m_h \times 1000 \Rightarrow m_h = 3846.1g$$

الفيضان  
 في السائل عند ارتفاعه  
 يسقط من ارتفاعه  
 ويخرج من الأنبوب  
 في السائل

EX When the mass of the glider increases, then glider goes with acceleration:

(a) more quickly  
 (b) more slowly  
 (c) Independently  
 (d) All of the above  
 (e) at the same rate



Experiment (18)

Simple

Harmonic

motion

engine\_team

# Ex 8: Simple harmonic motion:

$0 \leq \theta \leq 90^\circ$  النسبة:  $\sin \theta$  يتناقص من 1 إلى 0

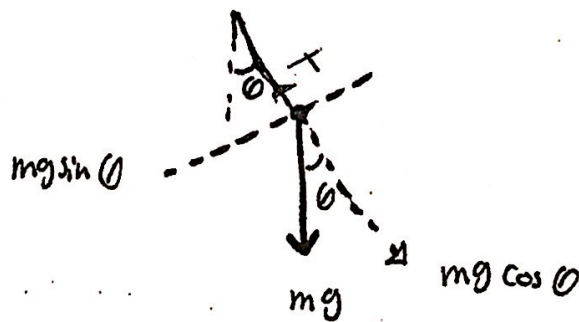
$\Rightarrow \Sigma F = ma$  حسب قانون نيوتن الثاني  
y-axis

$T - mg \cos \theta = ma_c \Rightarrow a_c$ : التسارع المركزي

x-axis

$mg \sin \theta = ma_t \Rightarrow a_t$ : tangent تسارع مماسي

$\Rightarrow$  The only force acting on simple pendulum:  $-mg \sin \theta$  restoring force



\*  $\boxed{1} T_{period} = 2\pi \sqrt{\frac{L}{g}}$

في هذه التجربة يوجد قانونين مهمين:

$T_{period}$ : الزمن الدوري للزخم لإتمام دورة كاملة بوحدة (sec)  
 $g$ : الجاذبية الأرضية ولازم قانونها معنا

أما أن بعض في الهواء / نعلم أنه لا يجادلها.

\* Remark:  $L$  و  $g$

$L \rightarrow cm \rightarrow g: cm/s^2$

$L \rightarrow m \rightarrow g: m/s^2$

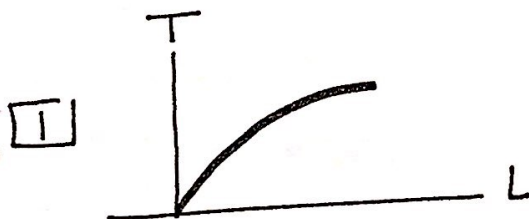
$\boxed{2} N = \frac{t}{T_{period}}$

$N$ : number of oscillations  
 $t$ : الزمن الكلي بوحدة (sec)

عدد الذبذبات

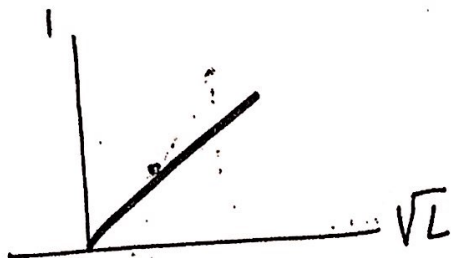
\* الرسومات المطلوبة لهذه التجربة:  $T_{period} = 2\pi \sqrt{\frac{L}{g}}$   
نسبته بالقانون:

العلاقة لوجية \* غير خطية.  
(علاقة جذرية)





2



$$b = \text{zero}$$

$$\text{slope} = \frac{2\pi}{\sqrt{g}}$$

طريقة إيجاد ال slope

$$① T = 2\pi\sqrt{\frac{L}{g}}$$

$$② y = mx + b$$

$$③ y \rightarrow T$$

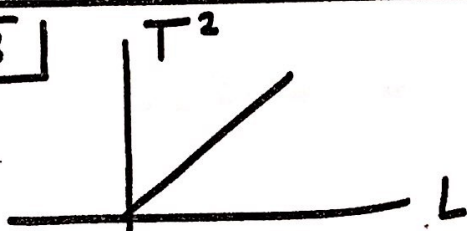
$$\sqrt{L} \rightarrow x$$

$$m \rightarrow \frac{2\pi}{\sqrt{g}}$$

$$b = \text{zero}$$

(بالمقارنة مع معادلات الخط المستقيم)

3

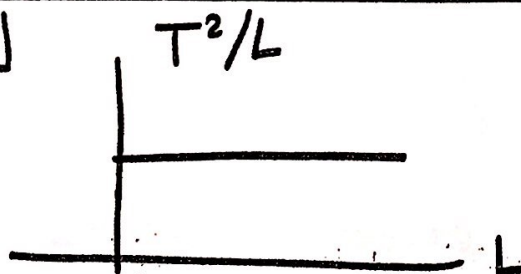


$$b = 0$$

$$\text{slope} = \frac{4\pi^2}{g}$$

$$T = 2\pi\sqrt{\frac{L}{g}} \Rightarrow \text{مربع الطرفين} \Rightarrow T^2 = \frac{4\pi^2}{g} L$$

4



$$\text{slope} = 0$$

$$b = \frac{4\pi^2}{g}$$

$$\text{توضيح: } T = 2\pi\sqrt{\frac{L}{g}} \Rightarrow \text{مربع الطرفين} \Rightarrow T^2 = \frac{4\pi^2}{g} L \Rightarrow \frac{T^2}{L} = \frac{4\pi^2}{g} + 0L$$

إذاً يأتي سؤال على أحد التسميات الخمسة  
 الشكل المستقيم للوسيلة  
 أو ملاحظة  $g$  مستقلة أو

### Simple Harmonic motion (Simple pendulum):

6] A simple pendulum 12 m in length oscillates in a location where  $g = 10 \text{ m/s}^2$ . The number of oscillations in 10 minutes:

- a) 2.5  
b) 87

- b) 123  
d) 149

$$2 \times 3.14 \times \sqrt{\frac{12}{10}} \approx 6.8$$

7] If the ratio between two pendulum lengths is  $L_2/L_1 = 16$ , then the ratio between two periods  $T_1/T_2$  is:

- a) 1/9  
c) 1/5

- b) 9  
d) 1/4

$$\frac{T_1}{T_2} = \sqrt{\frac{L_1}{L_2}} = \sqrt{\frac{1}{16}} = \frac{1}{4}$$

6]  $L = 12 \text{ m}$

$g = 10 \text{ m/s}^2$

$t = 10 \text{ min}$

$N = ?$

$$\Rightarrow N = \frac{t}{T_{\text{period}}} = \frac{10 \times 60}{6.87} = 87.3 \approx 87$$

$$T_{\text{period}} = 2\pi \sqrt{\frac{L}{g}} = 2\pi \sqrt{\frac{12}{10}} = 6.87 \text{ se} \quad \text{فرع c}$$

7]  $\frac{L_2}{L_1} = 16$  و  $\frac{T_1}{T_2} = ?$

$$\text{Sol: } \frac{T_1}{T_2} = \frac{2\pi \sqrt{\frac{L_1}{g}}}{2\pi \sqrt{\frac{L_2}{g}}} \Rightarrow \frac{T_1}{T_2} = \sqrt{\frac{L_1}{L_2}} = \sqrt{\frac{1}{16}} = \frac{1}{4}$$

$$\Rightarrow \frac{T_1}{T_2} = \sqrt{\frac{1}{16}} = \frac{1}{4} \quad \text{فرع d}$$

1) Q2) SHM: In simple pendulum experiment, the linear graph is plotted between

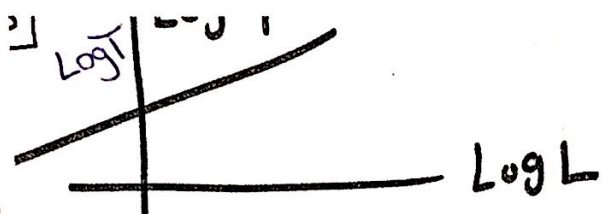
- a)  $T$  and  $L$  b)  $T^2$  and  $L$  c)  $T$  and  $L^2$  d)  $T^2$  and  $L^2$

2) SHM: When the length of the simple pendulum increases

- a) the mass of the ball will increase b) the speed of the ball will increase  
c) the period will decrease d) the period will increase

1) b)  $T^2$  and  $L$

2) c) The Period Will ~~decrease~~ <sup>Increase</sup>



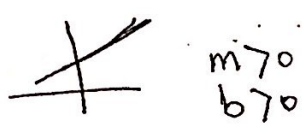
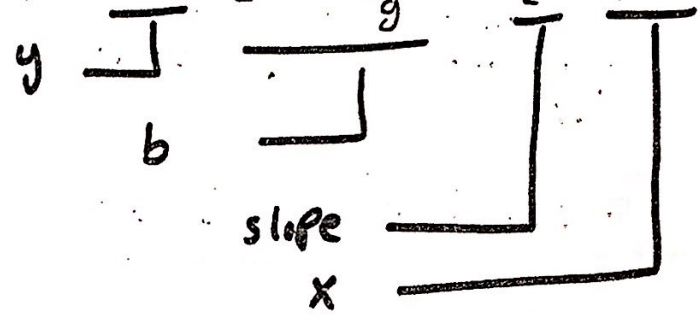
slope = 0.5

$b = \frac{1}{2} \log \frac{4\pi^2}{g}$

الطريقة ولكن صفتها اسهل :

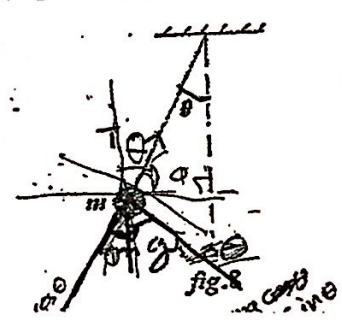
$T^2 = 4\pi^2 \frac{L}{g} \Rightarrow \log T^2 = \log \frac{4\pi^2 L}{g} \Rightarrow \log T^2 = \log \frac{4\pi^2}{g} + \log L$

$\Rightarrow 2 \log T = \log \frac{4\pi^2}{g} + \log L \Rightarrow \log T = \frac{1}{2} \log \frac{4\pi^2}{g} + \frac{1}{2} \log L$



13. The only force acting on the simple pendulum in our experiment is:

- a)  $-mg \sin \theta$
- b)  $-mg \cos \theta$
- c)  $T$
- d) Both (a) and (c) are correct



الإجابة

14. Which of the following graphs represents correctly the relation between the periodic time  $T$  (in sec) and the length of the pendulum  $L$  (in cm)?

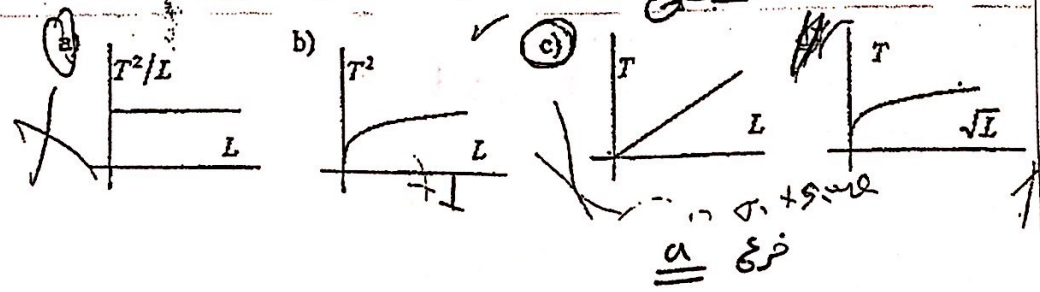
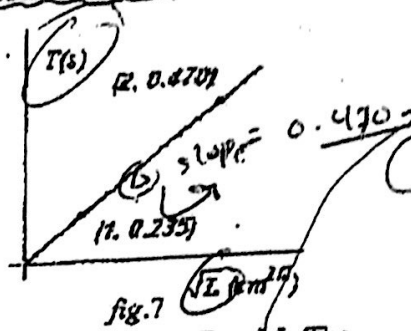




Fig. 7 is obtained by a student from the simple pendulum experiment, from this graph the gravitational acceleration (in  $\text{cm/s}^2$ ) is:

- 1)   
 a) 714.1   
 b) 1606.8   
 c) 40.1   
 d) 26.7

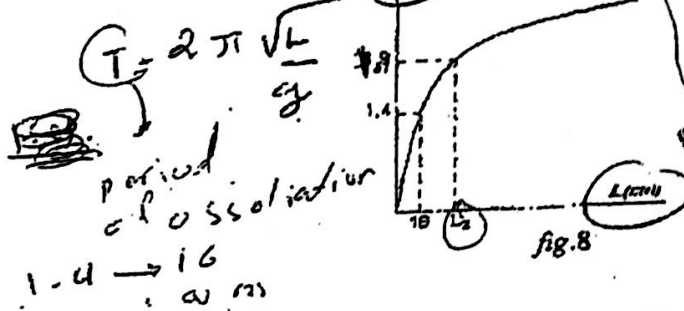
$$g = \frac{4\pi^2}{\text{slope}}$$



الجواب د

13. In the simple pendulum experiment, fig. 8 shows the relation between  $T$  and  $L$ . The value of  $L_2$  is (in cm):

- 2)   
 a) 14.7   
 b) 21.7   
 c) 10.8   
 d) 29.5



\* 1) slope =  $\frac{\Delta y}{\Delta x} = \frac{0.470 - 0.235}{2 - 1} = 0.235$

$$\Rightarrow \text{slope} = \frac{2\pi}{\sqrt{g}} \Rightarrow 0.235 = \frac{2 * 3.14}{\sqrt{g}} \Rightarrow \frac{2 * 3.14}{0.235} = \sqrt{g}$$

$$\Rightarrow g = 714.14 \text{ cm/s}^2$$

2)  $T_2 = 2\pi \sqrt{\frac{L_2}{g}} \Rightarrow 1.9 = 2 * 3.14 \sqrt{\frac{L_2}{g}}$

$$\Rightarrow 1.9 = 2 * 3.14 \sqrt{\frac{L_2}{321.957}} \Rightarrow L_2 = 29.47 \approx 29.5$$

فرقة د الجواب

$$\Rightarrow T_1 = 2\pi \sqrt{\frac{L_1}{g}} \Rightarrow 1.4 = 2 * 3.14 \sqrt{\frac{16}{g}} \Rightarrow g = 321.957 \text{ cm/s}^2$$

21) Error analysis: Suppose that we measure  $g$ , the acceleration of gravity, using a simple pendulum. If  $L$  is the length of the pendulum and  $T$  is the period then  $T = 2\pi \sqrt{\frac{L}{g}}$ . Suppose we measure the period  $T$  for one value of the length  $L$  and get the result  $L = 92.95 \pm 0.1$  cm and  $T = 1.936 \pm 0.004$  seconds. The fractional uncertainty in our answer for  $g$  is

- a) 0.4%   
 b) 0.2%   
 c) 0.1%   
 d) 0.3%

$$\Delta g = g \sqrt{\left(\frac{\Delta L}{L}\right)^2 + \left(\frac{2\Delta T}{T}\right)^2}$$

$$= 0.2\%$$

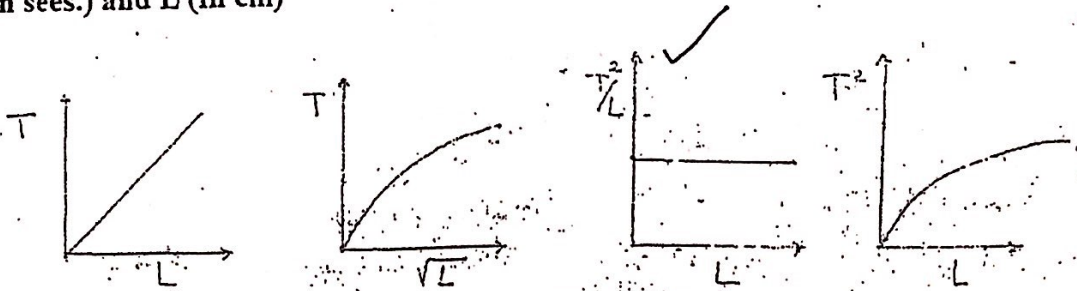
$$T^2 = 4\pi^2 \frac{L}{g}$$

$$g = 4\pi^2 \frac{L}{T^2}$$

مسألة رابعة  
ب. الجواب

## ➤ SIMPLE PENDULUM:

1- Which of the following graphs represents correctly the relationship between  $T$  (in secs.) and  $L$  (in cm)



2- If we plot  $\log T$  vs  $\log L$  where  $T$  is the period and  $L$  is the length of the pendulum, the slope will be:

$$\frac{4\pi^2}{g} \text{ d) } \log$$

$$\frac{2\pi}{\sqrt{g}} \text{ c) } \log$$

$$\frac{1}{2} \text{ b) }$$

$$-\frac{1}{2} \text{ a) }$$

13- The pendulum is set to oscillate through a small angle (about 5 degrees). Why?

لأنه عند زاوية صغيرة  $\sin \theta \approx \theta$

14- How dose one increase the accuracy of finding  $T$  (time period) in this experiment?

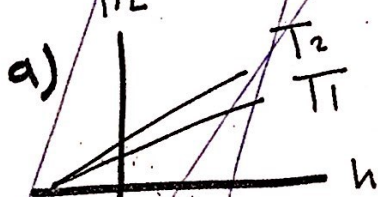
by increasing the number of oscillations

Which graph is correct

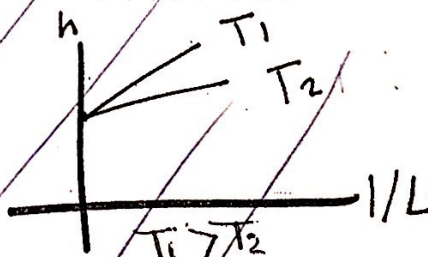
\* السؤال في الامتحان: (سؤال)

مثلاً الجواب  
هو ب) لأنه

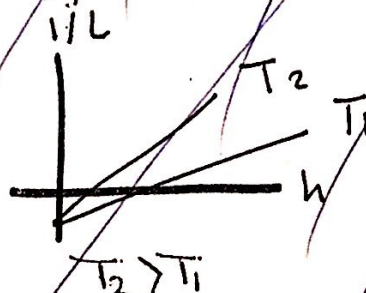
Ex:  $T_1 > T_2$



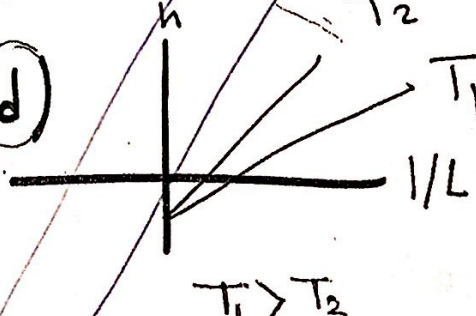
c)



b)



d)



e)

لأنه في المثل الرابع كلما نزلنا الأسفل يزيد الميل

### 11- Simple Pendulum:

In this experiment, increasing the number of oscillations of the which the time interval is measured.

- a) Causes the measured value of  $g$  to increase.
- b) Causes the measured value of  $g$  to decrease.
- c) Has no effect on the measured value of  $g$ .

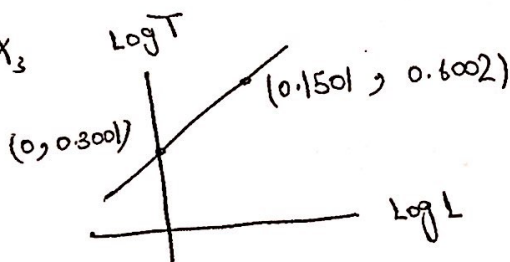
الإجابة ٢

True or false

EX<sub>1</sub> In simple harmonic motion, the angle used must be less than  $50^\circ$  (✓)  
 EX<sub>2</sub> In simple harmonic motion, the particle moves back and forth over the same path (✓)

مثال على الحل

EX<sub>3</sub>



Find  $g$ ?

$$\begin{aligned}
 b &= \frac{1}{2} \log \frac{4\pi^2}{g} \\
 0.3001 &= \frac{1}{2} \log \frac{4\pi^2}{g} \\
 10^{0.3001} &= 10^{\frac{1}{2} \log \frac{4\pi^2}{g}} \\
 10^{0.3001} &= \left( \frac{4\pi^2}{g} \right)^{\frac{1}{2}} \\
 10^{0.3001} &= \sqrt{\frac{4\pi^2}{g}} \Rightarrow g = 9.9 \text{ m/s}^2
 \end{aligned}$$



Ex Fig (8), is obtained by student from the simple pendulum exp, from the graph the gravitational acceleration in  $(\text{cm/s}^2)$  is:

(A) 1058.77

(C) 927.47

(B) 993.57

(D) 1020.66

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$\text{slope} = \frac{2\pi}{\sqrt{g}} = \frac{0.47 - 0.18}{3 - 1.5}$$

$$\frac{0.29}{1.5} = \frac{2\pi}{\sqrt{g}} \Rightarrow g = 1058.7 \text{ cm/s}^2$$

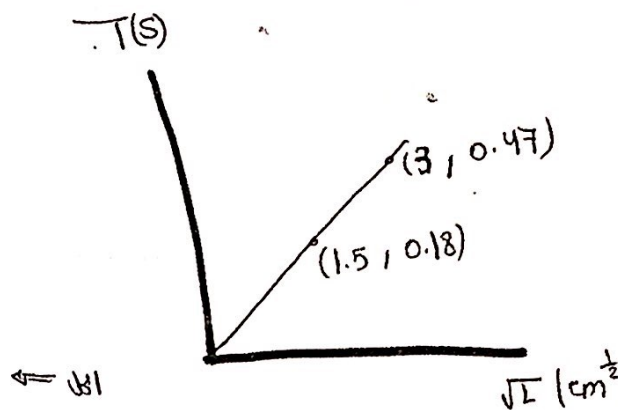


Fig (8)

Ex The relation between periodic time (T) and length of pendulum (L) is given by  $T = c\sqrt{L}$  where (c) is constant. For a certain length the period is (1 sec). If the length is doubled, then the periodic time becomes:

(A) 2.0

(B) 707

(C) 1.732

(D) 1.414

$$L_2 = 2L_1$$

$$T_2 = c\sqrt{L_2}$$

$$\frac{T_2}{T_1} = \frac{c\sqrt{L_2}}{c\sqrt{L_1}} \dots \text{--- ①}$$

$$\frac{T_2}{1} = \frac{\sqrt{2L_1}}{\sqrt{L_1}} \dots \text{--- ②}$$

$$g_{\text{moon}} = \frac{g_{\text{earth}}}{6}$$

$$\sqrt{\frac{L_2}{L_1}} = \frac{1}{1}$$

$$\sqrt{\frac{2L_1}{L_1}} = \frac{T_2}{1} \Rightarrow \sqrt{2} = \frac{T_2}{1} \Rightarrow T_2 = 1.4142 \text{ sec}$$

(D) 1.414

Ex the acceleration due to gravity on the moon is approximately 6 times smaller than the earth. Simple pendulum with length (L) is moved from the earth to the moon then which statement is correct.

(A) the pendulum will swing on moon 6 times faster than on earth.

(B) the pendulum will swing on moon 6 times slower than on earth.

(C) the pendulum will swing on moon 2.5 faster than on earth.

(D) the pendulum will swing on moon 2.5 slower than on earth.

$$N_{\text{moon}} = \frac{t}{T_{\text{period}}} \dots \textcircled{1}$$

$$N_{\text{earth}} = \frac{t}{T_{\text{period}}} \dots \textcircled{2}$$

نقسم المعادلتين : على افتراضهما أنه سوف تأخذ نفس الوقت للتجربة

$$\frac{N_{\text{moon}}}{N_{\text{earth}}} = \frac{\frac{t}{T_{\text{period moon}}}}{\frac{t}{T_{\text{period earth}}}} = \frac{T_{\text{period earth}}}{T_{\text{period moon}}}$$

$$T_{\text{period earth}} = 2\pi \sqrt{\frac{L}{g_{\text{earth}}}} \quad \sqrt{\frac{g_{\text{moon}}}{g_{\text{earth}}}}$$

$$\frac{N_{\text{moon}}}{N_{\text{earth}}} = 2.5 \Rightarrow \frac{2\pi \sqrt{\frac{L}{g_{\text{earth}}}}}{2\pi \sqrt{\frac{L}{g_{\text{moon}}}}} = 2.5 \Rightarrow \sqrt{\frac{g_{\text{earth}}}{g_{\text{moon}}}} = 2.5 \Rightarrow \frac{g_{\text{earth}}}{g_{\text{moon}}} = 6.25 \Rightarrow \frac{g_{\text{earth}}}{g_{\text{moon}}} = 6.25$$

العلاقة عكسية بين T و L  
عندما يكون T ثابتاً  
عندما يكون L ثابتاً  
عندما يكون g ثابتاً  
عندما يكون L ثابتاً  
عندما يكون g ثابتاً  
عندما يكون L ثابتاً  
عندما يكون g ثابتاً

**Ex** For a simple pendulum, If you plot  $\log(T)$  versus  $\log(L)$  you will have a straight line, The slope and y-intercept of the line respectively are:

- أ) 0.6 , 0.3    **ب) 0.5 , 0.3**    ج) 0.3 , 0.5    د) 0.7 , 0.6

ال slope كما اشتقنا في التجربة = 0.5  
وال y-intercept افتراضه 0.3 لأنه الوحيد الذي يعطي slope 0.5

# Experiment (9)

The Behavior of gases

with changes

In temperature  
and pressure.

(gas Laws)

engine\_team



Exp 9: The Behavior of Gases with changes in Temp. and pressure

=> gas law (Boyle's law)

القانون الثاني

$$\frac{P_1 V_1}{n_1 R T_1} = \frac{P_2 V_2}{n_2 R T_2}$$

(at constant T)

$$P_1 V_1 = P_2 V_2 = nRT$$

(Boyle's Law)

P: pressure (mm Hg) الضغط

V: Volume

n: no of moles

T: Temper

R: Constant

\* قانون بويل: أي نقطة ضغط، هناك نفس المالح وعلى نفس الارتفاع لهم نفس الضغط

لأن غاز

$$P_1 V_1 = P_2 V_2$$

\* عند تثبيت درجة الحرارة:  $PV = \text{constant} = nRT$

$$PV = \text{constant} = nRT$$

\* أنواع الضغط:

=>  $P_a$ : atmospheric pressure: أي نقطة مفتوحة ومعرضة للهواء يكون ضغطه

=>  $P_{\text{gas}}$ : pressure of confined gas: فقط الغاز المحصور

=> h: ضغط السائل

manometer



جهاز قياس الضغط:



\* متى نعرف الضغط المؤثر على النقطة المطلوبة دائماً ننظر إلى

حافوه النقطة:

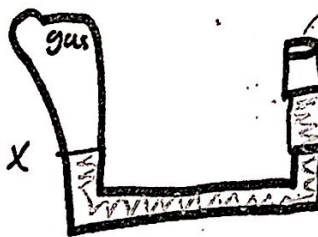
c:  $P_{\text{gas}}$

b:  $P_a$

a:  $h + P_a$

لأن ارتفاع ضغط جوي

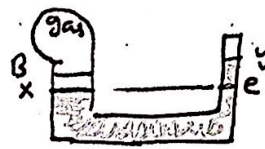
Ex:



$$h = y - e$$

Ex Boyle's Law shows that + to its volume at const

\* السيتامه الرسات :



طبق قانون بويل  
على النقطه e

$$e: \Rightarrow PV = C_1$$

$$\Rightarrow (h + P_a) V = C_1$$

$$\Rightarrow h + P_a = \frac{C_1}{V}$$

$$\Rightarrow h = \frac{C_1}{V} - P_a \quad \leftarrow \text{كما حفظه القانون}$$

$$\Rightarrow h = \frac{C_1}{V} - P_a$$

بناشغل بالانقطه [e]

$$\Rightarrow V = AL$$

$$\Rightarrow h = \frac{C_1}{AL} - P_a \Rightarrow h = \frac{C_2}{L} - P_a \quad \leftarrow \text{كما حفظه القانون}$$

\* رسمه بيانه والتغير بكونه القانون :

①

$$\Rightarrow h = \frac{C_2}{L} - P_a$$

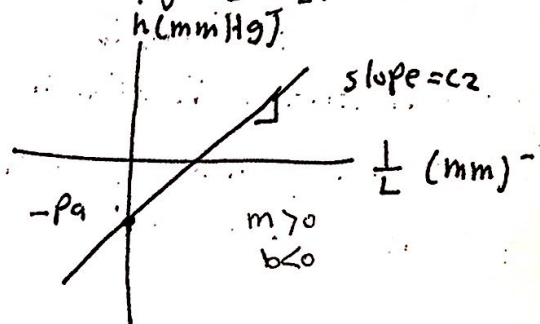
$$\Rightarrow y = mx + b$$

y : h

$$* m = \text{slope} = C_2$$

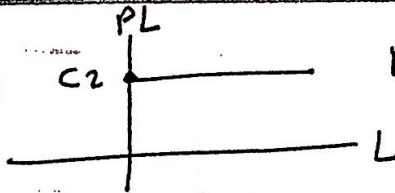
$$x = \frac{1}{L}$$

$$* b = -P_a \quad (\text{التقاط مع الصادات})$$



هذه الرسمه رسمه

②



$$PV = C_1$$

$$* PV = C_1$$

$$P AL = C_1$$

$$PL = \frac{C_1}{A}$$

$$y = mx + b$$

$$PL = 0L + C_2$$

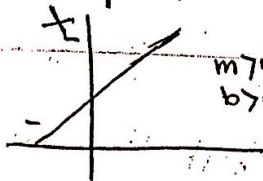
$$\text{slope} = \text{zero}$$

\* Line Parallel to L-axis

مقارنه مع معادله الخط المستقيم :

$$PL = C_2$$

③



②

$$h = \frac{C_2}{L} - P_a$$

$$\frac{1}{L} = \frac{h}{C_2} + \frac{P_a}{C_2}$$

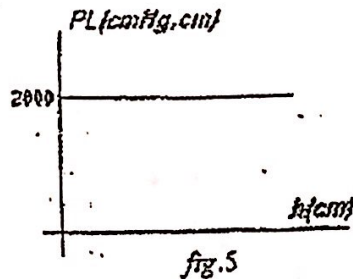
$$\text{slope} = \frac{1}{C_2}$$

$$y\text{-intercept} = \frac{P_a}{C_2}$$



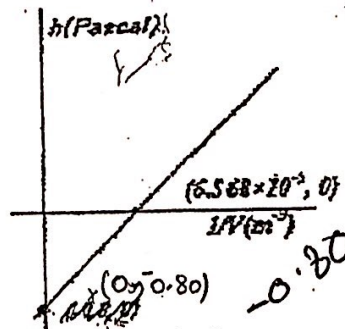
9. In the Boyle's law experiment, if the atmospheric pressure  $P_a = 700 \text{ mmHg}$ . What is the value of  $L$  when  $h = 37.5 \text{ cm}$ ?

- a) 13.9 cm  
b) 18.6 cm  
c) 2.6 cm  
d) 2.7 cm



10. In the Boyle's law experiment, the relation between  $h$  (in Pascal) and  $1/V$  (in  $\text{m}^{-3}$ ) is shown in fig. 6. The atmospheric pressure (in Pascal) is:

- a) 0.8  
b) -0.8  
c) -0.9  
d) 0.9



11. Depending on fig. 6, if the number of moles  $n = 5 \text{ moles}$  and the Universal Gas Constant  $R = 8.314 \text{ J/mole.K}$ , then the temperature of the gas is:

- a) 329°C  
b) 56°C  
c) 293°C  
d) 20°C

a) Solu:  $C_2 = b$  &  $h = \frac{C_2}{L} - P_a \Rightarrow 37.5 \times 10 = \frac{2000}{L} - 700 \Rightarrow L = 1.86 \text{ m}$

10)  $PV = nRT \Rightarrow P = \frac{nRT}{V} \Rightarrow (h + P_a) = \frac{nRT}{V}$

$h = \frac{nRT}{V} - P_a$

y-intercept =  $-P_a$   
 $-0.8 = -P_a$

#9 Sol  $P_a = 0.8 \text{ Pascal}$

$h = y$   
 $\frac{1}{V} \Rightarrow x$

slope  $\Rightarrow nRT$

y-intercept  $\Rightarrow -P_a$

11) slope =  $nRT$   
 $\frac{\Delta y}{\Delta x} = 5 \times 8.314$   
 $\frac{0 - (-0.8)}{6.56 \times 10^{-5} - 0} = 5 \times 8.314$   
 $\frac{0.8}{6.56 \times 10^{-5}} = 5 \times 8.314$   
 $T = 293.3 \text{ K}$

- 3- Two readings were taken for  $h$  (the difference between the two mercury levels) and  $L$  (the length of the enclosed gas) as shown in the table.

|             |      |      |
|-------------|------|------|
| $h$ (cm Hg) | 40.0 | 12.8 |
| $L$ (cm)    | 15.0 | 20.0 |

The atmospheric pressure is \_\_\_\_\_

$h = \frac{C_2}{L} - P_a$

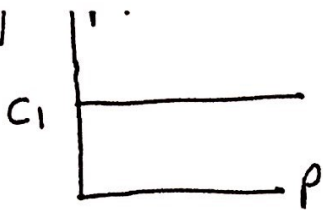
$P_a??$

Solu:  $40 = \frac{C_2}{15} - P_a$  (1)  
 $12.8 = \frac{C_2}{20} - P_a$  (2)  
 $\Rightarrow -40 = -\frac{C_2}{15} + P_a$   
 $12.8 = \frac{C_2}{20} - P_a$

$40 = \frac{-1628.7}{15} - P_a$   
 $P_a = -2228.7 \text{ Pascal}$



4



\* Parallel to P-axis

$PV = C_1$

$y = mx + b$

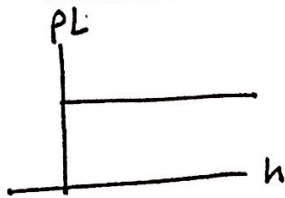
$y = mx + b$

$PV = 0P + b$

$\frac{PV}{V} = \frac{0P}{V} + \frac{b}{V}$

y-intercept

5



slope = 0

$b = C_2$

Line Parallel to h-axis

$PV = C_1$

$PAL = C_1$

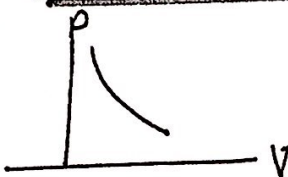
$PL = \frac{C_1}{A}$

$PL = C_2$

$y = mx + b$

zero  $C_2$

8

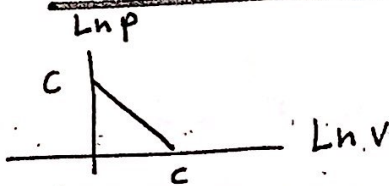


منحنى الزمان

طريقة القياس:

$cm \times 10 \rightarrow mm$

8



$PV = C$

$\ln PV = C$

$\ln P + \ln V = C$

$\ln P = C - \ln V$

slope = -1

y-inter = C

X

(1) Boyle's law can be written as:

(a)  $PV = \text{constant}$

(b)  $P/V = \text{constant}$

(c)  $V/T = \text{constant}$

(d)  $VT = \text{constant}$

المعادلة

$PV = \text{Constant}$

17. If the tube in fig.7 was filled by mercury and the atmospheric pressure is 760 mmHg, find the pressure of the confined gas.

- (a) 810
- (b) 785
- (c) 750
- (d) 725

Solut:  $P_x = P_c$

$P_{gas} = h + P_a$

$P_{gas} = (80 - 30) + 760$

$P_{gas} = 810 \text{ mmHg}$

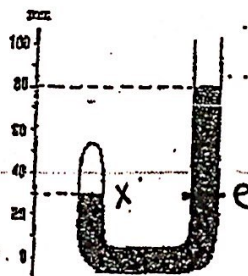


fig 7

X

### 8- Gas Laws:

B) A change of atmospheric pressure during the experiment:

(a) Would affect the results of the experiment.

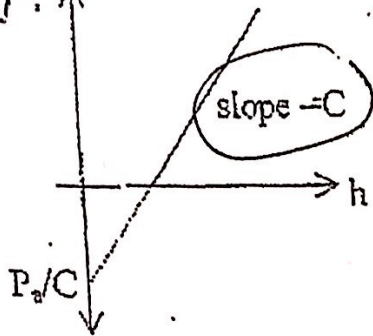
b) Would have no effect on the results of experiment.

✓

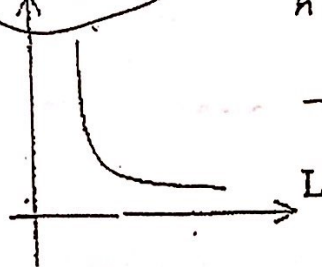
(a) لا تأثير

2) Which of the following graphs is correct for Boyle's law. If  $P$ ,  $V$  and  $P_a$  represent the pressure (in cm Hg), volume of gas ( $\text{cm}^3$ ) and atmospheric pressure (in cm Hg):

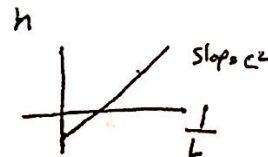
(a)  $1/L$



(b)  $(P_a + h)L$

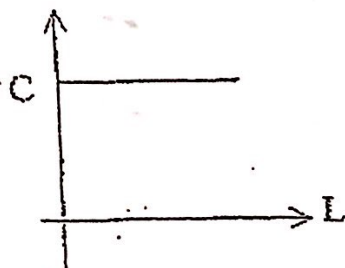


$$h = \frac{c_2}{L} - P_a$$

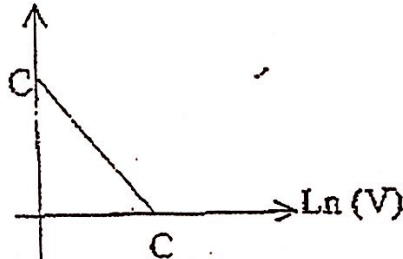


$C_2 = C$   
نقطة في حالة  
تكونت عن  
الاسمات  
لننا فقط في قسمها  
يعرف في ماري

(c)  $(P_a + h)$



(d)  $\ln(P)$



$$h = \frac{c_2}{L} - P_a$$

الرسم الصحيحة d وقد تم ذكر ذلك سابقاً  
أما سبب الخطأ الرسومات a و b و c

$$a: h = \frac{c_2}{L} - P_a \Rightarrow \frac{h + P_a}{c_2} = \frac{1}{L}$$

باتي

$$\Rightarrow \frac{1}{L} = \frac{h}{c_2} + \frac{P_a}{c_2} \rightarrow \text{التقاطع}$$

وذلك في الرسم كالتالي

والرسم الصحيحة

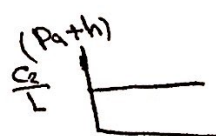
slope =  $c_2$

$$b: h = \frac{c_2}{L} - P_a \Rightarrow (h + P_a) = \frac{c_2}{L} \Rightarrow (h + P_a)L = c_2 + 0L$$

الرسم هذا slope = 0

$$\therefore (P_a + h) = \frac{c_2}{L} + 0L$$

التقاطع  $\frac{c_2}{L}$



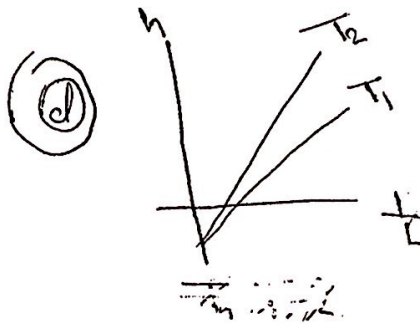
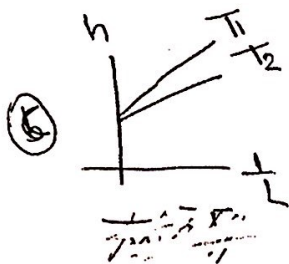
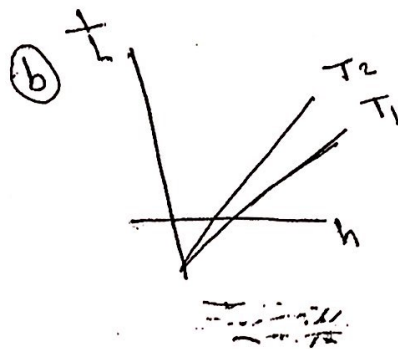
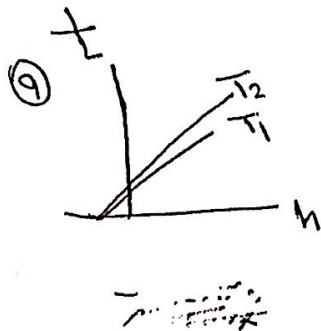
والرسم b  
 $b > 0$   
 $m = 0$

d:

تم ذكرها سابقاً



Ex Which graph is correct ... If  $T_1 > T_2$



→ رسمها المصحح  
والميل زائجا في حال كان ال intercept y موجبا  
كما ارتفعنا لارتفاع يزداد الميل  
لذلك في رسمه ⑨ ال رسمه موحدة وكن  
 $T_2 > T_1$

رسمه ⑥ ال رسمه خاطئة أصلا

الكل  
تم شرحها  
سابقا

→ رسمها المصحح  
والميل زائجا في حال كان ال intercept y سلبا  
كما نزلنا لارتفاع يزداد الميل  
لذلك في رسمه ④ ال رسمه خاطئة أصلا

④ ال رسمه موحدة و  $T_1 > T_2$

→  
رسمه أخرى  
مب

الاجابة ④



# True or False:

Write True (T) or False (F) for each statement (each one has 2 mark)

- 1) In Kinematics experiment, the tape represents the distance only. (X) distance and time
- 2) The unit of heat capacity is Calory. (X)  $\rightarrow$  calory / C
- 3) The parallex is considered as random error. (X) personal error
- 4) The error in measuring the diameter of cylindrical rod once using a micrometer is 0.005 mm. (X) (✓)
- 5) Boyle's law shows that the pressure of a gas is inversely proportional to its volume at constant temperature. (✓)
- 6) The specific heat capacity depends on the type of material. (✓)
- 7) In force and motion experiment, we increase the inclination of track to illuminate the normal force that acts on cart. (X) الميلان
- 8) We can get the resultant force (القوة المحصلة) and equilibrant force (القوة الموازنة) directly from the force table (vectors). (X) equilibrant force
- 9) In simple harmonic motion, the angle used must be less than 50°. (✓)
- 10) In elastic collision (تصادم مرن), the momentum and kinetic energy are conserved because the system is isolated. (X)
- 11) In force and motion experiment, when we increase the load on the cart and the driving force is constant, the acceleration of cart will be constant. (X) م ثابت،  $a$  يتغير
- 12) In simple harmonic motion, the particle moves back and forth over the same path. (✓)

engine\_team

1- Write the word "True" if the statement is true, and the word "False" if the statement is false: (4 marks)

- F a) The rate of change of position is called average velocity. ✓  
 F b) When two or more forces act simultaneously at a point on an object, the single force applied at the same point that would produce the same effect is the resultant force. (T)  
 F c) When the velocity of a body increases or decreases the same amount in successive units of time, the velocity is uniform. (F)  
 T d) In the force and motion experiment, the driving force is  $F = ma$  where  $m$  is the total mass of the system (i.e.  $m = m_c + m_a + m_h$ ).

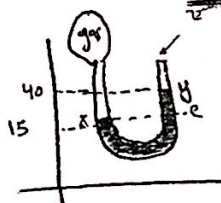
$$V_{Avg} = \frac{\Delta x}{\Delta t}$$

ما ياتو (اخر ما تبقو على)  
 قلة صفة في بقا تا بقو لوعة  
 resultant force هو قلة امة

ابعاد قوتنا اول  
 ولا بقو  
 ثابت

$$\begin{aligned}
 \checkmark \text{ driving force} &= ma = mhg \\
 &= (m_c + m_a + m_h)g
 \end{aligned}$$

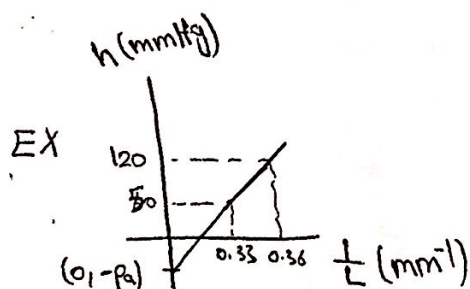
EX سؤال على المصفي



$$P_a = 750 \text{ mmHg}$$

Find the pressure of the confined gas?

$$\begin{aligned}
 P_x &= P_e \\
 P_{gas} &= P_a + h \\
 &= 750 + (40 - 15) \\
 &= 750 + 25 = 775 \text{ mmHg} \quad \#
 \end{aligned}$$



Find  $P_a$ ? (the atmospheric pressure)

$$h = \frac{C}{L} - P_a$$

y-intercept =  $P_a$  لقيمة  
0.33, 50

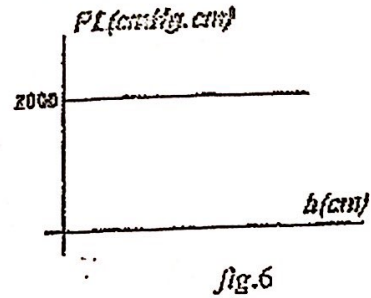
$$\begin{aligned}
 \text{slop} &= \text{slop} \\
 (0.33, 50) \text{ } \& \text{ } (0.36, 120) \text{ } \& \text{ } (0.33, 50)
 \end{aligned}$$

$$P_a = 720 \text{ mmHg}$$

$$\begin{aligned}
 \frac{\Delta y}{\Delta x} &= \frac{\Delta y}{\Delta x} \\
 \leftarrow \frac{50 - P_a}{0.33 - 0} &= 2333.3
 \end{aligned}$$

11. In the Boyle's law experiment, if the atmospheric pressure  $P_a = 700 \text{ mmHg}$ . What is the value of  $L$  when  $h = 37.5 \text{ cm}$ ?

- a) 13.9 cm
- b) 18.6 cm**
- c) 2.6 cm
- d) 2.7 cm
- e) can not be determine



$$PL = \frac{C_2}{L} + oh$$

y-intercept

$$\parallel P_a = \frac{C_2}{L} - h$$

$$70 = \frac{2000}{L} - 37.5$$

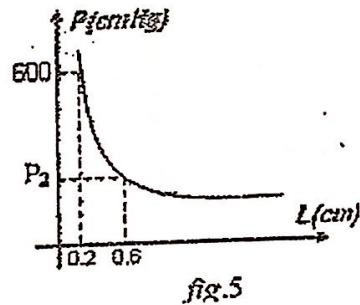
$$107.5 = \frac{2000}{L}$$

$$L = 18.6 \text{ cm}$$

**b) 18.6**

10. In the Boyle's law experiment, the following graph was obtained. The value of  $P_2$  will be:

- a) 200**
- b) 300
- c) 1200
- d) 1800



$$P_1 = \frac{C_1}{L_1} \parallel P_2 = \frac{C_2}{L_2}$$

لها لهما

$$\frac{P_1}{P_2} = \frac{L_2}{L_1}$$

$$\frac{600}{P_2} = \frac{0.6}{0.2} \Rightarrow P_2 = 200 \text{ cmHg}$$

**a) 200**

Q12) Gases laws: The graph that should be obtained if  $PV$  is plotted against  $P$  is

- a) a line parallel to  $P$  axis**
- b) a line passes through origin
- c) a line parallel to  $PV$  axis
- d) none of the above

$$PV = nRT + O$$



**a)**



**EX** The pressure of the expressed gas in the following figure is:

المسألة الثاني  
2015

(a) 1050 mmHg

(b) 780 mmHg

(c) 720 mmHg

(d) 450 cmHg

(e) 450 mmHg

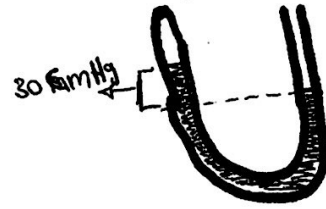
Sol:

$$P_{\text{gas}} = P_a + h$$

$$= 750 + 300$$

$$= \underline{450 \text{ mmHg}}$$

h ملاطمة من  
تولدت من  
mmHg ← 30 cmHg



$P_a = 750 \text{ mmHg}$

الإجابة هي (e)

**EX** According to the figure the atmosphere pressure in mmHg is:

المسألة  
الثاني  
2015

(a) 450

(b) 600

(c) 850

(d) 400

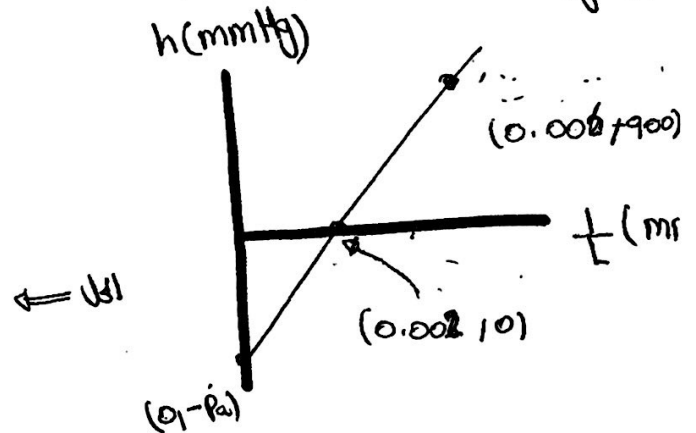
(e) 550

$$\text{slope} = \frac{\text{slope}}{(0.002, 0)} = \frac{(0.006, 900) - (0.002, 0)}{(0.006 - 0.002) - (0.002 - 0)}$$

$$= \frac{900 - 0}{0.006 - 0.002} = \frac{0 - P_a}{0.002 - 0}$$

$$225000 = \frac{P_a}{0.002}$$

$$P_a = \underline{450 \text{ mmHg}}$$



**EX** In Boyle's Law experiment, Boyle's Law is  $PV = \text{constant}$  at constant:

المسألة الثاني  
2015

(a) pressure

(b) Temperature

(c) volume

(d) All of the above

Experiment (II)

specific heat capacity  
of metals

engine\_team

# Ex 11: specific heat Capacity of metals.

kg  $\rightarrow$  g  $\times 10^3$

ملاحظة

المتاوتن لهذه التجربة :

$$\frac{Q}{\Delta T} = mc$$

Q:  $\Rightarrow$  heat  $\Rightarrow$  وحدة : Calori / Jou

$\Delta T$ :  $\Rightarrow$  Temperature  $\Rightarrow$   $^{\circ}C$  (الدرجة)

m:  $\Rightarrow$  mass (g) / (kg) الكتلة

c:  $\Rightarrow$  specific heat Capacity ( $\frac{Cal}{g \cdot ^{\circ}C}$ )  $\Rightarrow$  الـ  $\frac{Cal}{g \cdot ^{\circ}C}$

\* Remark: 1 Calori = 4.18 Jou

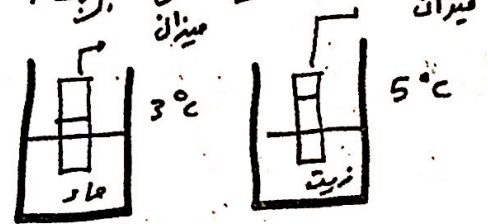
c: specific heat Capacity:  $\Rightarrow$  مقدار الطاقة اللازمة لرفع درجة حرارة 1 غرام من المادة بدرجة 1  $^{\circ}C$

The quantity of heat required to raise the temperature of one gram of a substance by  $1^{\circ}C$

depend on  $\Rightarrow$  type of metal only  $\Rightarrow$  تعتمد على نوع المعدن

فقد الحرارة  $\Rightarrow$  فقدان

\* مثال توضيحي لفكر التجربة :



\* هنا وضعنا الواسن أخذ نفس درجة الحرارة  $30^{\circ}C$  كده (إجمالي).  
\* الزيت سخف أسرع بالزغامة عند نفس درجة حرارة الماء.  
\* الزيت سخف أسرع ويبرد أسرع بالتالي يحتاج إلى طاقة أقل  $\Rightarrow$  أقل

\* الماء يبرد أبطأ ويبسفن أبطأ بالتالي تحتاج إلى طاقة أكبر  $\Rightarrow$  أكبر c أكبر

c الزيت > c الماء

تعتمد دائماً على نوع المادة : c

سؤال متداول

\* Ex: If the specific heat Capacity of body is small then it:  $\Rightarrow$   $\frac{Q}{\Delta T}$   $\Rightarrow$  heat Capacity  $\Rightarrow$  فقدان

soluion:  $\Rightarrow$  Loses heat faster and gains heat faster

\*  $\left(\frac{Q}{\Delta T}\right) \Rightarrow$  heat Capacity  $\Rightarrow$  فقدان

$\frac{Cal}{^{\circ}C}$   
 $\frac{J}{^{\circ}C}$   
 $\frac{Cal}{F}$   
 $\frac{Cal}{Kelvin}$

1 Cal = 4.18 J

\* ملاحظة :  $K = ^{\circ}C + 273$

F = 1.8  $^{\circ}C$  + 32



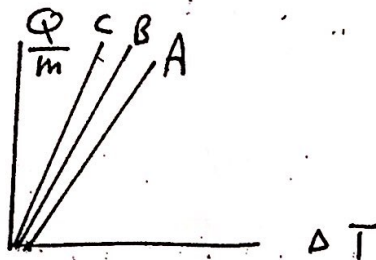
The Unit of the heat Capacity is Cal?? answer  $\rightarrow$  false (X)

\* heat capacity: هي الطاقة اللازمة لرفع درجة الحرارة بمقدار واحد فقط

The heat absorbed by one part of the system is equal to the heat lost by the other part of the system.

\* Remark:  $\frac{Q}{\Delta T}$  : depend on  $\text{Type of metal}$  and  $\text{mass}$

EX



\*  $\text{slope} = c$   $\rightarrow$  بزيادة

الخط ميل  $\Rightarrow$  اعلى  $\Rightarrow$

اعلى ميل  $\Rightarrow$  اقل  $\Rightarrow$

$$① * \frac{Q}{\Delta T} = mc$$

$$② * \frac{Q}{\frac{Q}{m}} = \frac{\Delta T}{\Delta T} c$$

y                      x                      slope  $\leftarrow$

\* متى خل الاستقامة على هذه التجربة: لازم نعرف

$$\Delta Q_{\text{lost}} = \Delta Q_{\text{gains}} \quad \text{قانون حفظ الطاقة}$$

$$\Delta Q_{\text{lost}} - \Delta Q_{\text{gains}} = \text{zero}$$

$$\sum \Delta Q_{\text{المادة}} = \text{zero}$$

دائماً تكونت هذه المعادلة  $\Rightarrow$

$$\sum \Delta Q = \text{zero} \quad \text{لجميع المعاد}$$

$$\Delta Q_{\text{المادة}} = (mc \Delta T)_{\text{المادة}} \Rightarrow \Delta T = T_f - T_i$$

له بعض النظم من المادة التي فقدت طاقة أو المادة التي اكتسبت طاقة

Ex: A metal of mass 100g lost 150 cal of heat the difference between the final and initial temperature is 15°C what the specific heat capacity of the metal??

Solution:  $\Delta Q = (m c \Delta T)$

metal :  $\Delta Q$  فقط في  
محيطها القانون الأول

$$\Rightarrow 150 = 100 * C * 15^\circ \Rightarrow \frac{150}{100 * 15} = C \Rightarrow C = 0.1 \text{ cal/g}$$

### Specific heat capacity experiment:

1) A 60 gm piece of a metal is heated to 120°C and then dropped into a beaker with 30gm of water ( $C_w = 1 \text{ cal/g} \cdot ^\circ\text{C}$ ) at 20°C. If the equilibrium temperature of the system is 31°C, then the specific heat capacity (in cal/g°C) of metal closes to:  
(Ignore the mass of beakers).

①

- a) 0.04  
c) 0.08

- b) 0.05  
d) 0.06

②

1) In this experiment, the heat transfer from the metal to the water until:

- a) The specific heat capacity of water becomes equal to the metal.  $\times$   
b) The heat capacity of water become equal to the metal  
c) The final temperature of water equals the initial temperature of metal.  
d) The final temperature of water equals the final temperature of metal.

Solution: ①  $\sum \Delta Q_{\text{metal}} = \text{Zero}$

$$\Delta Q_{\text{metal}} + \Delta Q_{\text{water}} = 0$$

$$(m c \Delta T)_{\text{metal}} + (m c \Delta T)_{\text{water}} = 0$$

$$(60 * C * (T_f - T_i))_{\text{met}} + (30 * 1 * (T_f - T_i)) = 0$$

$$(60 * C * (31 - 120)) + (30 * (31 - 20)) = 0$$

$$-5340C + 330 = 0$$

$$\frac{-5340C}{-5340} = \frac{-330}{-5340} \Rightarrow C = 0.06 \text{ cal/g} \cdot ^\circ\text{C}$$

\* هذه الطريقة سهلة وبسيطة بحيث  $\Delta T = T_f - T_i$  دائماً على ما كانت الحالة

② d: The final temperature of water equals the final temperature of metal.



### Specific Heat Capacity Experiment:

(5) 100g of copper piece is heated to  $50^{\circ}\text{C}$  and dropped in 60g of water at  $80^{\circ}\text{F}$ , the specific heat capacity of copper and water is 0.14, 1 cal/g.  $^{\circ}\text{C}$ , respectively. The final equilibrium temperature  $T_f$  is (in  $^{\circ}\text{C}$ ):

- (a) 25.9 (b) 13.8 (c) 31.1 (d) 38.3

(6) Depending on the previous question, the heat capacity of copper piece (in cal/  $^{\circ}\text{C}$ ) is:

- (a) 12 (b) 60 (c) 0.12 (d) 14

(7) In this experiment, you measure the temperature of boiling water because it represents:

- (a) The initial temperature of the metal.  
(b) The initial temperature of the cup.  
(c) The final temperature of the metal.  
(d) The temperature of the atmosphere.

Solut: 5)  $T_{\text{water}} = 80^{\circ}\text{F}$

$$F = 1.8^{\circ}\text{C} + 32$$

$$80 = 1.8^{\circ}\text{C} + 32$$

$$T_{\text{water}} = 26.6^{\circ}\text{C}$$

$$* \sum \Delta Q = 240$$

$$\Rightarrow (\Delta Q)_{\text{copper}} + (\Delta Q)_{\text{water}} = 0$$

$$\Rightarrow (m C \Delta T)_{\text{copper}} + (m C \Delta T)_{\text{water}} = 0$$

$$\Rightarrow (100 * 0.14 (T_f - 50))_{\text{copper}} + (60 * 1 * (T_f - 26.6))_{\text{water}} = 0$$

$$(14 (T_f - 50)) + (60 (T_f - 26.6)) = 0$$

$$14 T_f - 700 + 60 T_f - 1596 = 0$$

$$74 T_f - 2296 = 0$$

$$74 T_f = 2296$$

$$T_f = 31^{\circ}\text{C}$$

$$* T_f_{\text{copper}} = T_f_{\text{water}}$$

\* نلاحظ: دالة  $T_f$  متساوية لجميع المواد الموجودة في النظام فمساوية إلى

ملاحظة: دالة  $T_f$  متساوية لجميع المواد الموجودة في النظام فمساوية إلى



Ex: Two Blocks of metal are in an isolated system  
 One with a heat Capacity of  $[2000 \text{ J/C}^\circ]$  and an  
 initial temperature of  $[427^\circ\text{C}]$  and the second with heat  
 Capacity of  $[500 \text{ J/C}^\circ]$  at a temperature of  $[90^\circ\text{C}]$   
 brought into thermal contact, what's the final  
 temperature of the blocks after thermal equilibrium  
 is reached?

- a) 370.6    b) 347.6    c) 539.3    d) ~~359.6~~  
 e) 995.6

$$\left( \frac{\Delta Q}{\Delta T} \right)_{\text{first metal}} = 2000$$

$$\frac{\Delta Q}{T_F - 427} = 2000 \quad \text{--- (1)}$$

$\Delta Q$  = heat

Thermal equilibrium

$$\left( \frac{\Delta Q}{\Delta T} \right)_{\text{second metal}} = 500$$

$$\frac{\Delta Q}{T_F - 90} = 500 \quad \text{--- (2)}$$

$$\Rightarrow \frac{\Delta Q}{T_F - 427} = \frac{2000}{5000} \quad \Leftarrow$$

isolated system

$$\frac{\Delta Q}{(T_F - 90)}$$

$$T_F - 90 = 4 \Rightarrow T_F - 90 = 4 T_F - 1708$$

**Ex** 432 J of energy is required to raise the temperature of aluminum from 59°F to 35°C, calculate the mass (in g) of aluminum: [specific heat capacity of aluminum is 0.90 J/g·°C].

2016 ☐ (a) 24 ☐ (b) 33 ☐ (c) 54 ☐ (d) 144 ☐ (e) 233

$T_i = 59^\circ\text{F} \Rightarrow \frac{59-32}{1.8} = T_i^\circ\text{C}$   
 $T_i = 15^\circ\text{C}$   
 $T_f = 35^\circ\text{C}$

$$\Delta Q_{\text{AL}} = (m c \Delta T)_{\text{AL}}$$

$$432 = m \times 0.90 (T_f - T_i)$$

$$432 = m \times 0.90 (35 - 15)$$

$$m = 24 \text{ g}$$

**Ex** two metal samples, X and Z of the same mass and initially at 25°C, are heated so that each receives the same amount of thermal energy, which metal will have the highest final temperature: [specific heat capacity  $c_X = 0.851 \text{ J/g}\cdot^\circ\text{C}$   $c_Z = 0.8951 \text{ J/g}\cdot^\circ\text{C}$ ]

- 2016 ☐ (a) metal X ☐ (b) metal Y ☐ (c) both reach the same temperature ☐ (d) none of above since we don't know the mass of metals

**Ex** A combination of 0.125 kg of water at 20°C, 0.4 kg of Aluminum at 26°C and 0.1 kg of copper at 100°C is mixed in an insulated container and allowed to come to thermal equilibrium. Ignore any energy transfer to or from the container. What's the final temperature of the mixture?

$c_{\text{water}} = 4186 \text{ J/kg}\cdot^\circ\text{C}$  /  $c_{\text{AL}} = 900 \text{ J/kg}\cdot^\circ\text{C}$  /  $c_{\text{copper}} = 387 \text{ J/kg}\cdot^\circ\text{C}$

2016 ☐ (a) 21.1 ☐ (b) 700 ☐ (c) 22.1 ☐ (d) 23.6 ☒ (e) 25.7

$\sum \Delta Q = 0$

$$\Delta Q_{\text{water}} + \Delta Q_{\text{copper}} + \Delta Q_{\text{AL}} = 0$$

$$(m c \Delta T)_{\text{water}} + (m c \Delta T)_{\text{copper}} + (m c \Delta T)_{\text{AL}} = 0$$

$$0.125 \times 4186 \times (T_f - 20) + (0.1 \times 387 \times (T_f - 100)) + (0.4 \times 900 \times (T_f - 26)) = 0$$

$$523.25 T_f - 10465 + 38.7 T_f - 3870 + 360 T_f - 9360 = 0$$

$$921.95 T_f - 23695 = 0$$

$$T_f = 25.7^\circ\text{C}$$



### Specific Heat:

0- what is the main source of error in this experiment? Due to this error will the value of specific heat obtained be greater or smaller than the expected value?

10- lost of heat in the surrounding / it will be smaller than the expected value.  
Random error

دائماً ضائع الطاقة يؤدي الى تقليل القيمة

Q9) Specific heat: In this experiment you measure the temperature of the boiling water because it represents

- a) the final temperature of the metal    b) the initial temperature of the cup  
c) the initial temperature of the metal    d) the temperature of the atmosphere

Q16) The unit of heat is

a) C

b) K

c) J

d) W

Joule Calori

Q17) If the specific heat capacity of a body is small it

a) loses heat faster

b) gains heat slower

c) has a small density

d) none of the above



$$20) \frac{Q}{\Delta T} = mc$$

$$1] \frac{Q}{\Delta T} = m_1 c_1 = 50 \times 0.42 = 21$$

$$2] \frac{Q}{\Delta T} = m_2 c_2 = 50 \times 0.36 = 18$$

$$21, 18 \quad \underline{b} \text{ ع$$

### 9- Specific Heat:

A) A 100 gm copper block with specific heat 0.1 cal/gram °C at a temperature (T= 95°C) calorimeter is immersed a calorimeter 100 grams of water initially at 20 °C. If the final temperature is 25 °C. The heat capacity of the calorimeter is —

$$\sum \Delta Q = 0$$

$$\Delta Q_{\text{copper}} + \Delta Q_{\text{calorimeter}} + \Delta Q_{\text{water}} = 0$$

$$(mc\Delta T) + (mc\Delta T) + (mc\Delta T) = 0$$

$$(100 \times 0.1 \times (25 - 95)) + (100 \times C \times (25 - 20)) + (100 \times 1 \times (25 - 20)) = 0$$

$$-700 + 500C + 500 = 0$$

$$500C = +200$$

$$C = +0.4 \text{ cal/g} \cdot ^\circ\text{C}$$

B) To minimize the heat loss to the surroundings, one should:

(a) Insulate the calorimeter.

b) Increase the initial temperature of the copper block.

c) Decrease the mass of the water in the calorimeter.

d) Increase the mass of the water in the calorimeter.

### 12- Specific Heat Capacity of Metals:

⊗ The unit of Specific heat capacity is  $\text{cal/g} \cdot ^\circ\text{C}$  or  $\text{J/g} \cdot ^\circ\text{C}$

⊗ The major error contributing to this experiment is

Random error

(Lost heat to surroundings)

$$6) \frac{Q}{\Delta T} = mc \Rightarrow 100 * 0.14 = 14 \text{ Cal/}^\circ\text{C}$$

- \* Two pieces of metal of equal masses (50g) are put in 100g water of temperature  $20^\circ\text{C}$  and the specific heat capacity of water is  $1 \text{ cal/g}^\circ\text{C}$ . The specific heat capacity and initial temperature of the metals ( $m_1$  and  $m_2$ ) are  $0.42 \text{ cal/g}^\circ\text{C}$ ,  $55^\circ\text{C}$  and  $0.36 \text{ cal/g}^\circ\text{C}$ ,  $70^\circ\text{C}$ , respectively. Depending on this information answer questions (18 to 20).

18. The equilibrium temperature ( $T_f$ ) of the system is:  $\rightarrow$

(a)  $28.2^\circ\text{C}$

(b)  $47.3^\circ\text{C}$

(c)  $31.8^\circ\text{C}$

(d)  $73.6^\circ\text{C}$

مسألة جمع  
أكاد

19. The heat gained by the metals (in cal) is:

(a) 1155

(b) 1180

(c) 1260

(d) 1320

20. The heat capacity of the two metals  $m_1$  and  $m_2$ , respectively, in ( $\text{cal/}^\circ\text{C}$ ) is:

(a) 18, 21

(b) 21, 18

(c)  $8.4 \times 10^3$ ,  $7.2 \times 10^3$

(d)  $7.2 \times 10^3$ ,  $8.4 \times 10^3$

$$18: \sum \Delta Q_{\text{metals}} = 0$$

$$\Delta Q_1 + \Delta Q_2 + \Delta Q_{\text{water}} = 0$$

$$(m c \Delta T)_{m_1} + (m c \Delta T)_{m_2} + (m c \Delta T)_{\text{water}} = 0$$

$$(50 * 0.42 * (T_f - 55))_{m_1} + (50 * 0.36 * (T_f - 70))_{m_2} + (100(T_f - 20)) = 0$$

$$(21(T_f - 55)) + (18(T_f - 70)) + (100 T_f - 2000) = 0$$

$$21 T_f - 1155 + 18 T_f - 1260 + 100 T_f - 2000 = 0$$

$$139 T_f - 4415 = 0$$

$$\frac{139 T_f}{139} = \frac{4415}{139} \Rightarrow 31.76 \Rightarrow 31.8^\circ\text{C}$$

المعادلة التي فيها الماء = المعادلات التي فيها المعادن

$$m_w c_w \Delta T_w = m_1 c_1 \Delta T_1 + m_2 c_2 \Delta T_2$$

$$= 100 * 1 * (31.8 - 20)$$

$$31.8 = 11.8$$