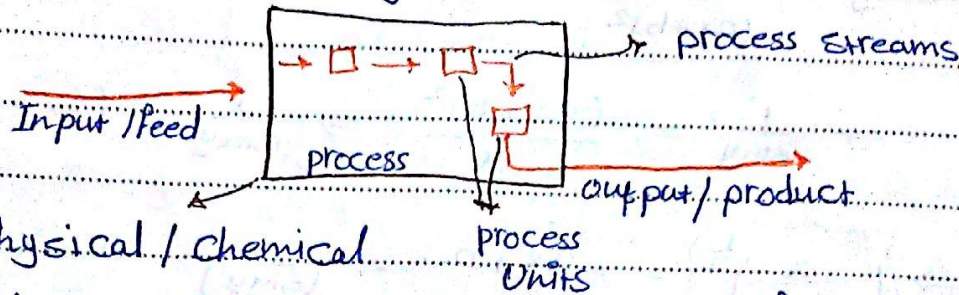


## Chapter 3 → Process and Process Variables.

Process: any operation or series of operations by which a particular objective is accomplished.

\* In Chemical Engineering



physical / chemical changes in a substance / mixture of substances.

### Chemical Engineer

Design of a process

Operate a process day-by-day

Formulation of a process and specifications of industrial process units

running of the process (troubleshooting)

(reactor / separation unit, heat exchange, ... etc.)

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1- Mass and Volume &

density = mass per unit volume  $[ \frac{M}{L^3} ]$

$\frac{M}{L^3} \rightarrow \frac{g}{cm^3}$   
 $\downarrow$   
 $\frac{kg}{m^3}$   
 $\downarrow$   
 $\frac{lbm}{ft^3}$



Subject:.....

\* specific volume = volume occupied by unit mass

$$= \frac{1}{\text{density}} \quad [E] \quad \frac{L^3}{M} \quad \begin{matrix} \nearrow \text{cm}^3/\text{g} \\ \nearrow \text{m}^3/\text{kg} \\ \searrow \text{ft}^3/\text{lbm} \end{matrix}$$

\* liquid and solids & density  $\neq f(p)$ , changes very slightly w/ temperature.

e.g. a)  $0^\circ\text{C}$ ,  $e = 0.99988 \text{ g/cm}^3$

b)  $4^\circ\text{C}$ ,  $e = 1.00000 \text{ g/cm}^3$

c)  $100^\circ\text{C}$ ,  $e = 0.95838 \text{ g/cm}^3$

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\* Specific gravity = ratio of substance density  $e$  to the density of a reference substance at specific conditions,  $e_{\text{ref}}$

$$SG = \frac{e}{e_{\text{ref}}}$$

\*  $e_{\text{ref}}$  is usually that of water at  $4^\circ\text{C}$  (for liq. and solids)

e.g.  $SG = 0.6 \frac{20^\circ}{40}$

= specific gravity of that substance

at  $20^\circ\text{C}$  with ref to water @  $4^\circ\text{C}$  is 0.6

$$e_{\text{ref}} (\text{water @ } 4^\circ\text{C}) = 1.000 \text{ g/cm}^3$$

$$= 1000.0 \text{ kg/m}^3$$

$$= 62.43 \text{ lbm/ft}^3$$



TYS - Pg # 44

Q28 SG = 0.50  $\rho = ? \text{ g/cm}^3$

$$\rho = \text{SG} \times \rho_{\text{ref}} = 0.5 \times 1.000 = 0.500 \text{ g/cm}^3$$

$$\text{specific volume} = \frac{1}{\rho} = \frac{1}{0.50} = 2 \text{ cm}^3/\text{g}$$

$$\rho = 0.50 \times 62.43 = 31.22 \text{ lbm/ft}^3$$

$V = 3 \text{ cm}^3$ ,  $m = ?$

$$m = \rho V = \frac{0.5 \text{ g}}{\text{cm}^3} \times 3 \text{ cm}^3 = 1.50 \text{ g}$$

$m = 18 \text{ g}$ ,  $V = ?$

$$V = \frac{m}{\rho} \Rightarrow \frac{18 \text{ g}}{0.500 \text{ g}} = 36 \text{ cm}^3$$

## 2- Flow rates

A Mass and Volumetric Flow rate

Flow rate is rate at which a Material is transported

mass Flow rate

volumetric Flow rate

$$[=] \frac{\text{L}^3}{\text{s}} (\dot{V})$$

$$[=] \frac{\text{M}}{\text{s}} (\dot{m})$$

$$\rho = \frac{m}{V} = \frac{\dot{m}}{\dot{V}}$$

TYS - Pg # 46

Q1  $\dot{m} = 6.59 \text{ g/s}$ ,  $\rho = 0.659 \text{ g/cm}^3$ ,  $V = ?$

$$V = \frac{m}{\rho} = \frac{6.59 \text{ g}}{0.659 \text{ g}} = 10.0 \text{ cm}^3/\text{s}$$

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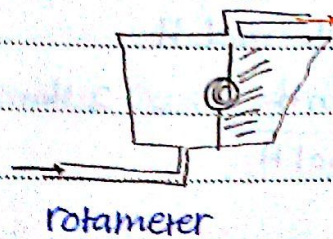




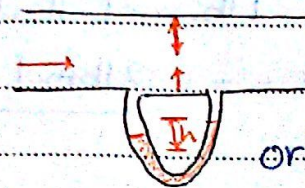
$$\left. \begin{array}{l} m_{in} = m_{out} \\ e_{in} v_{in} = e_{out} m_{out} \end{array} \right\} \begin{array}{l} \text{if } e_{in} = e_{out} \\ \Rightarrow v_{in} = v_{out} \end{array}$$

### B. Flow rate measurement &

Using Flow meter (device)



rotameter



orifice meter

### 3. Chemical Composition &

needed because most materials are in mixture.

physical properties  $\longleftrightarrow$  composition.

\* Molecular weight =  $\sum$  atomic weight =  $M$

SI  $\left[ \begin{array}{l} \text{gram-mole} = \text{g-mole} = \text{mol} \\ \text{kg-mole} = \text{kmol} \end{array} \right.$

Amer  $\left[ \text{lb-mol}, \text{ton-mol} \right]$

eg.  $M(\text{NH}_3) = 14 + 1 \times 3 = 17 \text{ g/mol}$

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$\text{kg/kmol}$

$\text{lbm/lbmol}$

\*  $\frac{\text{g}}{\text{lbm}} = \frac{\text{mol}}{\text{lbmol}} \quad \left[ \frac{\text{kg}}{\text{lbm}} = \frac{\text{kmol}}{\text{lbmol}} \right]$



$$m = M \times N$$

$N = \# \text{ of mole}$

$$\dot{m} = M \times \dot{N}$$

$\dot{N} = \text{molar flow rate}$

TYS- Pg #49s

Q3s- 1 lb-mol  $H_2O$ , how many lb-mol, lbm of  $H_2$  and H are in there?

1 lb-mol  $H_2O$  has 2 lb-mol H

$$= \frac{2 \text{ lbmol H}}{1 \text{ lbmol H}} \times 1 \text{ lbmol H} = 2 \text{ lbmol H}$$

1 lbmol  $H_2O$  has 1 lbmol  $H_2$

$$= \frac{1 \text{ lbmol } H_2}{1 \text{ lbmol } H_2} \times 2 \text{ lbmol } H_2 = 2 \text{ lbmol } H_2$$

Q4s- 2 kmol  $C_3H_8 = ?$  g-mole = ? Kg

$$\frac{2 \text{ kmol } C_3H_8}{1 \text{ kmol}} \times 10^3 \text{ mol} = 2000 \text{ mol } C_3H_8$$

$$m(\text{kg}) = M \cdot N(\text{kmol})$$

$$M(C_3H_8) = 3 \times \underset{\text{C}}{12} + 8 \times \underset{\text{H}}{1} = 44 \text{ Kg/mol}$$

$$m = \frac{44 \text{ Kg}}{\text{kmol}} \times 2 \text{ kmol} = 88 \text{ Kg}$$

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Q5s-  $\dot{m}(H_2) = 100 \text{ Kg/h}$ , molar flowrate mol/h?

$$\dot{m} = M \cdot \dot{N}$$

$$\dot{N} = \frac{\dot{m}}{M} = \frac{100 \text{ Kg}}{\text{h}} \times \frac{\text{kmol}}{2 \text{ Kg}} \times \frac{10^3 \text{ mol}}{\text{kmol}} = 50 \times 10^3 \text{ mol/h}$$



Subject: .....

\* Mass Fraction and Mole Fractions

$$\text{Mass Fraction} = x_A = \frac{\text{mass of A}}{\text{total mass}}$$

$$\text{percent by mass} = 100 \times x_A$$

$$\text{Mole Fraction} = y_A = \frac{\text{moles of A}}{\text{total moles}}$$

$$\text{mole percent} = 100 \times y_A$$

☒ mass Fraction  $\xleftrightarrow[\text{Calculations}]{\text{basis of}}$  mole Fraction

TYS - pg # 525

Q1  $\rightarrow$   $M(H) = 1$  ,  $M(Br) = 80$

a)  $x_{Br}$       b)  $y_{Br}$       in pure HBr?

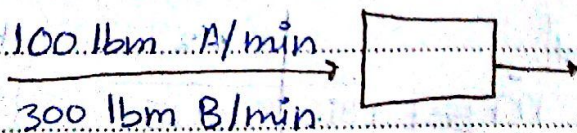
Basis of calculations : m: 1 mol HBr

$$= 1 \text{ mol H} + 1 \text{ mol Br}$$

$$x_{Br} = \frac{M_{Br}}{m_{\text{total}}} = \frac{\overset{\text{mol Br}}{\downarrow} 1 \times \overset{\text{g/mol Br}}{80}}{\underset{\text{H}}{1 \times 1} + \underset{\text{Br}}{1 \times 80}} = \frac{80}{81} \text{ g Br / g HBr}$$

$$y_{Br} = \frac{N_{Br}}{N_{\text{total}}} = \frac{1}{1+1} = 0.5 \text{ mol Br / mol HBr}$$

Q2



$$\dot{m} = M \cdot \dot{U}$$

$$M_A = 2, \quad M_B = 3$$

$$\dot{m}_A = 100 \text{ lbm A/min}$$

$$x_A = \frac{100}{100 + 300} = 0.25 \text{ lbm A / lbm}$$

$$y_A = \frac{100/2}{100/2 + 300/3} = \frac{50 \text{ lbmol A}}{50 + 100} = 0.33 \text{ lbmol A / lbmol}$$

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$$\dot{n}_B = 300/3 = 100 \text{ lbmol/B./min}$$

$$\dot{n}_{\text{total}} = 400 \text{ lbmol/min}$$

$$\dot{n}_{\text{total}} = \frac{100}{2} + \frac{300}{3} = 150 \text{ lbmol/min}$$

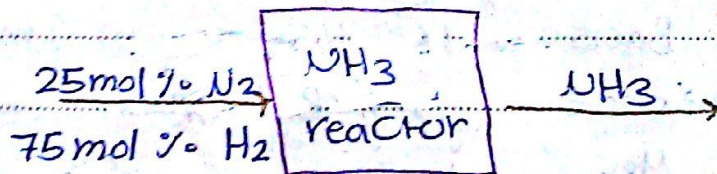
\* Average Molecular Weight  $\rightarrow$

$$\bar{M} = \sum y_i M_i \Rightarrow y_i = \text{mole Fraction}$$

$$\frac{1}{\bar{M}} = \sum \frac{x_i}{M_i} \rightsquigarrow x_i = \text{mass Fraction}$$

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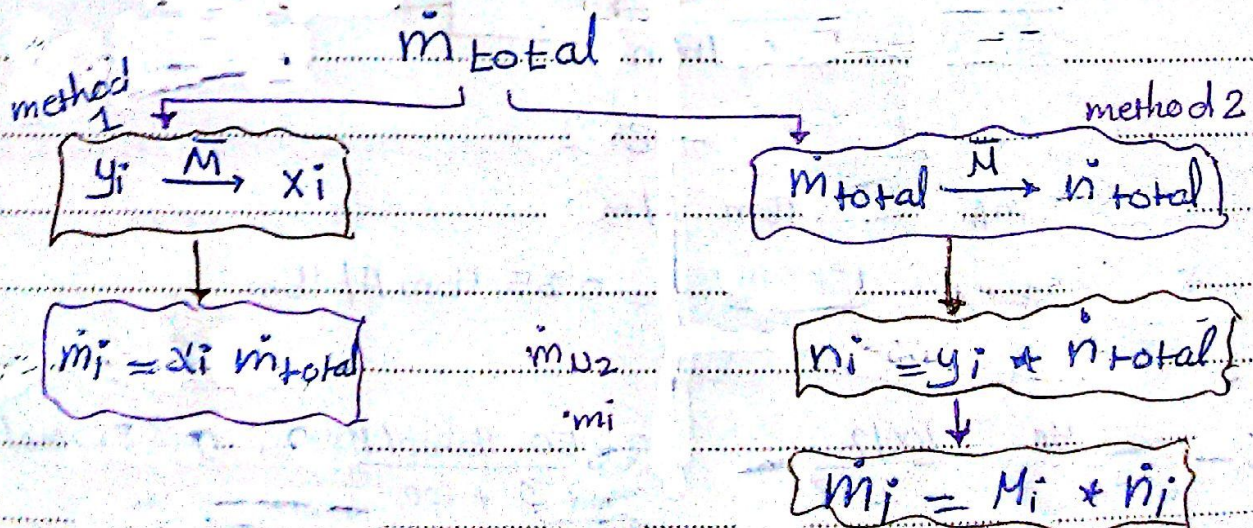
\* P3-17  $\rightarrow$



3000 kg/h

Find  $\rightarrow m_{N_2} = ??$

$$M(N_2) = 28, \quad M(H) = 2$$





Subject: .....

Method 1 ~

To convert  $y_i \rightarrow x_i$ , we need a basis ~

Basis: 100 mol mixture.

|                               | $N_2$                                                             | $H_2$                                        |
|-------------------------------|-------------------------------------------------------------------|----------------------------------------------|
| $y_i$                         | 0.25                                                              | 0.75                                         |
| $n_i$                         | $0.25 * 100$<br>$= 25$<br>$\downarrow * 28$<br>$M_{N_2}$<br>700 g | 75<br>$\downarrow * 2$<br>$M_{H_2}$<br>150 g |
|                               | $m_{total} = 850 g$                                               |                                              |
| $x_i = \frac{m_i}{m_{total}}$ | $\frac{700}{850} = 0.82$                                          | $\frac{150}{850} = 0.18$                     |

$$\dot{m}_{N_2} = X_{N_2} * \dot{m}_{total}$$

$$= 0.82 * 3000$$

$$= 2470 \text{ kg}_{N_2}/h$$

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Method (2)  $\bar{M} = \sum y_i M_i$   
 $= (0.25)(28) + (0.75)(2)$   
 $= 8.5 \text{ g/mol}$

$$\dot{n}_{\text{total}} = \frac{\dot{m}_{\text{total}}}{\bar{M}} = \frac{3000}{8.5} = 353 \frac{\text{kmol}}{\text{h}}$$

$$\dot{n}_{N_2} = y_{N_2} * \dot{n}_{\text{total}} = 0.25 * 353 = 88.2 \frac{\text{kmol } N_2}{\text{h}}$$

$$\dot{m}_{N_2} = \dot{n}_{N_2} * M_{N_2} = (88.2)(28) = 2470 \text{ kg } N_2 / \text{h}$$

\* P3-19  $\Rightarrow$

mixture: 10 mol% ethyl alcohol =  $y_1$   $M_1 = 46$

75 mol% ethyl acetate =  $y_2$   $M_2 = 88$

15 mol% acetic acid =  $y_3$   $M_3 = 60$

a)  $x_i = ??$

b)  $\bar{M} = ??$

c) if  $n_2 = 25 \text{ mol}$ ,  $m_{\text{total}} = ?$

Basis  $\Rightarrow 100 \text{ mol}$

|                                      | (1)                        | (2)              | (3)                                                                      |
|--------------------------------------|----------------------------|------------------|--------------------------------------------------------------------------|
| $y_i$                                | 0.10                       | 0.75             | 0.15                                                                     |
| $n_i$                                | 10                         | 75               | 15                                                                       |
| $m_i$                                | $10 * 46 = 460$            | $75 * 88 = 6600$ | $15 * 60 = 900 \rightarrow m_{\text{total}} = \sum m_i = 7960 \text{ g}$ |
| $x_i = \frac{m_i}{m_{\text{total}}}$ | $\frac{460}{7960} = 0.058$ | 0.38             | 0.11                                                                     |

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$$b) \bar{M} = \sum y_i M_i$$

$$= (0.10)(46) + (0.75)(88) + (0.15)(60) \\ = 79.6 \text{ g/mol}$$

$$c) m_{\text{total}} = \bar{M} \times n_{\text{total}}$$

① طريق

$$= \frac{m_i}{x_i}$$

$$n_{\text{total}} = \frac{n_2}{y_2} = \frac{25}{0.75} = 33.3 \text{ kmol}$$

$$m_{\text{total}} = (79.6)(33.3) = 2653 \text{ kg}$$

method 2  $\rightarrow m_2 = n_2 \times M_2$

$$= 25 \times 88 = 2200 \text{ kg}$$

$$m_{\text{total}} = \frac{2200}{0.83} = \frac{m_2}{x_2} \Rightarrow 2653 \text{ kg}$$

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## \* Concentration

$$\text{mass concentration} = \frac{\text{mass of component}}{\text{Volume of mixture}}$$

$$[=] \frac{\text{Kg}}{\text{m}^3}, \frac{\text{g}}{\text{cm}^3}, \frac{\text{lbm}}{\text{ft}^3}, \frac{[\text{M}]}{[\text{L}^3]}$$

$$\text{molar conc.} = \frac{\# \text{ of moles of a component}}{\text{Volume of mixture}}$$

$$\downarrow [=] \frac{\text{Kmol}}{\text{m}^3}, \frac{\text{lb-mol}}{\text{m}^3}, \frac{\text{lb-mol}}{\text{ft}^3}, \dots$$

$$\text{molarity} = \text{molar conc. in } \frac{\text{mol}}{\text{L}} \quad \begin{matrix} \swarrow & \searrow \\ \text{solute} & \text{solution} \end{matrix}$$

$$2 \text{ molar A} = 2 \text{ mol A} / \text{L. soln.}$$

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S

T

A

R

S Notebook



\* parts per million (ppm), parts per billion (ppb) used to express the conc of 'trace species' in mixture of gases or liquids

mass ratio  $\rightarrow$  liquid

mole ratio  $\rightarrow$  gas

$$* \text{ ppm} = \frac{\text{Parts of species (g, mol)}}{10^6 \text{ parts of mixture (g, mol)}} = \frac{y_i \times 10^6}{x_i \times 10^6}$$

$$* \text{ ppb} = \frac{\text{parts of species (g, mol)}}{10^9 \text{ parts of mixture (g, mol)}} = \frac{y_i \times 10^9}{x_i \times 10^9}$$

Ty - Pg 54  $\rightarrow$

Liquid - mostly water - contain 125 ppb phenol (mass ratio)

1. mass fraction = ?

$$x = \text{ppb} \times 10^{-9} \\ = 125 \times 10^{-9}$$

2. How many mg phenol in 1 kg liquid ?

|                                       |                   |                  |
|---------------------------------------|-------------------|------------------|
| $125 \times 10^{-9} \text{ g phenol}$ | $10^3 \text{ mg}$ | $10^3 \text{ g}$ |
| $\text{g liquid}$                     | $\text{g}$        | $\text{kg}$      |

$$= 125 \times 10^{-3} \text{ mg phenol / kg liquid}$$

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$$3. C_{ph} (g/L) = ?$$

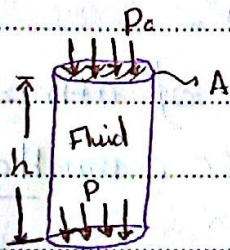
assuming  $\rho \approx \rho_w = 1g/cm^3$

$$C_{ph} = \frac{125 \times 10^{-9} \text{ g phenol}}{\text{g soln}} \left| \frac{1g}{cm^3} \right| \frac{10^3 cm^3}{L} = 125 \times 10^{-6} \text{ phenol/L}$$

\* Pressure ~

$$P = \frac{F}{A} \quad [=] \quad \frac{N}{m^2} \quad , \quad \frac{lb_f}{in^2} \quad , \quad \frac{\text{dyne}}{cm^2}$$

$\downarrow$  Pa                       $\downarrow$  psi



$$F = F_0 + W$$

$$PA = P_0 A + \rho A h g$$

$$P = P_0 + \rho g h$$

hydro static pressure

atmospheric pressure

If  $P_0 = 0$ ,  $P = \rho g h$

$$= \rho g h$$

↳ head pressure

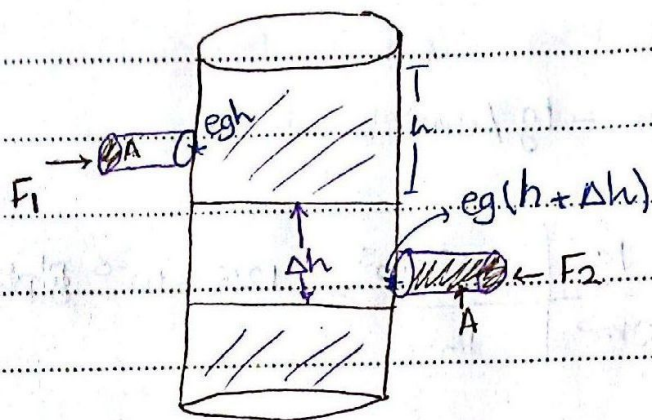
Example ~ Express  $2 \times 10^5$  Pa in terms of mmHg

$$P_h = \frac{2 \times 10^5}{\rho g} = \frac{2 \times 10^5 \frac{N}{m^2}}{13600 \frac{kg}{m^3} \times 9.8 \frac{m}{s^2}} = 1.5 \text{ mHg} = 1500 \text{ mmHg}$$

$\downarrow$   $\rho_{Hg}$

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$$F_2 > F_1$$

$$\Rightarrow P_2 > P_1$$

$$(A_2 = A_1)$$

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\* Atmospheric pressure is

pressure at the base of column of air located at measurement point.

(top of column = top of atmosphere)

\* at sea level  $P_{atm} = 1 \text{ atm} = 760.0 \text{ mmHg}$

1) \* Absolute pressure  $\leftrightarrow$  pressure of zero corresponds to perfect vacuum.

2) \* Gauge pressure = pressure relative to atmospheric pressure

$$P_{abs} = P_g + P_{atm}$$

$\downarrow$                        $\downarrow$   
 $P_{sia}$                        $P_{sig}$

\*  $P_g$  can be -ve

if  $P_{abs} = 75.0 \text{ cmHg}$ ,  $P_{atm} = 76.0 \text{ cmHg}$

$$P_g = 75.0 - 76.0 = -1 \text{ cmHg}$$



Subject: .....

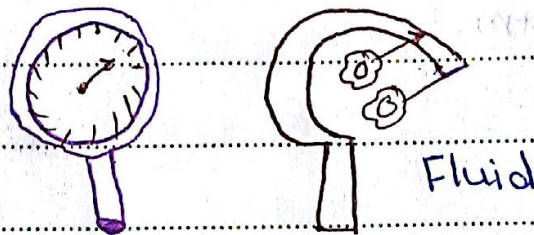
\* Fluid Pressure Measurement & →

pressure measurement devices & →

1) \* Elastic - Element method

Bourden tubes

the most common

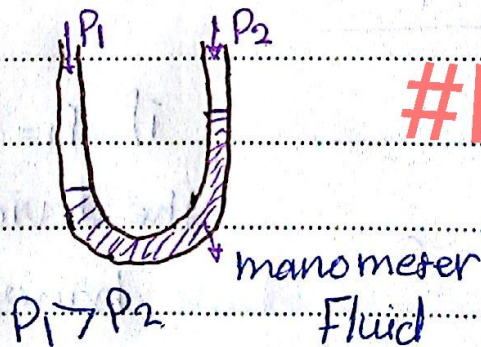


\* Measures the gauge pressure

From perfect vacuum to 7000 atm

- Below 3 atm, manometer gives more accurate measurement

2) liquid - Column methods : manometer



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3) Electrical Methods :

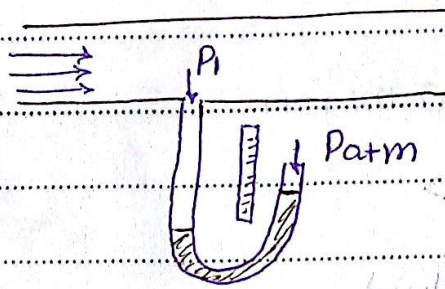
Strain gauge.

\*



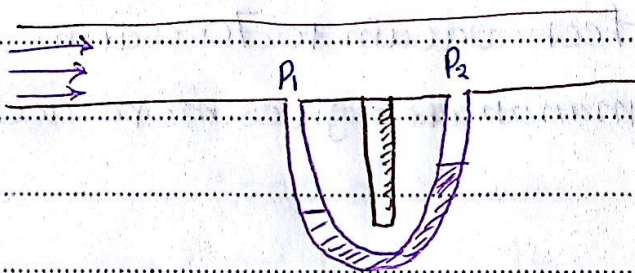
\* Three types of Manometers:

1- Open - end manometer.

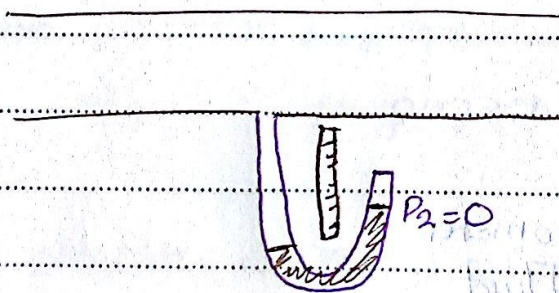


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2- Differential Manometer.

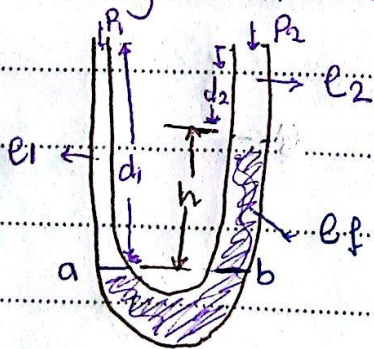


3- Sealed - end manometer.



if  $P_1 = P_{atm}$   
the device is called  
barometer.

\* Reading the Pressure from the Manometer.



$P_a = P_b$  (continuous fluid  
at the same level)



Subject: .....

$$P_a = P_b$$

$$P_1 + \rho_1 g d_1 = P_2 + \rho_2 g d_2 + \rho_f g h \quad \boxed{h = d_1 - d_2}$$

1) \* Differential manometer

$$\rho_1 = \rho_2 = \rho_3$$

$$P_1 - P_2 = (\rho_f - \rho) g h$$

2) \* IF Fluid (1) and Fluid (2) are gases.

$$\rho_1 \ll \rho_f, \rho_2 \ll \rho_f$$

$$[P_1 - P_2 = \rho_f g h]$$

3) \* IF  $P_1$  and  $P_2$  are head pressure

$$\boxed{P_1 - P_2 = h}$$

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\* Temperature

a measure of the average kinetic energy possessed by a substance molecules.

\* Temp is determined indirectly by measuring (device name)

1- electrical resistance a conductor (resistance thermometer)

2- Voltage at the conjunction of two dissimilar metals (thermocouple)



### 3. Spectra of emitted radiation (pyrometer)

#### H. Volume of fixed mass of fluid (thermometer)

#### - Temp Scales:-

1) Celsius (centigrade) scale :  $T_f(\text{water at } 1 \text{ atm}) = 0^\circ\text{C}$

$$T_b(\text{water at } 1 \text{ atm}) = 100^\circ\text{C}$$

$$\text{Absolute Zero} = -273.15^\circ\text{C}$$

2) Fahrenheit Scale :  $T_f = 32^\circ\text{F}$  } absolute =  $-459.67^\circ\text{F}$   
 $T_b = 212^\circ\text{F}$  } Zero

3) Kelvin = Celsius + 273.15 } absolute temp  
 # absolute zero = 0

4) Rankine = Fahrenheit + 459.67

absolute zero = 0

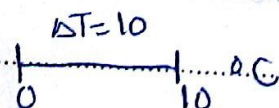
$$* T(\text{K}) = T(^{\circ}\text{C}) + 273.15$$

$$T(^{\circ}\text{R}) = T(^{\circ}\text{F}) + 459.67$$

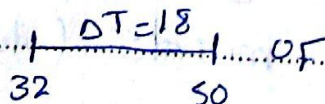
$$T(^{\circ}\text{R}) = 1.8 T(\text{K})$$

$$T(^{\circ}\text{F}) = 1.8 T(^{\circ}\text{C}) + 32$$

$$\Delta T(^{\circ}\text{C}) = \frac{\Delta T(^{\circ}\text{F})}{1.8}$$



$$\Delta T(\text{K}) = \frac{\Delta T(^{\circ}\text{R})}{1.8}$$



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$$\Delta T(K) = \Delta T(^{\circ}C)$$

$$\Delta T(^{\circ}R) = \Delta T(^{\circ}F)$$

P3.48 ~ a)  $T = 85^{\circ}F$  to  $^{\circ}R$ ,  $^{\circ}C$ ,  $K$

$$T(^{\circ}R) = 85 + 460 = 545^{\circ}R$$

$$T(^{\circ}C) = \frac{85 - 32}{1.8} = 29.4^{\circ}C$$

$$T(K) = 29.4 + 273.15 = 302.55 K$$

c)  $\Delta T = 85^{\circ}C$ , to  $K$ ,  $^{\circ}F$ ,  $^{\circ}R$

$$\Delta T(K) = 85 K$$

$$\Delta T(^{\circ}F) = 1.8(85) + 32 = 185^{\circ}F$$

$$\begin{aligned}\Delta T(^{\circ}R) &= 185 + 459.67 \\ &= 644.67^{\circ}R\end{aligned}$$

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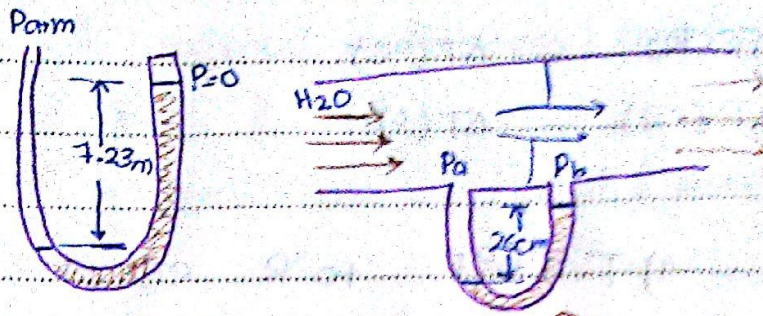
21 / Oct / 2015

Subject: .....

manometer Fluid of unknown density

$P_{\text{atm}} = 756 \text{ mmHg}$

P3-43



What is  $\Delta P = P_a - P_b$  in mmHg?

Soln  $\Delta P = (\rho_f - \rho) g h$   
↓  
water

For the barometer

$$\Delta P = (P_f - \rho_{\text{air}}) g h$$

$$P_{\text{atm}} - 0 = (\rho_f) g (7.23 \text{ m})$$

|          |                |          |
|----------|----------------|----------|
| 756 mmHg | 101325 Δ5      |          |
|          | m <sup>2</sup> | 760 mmHg |

|          |                      |                        |       |                          |
|----------|----------------------|------------------------|-------|--------------------------|
| $\rho_f$ | Kg<br>m <sup>3</sup> | 9.8m<br>s <sup>2</sup> | 7.23m | N·s <sup>2</sup><br>kg·m |
|----------|----------------------|------------------------|-------|--------------------------|

$$\rho_f = 1420 \text{ kg/m}^3$$

$$\Delta P_{a \rightarrow b} = (1420 - 1000) (9.8) (0.26 \text{ m})$$

$$= 8.0 \text{ mmHg}$$

#Madar\_team