



Heat and Mass Transfer Operations

Second semester 2016/2017

Student name:

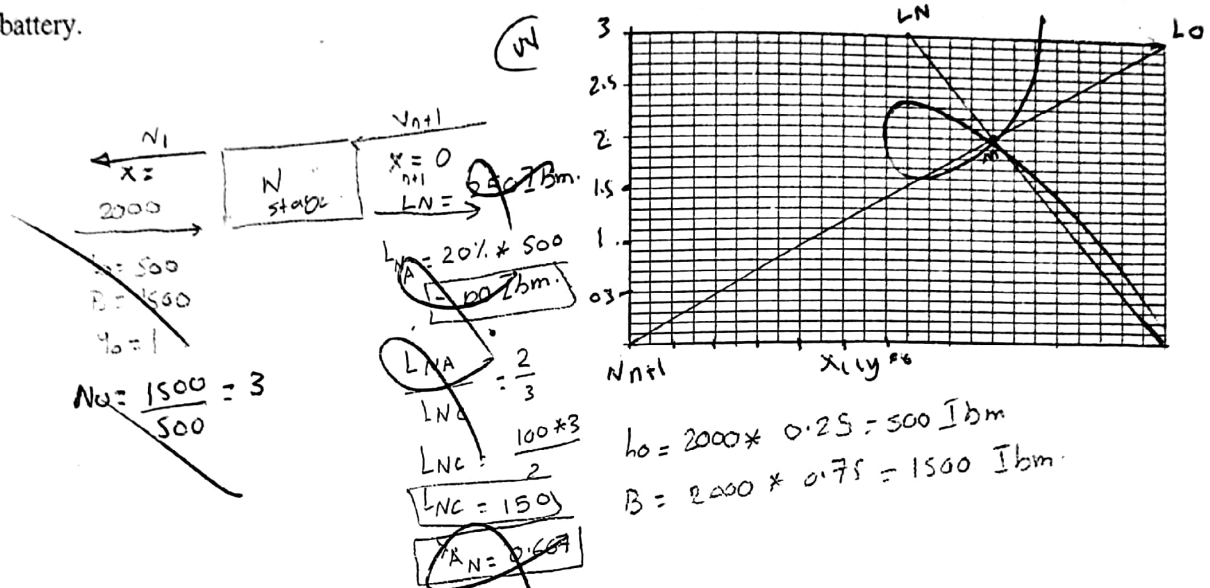
Student No.: ~~XXXXXXXXXX~~ Seat No.: ~~XXXXXXXXXX~~

Quiz #3

March 23, 2017

2000 lbm of waxed paper per day is to be dewaxed in a continuous countercurrent multistage leaching. The waxed paper contains, by weight, 25% paraffin wax and 75% paper pulp. Pure kerosene is used as solvent to leach paraffin wax. The flow rate of paraffin wax in the final underflow slurry is 20% of the paraffin wax flow rate fed to the battery. Experiments show that the underflow slurry from each stage is essentially contains 2 lb of paraffin wax-kerosene solution per 3 lb of insoluble paper pulp. Use N-xy diagram to:

- Find the reasonable flow rate of kerosene stream introduced to the leaching battery.
- Determine the corresponding flow rate and composition for the overflow exit stream leaves leaching battery.





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Heat and Mass Transfer Operations

Second semester 2016/2017

Student name: [REDACTED]

Student No.: [REDACTED]

Seat No.: 35

Quiz #3

March 23, 2017

2000 lbm of waxed paper per day is to be dewaxed in a continuous countercurrent multistage leaching. The waxed paper contains, by weight, 25% paraffin wax and 75% paper pulp. Pure kerosene is used as solvent to leach paraffin wax. The flow rate of paraffin wax in the final underflow slurry is 20% of the paraffin wax flow rate fed to the battery. Experiments show that the underflow slurry from each stage is essentially contains 2 lb of paraffin wax-kerosene solution per 3 lb of insoluble paper pulp. Use N-xy diagram to:

- Find the reasonable flow rate of kerosene stream introduced to the leaching battery.
- Determine the corresponding flow rate and composition for the overflow exit stream leaves leaching battery.

Feed 2000 lbm

$$(A) = 0.25 \times 2000 = 500 \text{ lbm Solul. (paraffin wax)}$$

$$\text{Paper pulp} = 1500 \text{ lbm.} = (0.75 \times 2000)$$

$$N_0 = \frac{1500}{\text{Solution}} = \frac{1500}{L_0}$$

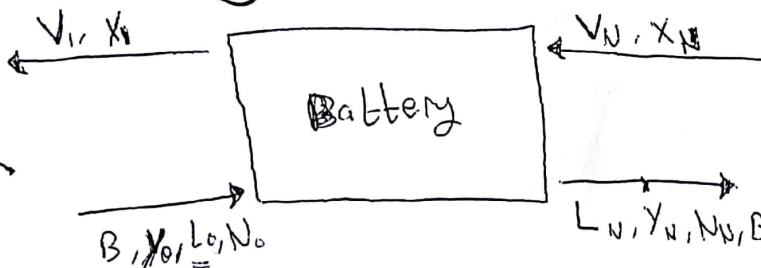
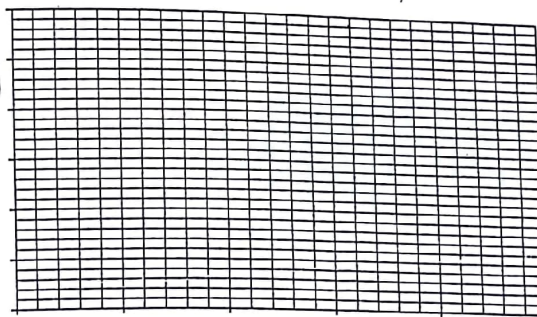
$$L_0 = (0.25)(2000)$$

$$\frac{2 \text{ solution}}{3 \text{ paper pulp}} \rightarrow N = \frac{3}{2} = 1.5$$

in each solution stage

so

$$L_0 = \frac{1500}{1.5} = 1000$$





Heat and Mass Transfer Operations

First semester 2017/2018

Student name: [REDACTED]

Student No.: [REDACTED]

Seat No.: 34

Quiz #3

November 15, 2017

In a single-stage leaching of oil from certain vegetable seeds, 200 kg of the seeds containing 20 wt% oil is leached using pure hexane solvent. The mass ratio of solution to insoluble solid for the slurry underflow is essentially constant at 0.5 kg solution/kg insoluble solid. Find the reasonable amount of solvent required. With such reasonable amount of solvent, calculate the amounts and compositions of the overflow and the underflow slurry leaving the stage.

$B = 200 \text{ kg}$

0.2% oil leaching

0.5 kg solution
kg insoluble

$N = \frac{B}{L}$

$= 200 \div 0.2 = 1000$

$N = \frac{B}{L} = \frac{200}{40} = 5$

pure hexane $x_2 = 0$

$x_1 = 0.2$

$y = 0.5$

R-L:

$\frac{V}{M} = \frac{L \cdot M}{L \cdot V}$

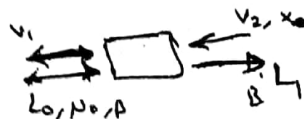
$\frac{40}{M} =$

3.6

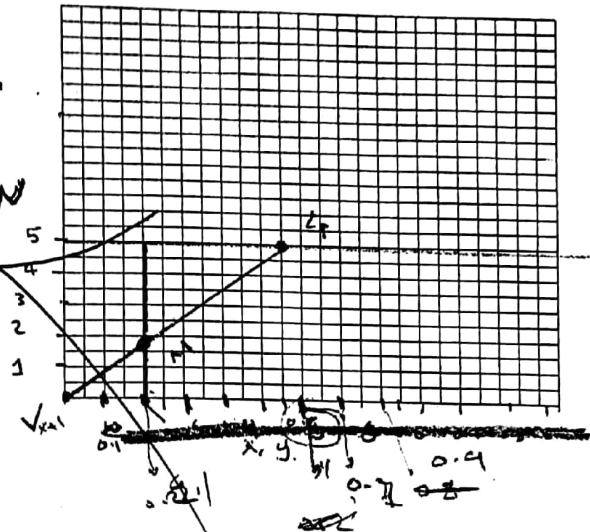
200.5

$L = ?$

$N = \frac{B}{L} = \frac{200}{0.5} = 400$



$M = V_1 + L_0 = V_2 + B$



200 kg

5 kg

$y = \frac{N-1}{N}$

200 kg seeds
20%

0.5 solution

$200 \div 0.5 = M = 200.5 \text{ kg}$



Heat and Mass Transfer Operations
Student name: ~~XXXXXXXXXX~~
Quiz #4

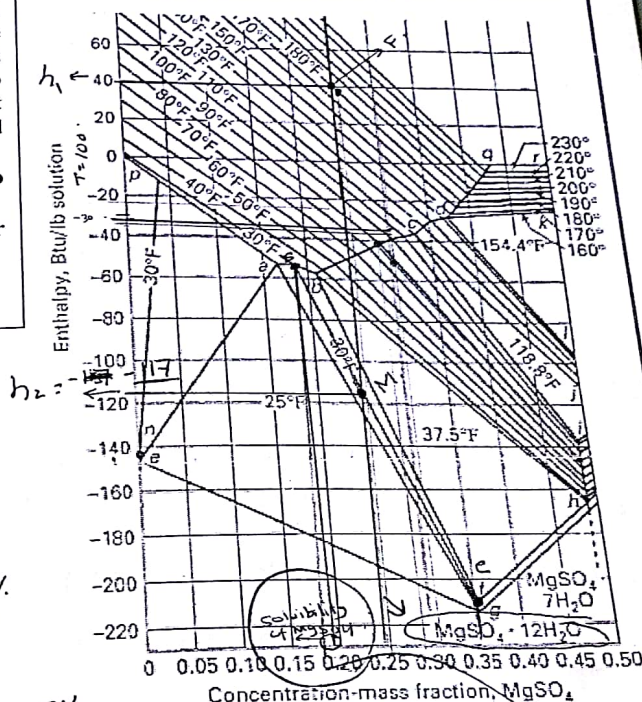
Student No.: ~~XXXXXXXXXX~~

Second semester 2016/2017
Seat No.: ~~XXXXXXXXXX~~

March 18, 2017

MgSO₄ aqueous solution contains 33.5 lbm MgSO₄/100 lbm total water and temperature of 180 °F. This solution is fed to cold crystallizer at rate of 1000 lbm/h in order to produce crystals. The crystallizer operates at 30 °F. Assume that no water is vaporized from crystallizer.

- Which type of hydrated crystals is going to be produced at these conditions?
- Estimate the solubility of MgSO₄ in water at 30 °F.
- Calculate the yield of crystals.
- Estimate the required cooling rate.



$F = 1000 \text{ lbm/h}$
 0.25 MgSO_4
 $0.75 \text{ H}_2\text{O}$
 $T = 180^\circ\text{F}$

30°F

$S =$
 $\text{MgSO}_4 = 19\%$
 $\text{H}_2\text{O} = 81\%$

C
 $\text{MgSO}_4 = 35.7\%$
 $= \frac{\text{Mwt MgSO}_4}{\text{Mwt MgSO}_4 + 12}$
 $= \frac{120}{120 + 12 \times 18}$

crystal hydrate type
 $\text{MgSO}_4 \cdot 12 \text{ H}_2\text{O}$

$X = 0.19 \text{ lbm MgSO}_4$

$\text{solubility} = \frac{0.19 \text{ lbm}}{0.81 \text{ lbm H}_2\text{O}} \times 100 = 23.4\%$

$M = F = 1000 \text{ lbm/h}$

by Lever Rule.

$$\frac{S}{Sc} = \frac{C}{M}$$

$$\frac{2.5}{6.5} = \frac{C}{1000}$$

$C = 384.6 \text{ lbm/h}$

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$\text{solubility} = \frac{0.19 \text{ lbm MgSO}_4}{100 \text{ lbm total water}}$

yield = Amount of crystal = 384.6 lbm/h

d)

$$q = h_2 M - F \times h_1$$

$$q = -117 \times 1000 - 1000 \times 40$$

$$q = -157 \times 10^3 \text{ Btu/lbm solution}$$



Heat and Mass Transfer Operations

First semester 2016/2017

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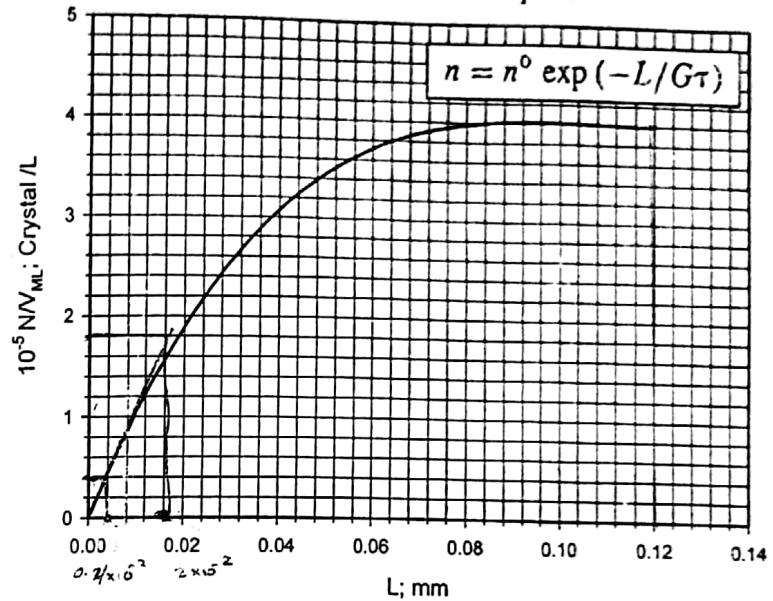
Student No. _____

Seat No.: 19

Quiz #4

December 6, 2016

Screen analysis (Tyler Standard Screen Scale) for crystal samples of certain salt resulted in the curve shown below with crystal growth rate of 0.15 mm/h. The crystallizer has a residence time of 2 h. Find the nucleation rate B^0 and the total number of crystals, N_T , per unit volume of mother liquor:



$$B^0 = n^0 G^0$$

$$n^0 = \text{slope} = \frac{\Delta(NV_mL)}{\Delta L}$$

$$= \frac{(1.8 \times 10^5 - 0.4 \times 10^5)}{0.02 - 0.004}$$

$$n^0 = 8.75 \times 10^4 \text{ Crystal mm}^{-1} \text{ h}^{-1}$$

$$B^0 = 8.75 \times 10^4 \times 0.15$$

$$B^0 = 1.31 \times 10^6 \text{ Crystal L}^{-1} \text{ h}^{-1}$$

$$n = n^0 \exp\left(-\frac{L}{G\tau}\right)$$

$$= 8.75 \times 10^4 \times \exp\left(-\frac{0.12}{0.15 \times 2}\right)$$

$$n = 5.8 \times 10^4 \text{ Crystal L}^{-1} \text{ h}^{-1}$$

$$B^0 = n^0 G^0$$

$$B^0 = n^0 G^0$$

$$n^0 = \text{slope} = \frac{(2 - 0.4) \times 10^5}{0.02 - 0.004 \times 10^{-2}} = 1 \times 10^7$$

$$B^0 = 1 \times 10^7 \times 0.15 = 1.5 \times 10^6 \text{ C/L.h}$$

$$n = 1 \times 10^7 \exp\left(-\frac{0.12}{0.15 \times 2}\right)$$

$$n = 7 \times 10^6 \text{ Cr.}$$

$$N_T = \int_0^L n \, dL$$

$$N_T = \int_0^L n \, dL$$



$$= \int_0^L n \, dL = n \Delta L$$

$$= 6.7 \times 10^6 (0.12)$$

$$N_T = 8.04 \times 10^5 \text{ Crystals}$$



Heat and Mass Transfer Operations

First semester 2017/2018

Student name: [redacted] Student No.: [redacted]

Seat No.: 34

Quiz #4

December 3, 2017

Use the following moment equation to find the cumulative and differential crystal distribution equations (on length basis) for constant growth rate:

$$x_k = \frac{\int_0^z n z^k dz}{\int_0^\infty n z^k dz} \quad k=1$$

$$x_k = \frac{\int_0^z n z^k dz}{\int_0^\infty n z^k dz}$$

Cumulative

(length)

Cumulative

$k=1$

$$x_1 = 1 - (1+z)e^{-z}$$

differential

$$\frac{dx_1}{dz} = ze^{-z}$$



Heat and Mass Transfer Operations

First semester 2016/2017

Student name: [REDACTED]

Student No.: [REDACTED]

Seat No.: 25

December 6, 2016

Quiz #4

Screen analysis (Tyler Standard Screen Scale) for crystal samples of certain salt resulted in the curve shown below with crystal growth rate of 0.15 mm/h. The crystallizer has a residence time of 2 h. Find the nucleation rate B^0 and the total number of crystals, N_T , per unit volume of mother liquor: τ .

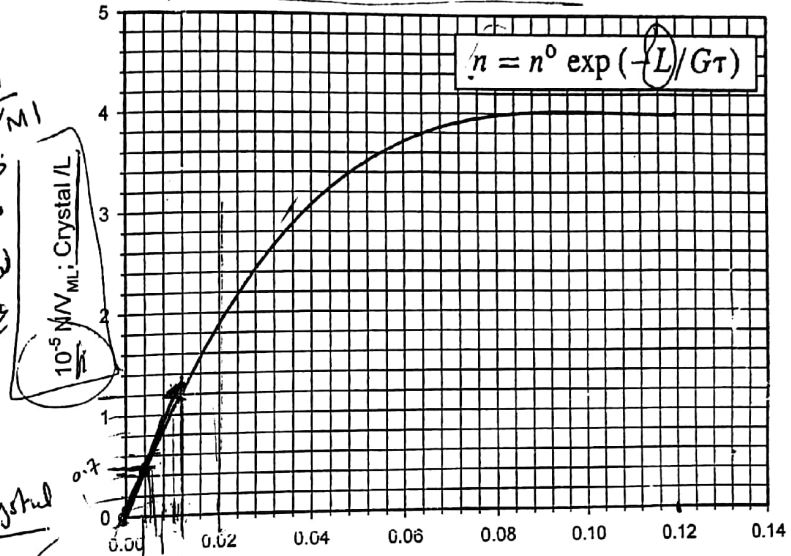
$G = 0.15 \text{ mm/h}$

$\tau = 2 \text{ h}$

$B^0 = G \cdot n^0$

$n^0 = \text{slope at } L=0$

$B^0 = 0.15 \frac{\text{mm}}{\text{h}} \times 1 \times 10^{+3} \frac{\text{crystal}}{\text{L} \cdot \text{mm}}$
 $= 1.5 \times 10^{+5} \frac{\text{crystal}}{\text{L} \cdot \text{h}}$



Slope = $\frac{0.5 - 1}{5 \times 10^{-3} - 0.01} = 100 \times 10^{+5} \frac{\text{crystal}}{\text{L} \cdot \text{mm}}$
 $B^0 = G n^0$

$N_T = \int_0^{\infty} n^0 \exp(-L/G\tau) dL$

$\frac{n^0 e^{-L/G\tau}}{-1/G\tau} \Big|_0^{\infty} = \frac{1 \times 10^{-3} \times e^{-0.12/2 \times 0.15}}{-1/(0.15 \times 2)} + n^0 e^{-L/G\tau}$

$N_T = 989.04 \times 10^3 \frac{\text{crystal}}{\text{L}}$



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Second semester 2015/2016

Heat and Mass Transfer Operations

Student name:

Student No.:

Serial No.: 52

April 20, 2015

Quiz #4

- a) If a crystal growth of some salt is $G=0.15$ mm/h, use the experimental curve below to approximate the nucleation rate B^0 :

$$\lim_{L \rightarrow 0} \frac{1}{V_m L} \frac{dN}{dt} = B^0$$

$$B^0 = G \cdot n^0$$

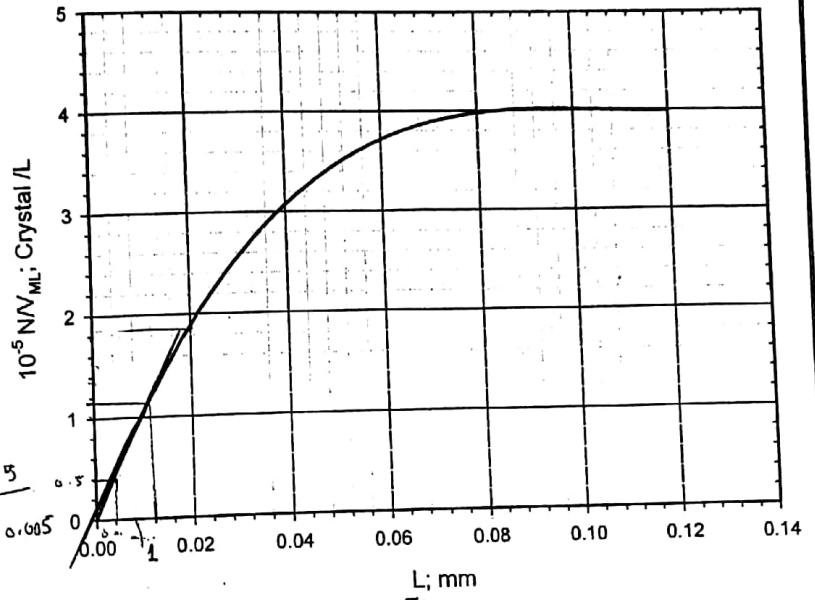
$$n = n^0 \exp(-L/G)$$

$$1.8 \times 10^{-5} = n^0 \exp(-0.02/0.15)$$

$$\text{slope}_1 = n^0$$

$$\text{slope}_2 = n^0 \quad n^0 = \text{slope}_2 = \frac{1.1 - 0.5}{0.012 - 0.005}$$

$$B^0 = G \cdot n^0$$



- b) For two-step theory, use diffusion and reaction rate equations to derive the following crystal growth overall coefficient:

$$\frac{1}{K_c} = \frac{1}{k_c} + \frac{1}{k_i}$$

Mention two significant parameters that affect such coefficient.

Diffusion-reaction Rate

- ① mass transfer of solute from bulk of solution to the crystall solution

$$\frac{dm}{dt} = K_c A (C - C_i)$$

- ② pseudo First order rxn occurs the crystal-solution interface

$$\frac{dm}{dt} = k_i A (C_i - C_s)$$

K_c depends velocity of the solution
determine degree of agglomeration (R_x)

$$\frac{dm}{dt} = \frac{A(C - C_i)}{1/K_c + 1/K_i}$$

At low velocity $\rightarrow$ the growth rate controlled by mass transfer step

Overall Coeff (K_c) $\frac{dm}{dt} = K_c A (C - C_s)$

$$\frac{1}{K_c} = \frac{1}{K_c} + \frac{1}{K_i}$$

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Heat and Mass Transfer Operations

Student name: [REDACTED]

Student No.: [REDACTED]

Second semester 2016/2017

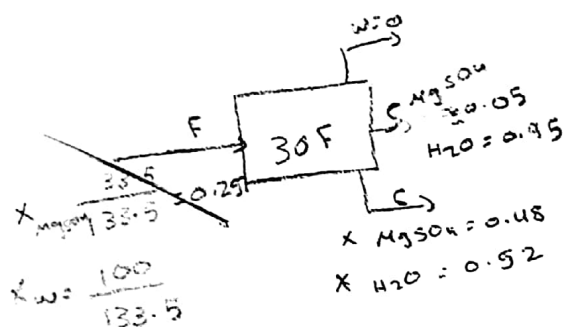
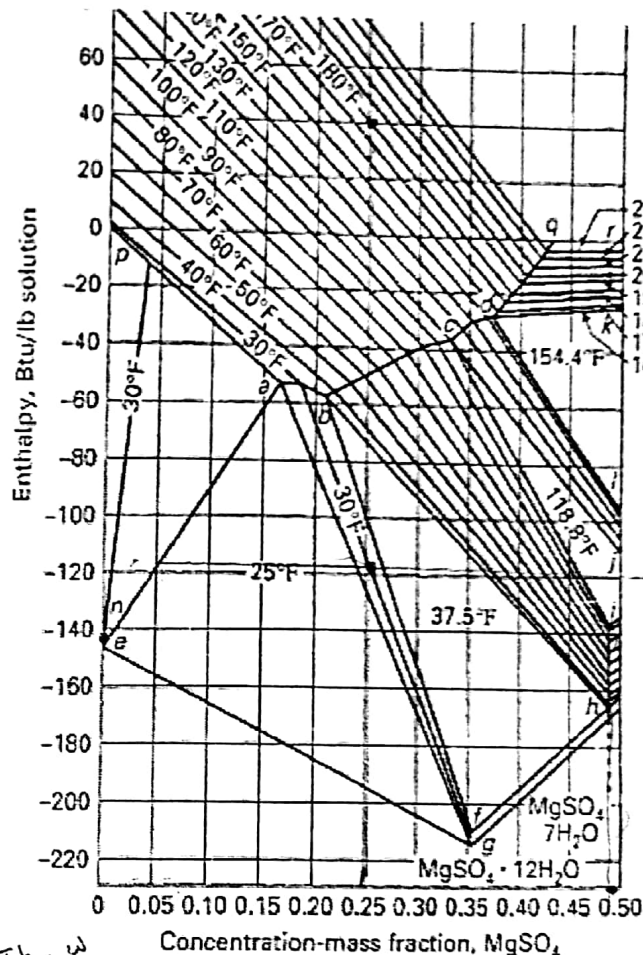
Seat No.: 8

Quiz #4

March 18, 2017

$MgSO_4$ aqueous solution contains 33.5 lbm $MgSO_4$ /100 lbm total water and temperature of 180 °F. This solution is fed to cold crystallizer at rate of 1000 lbm/h in order to produce crystals. The crystallizer operates at 30 °F. Assume that no water is vaporized from crystallizer.

- Which type of hydrated crystals is going to be produced at these conditions?
- Estimate the solubility of $MgSO_4$ in water at 30 °F.
- Calculate the yield of crystals.
- Estimate the required cooling rate.



a) $MgSO_4 \cdot 7H_2O$

b) Solubility = 0.05 $\Rightarrow$ Assume 100 lbm w
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Solubility = 0.05 $\Rightarrow$ Assume 100 lbm w

c) $0 = 0.95S + 0.52C$

$1000 = S + C \Rightarrow C = 1000 - S$

$0 = 0.95S + 0.52(1000 - S)$

$S = 353.74 \text{ lbm}$

$C = 646.26 \text{ lbm}$



Heat and Mass Transfer Operations

Second summer semester 2016/2017

Student name: [REDACTED]

Student No.: [REDACTED]

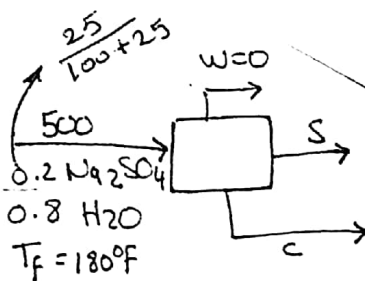
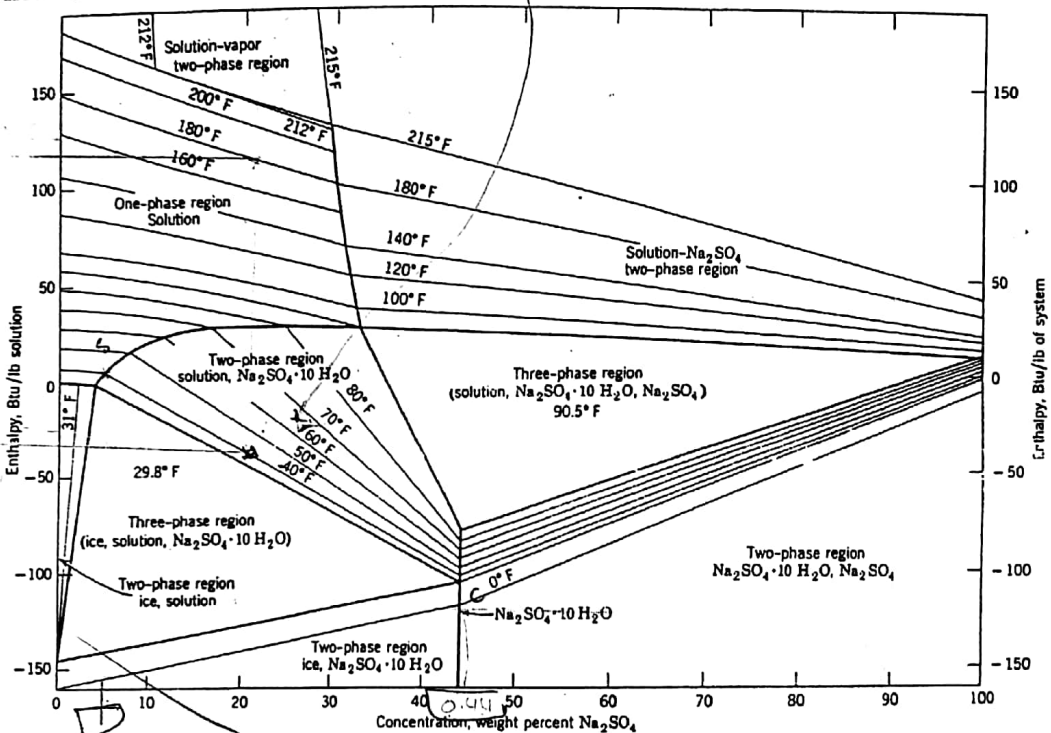
Seat No.: 15

Quiz #4

August, 22, 2017

A 500 lbm/h aqueous solution of Na_2SO_4 (25 kg Na_2SO_4 /100 kg H_2O) at 180 °F is fed continuously to a crystallizer in which the equilibrium temperature is 40 °F. Neglect the amount of water evaporated.

- Are the resulted crystals anhydrous or hydrated? Why? If they are hydrated which type of hydrated crystal will be produced? Hydrated $\text{Na}_2\text{SO}_4 \cdot 10\text{H}_2\text{O}$
- Find the solubility of solution inside the crystallizer.
- Calculate the yield of crystals using lever rule.
- Calculate the net heat added/removed from crystallizer. ?



* 40°F

$$F = S + C$$

$$F = H_1$$

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solubility of the solution:

$$\bar{S}C = 5.9 \text{ cm}$$

$$\bar{S}F = 2.4 \text{ cm}$$

$$\frac{C}{F} = \frac{S F}{S C F}$$

$$C = (F) \left(\frac{S F}{S C} \right)$$

$$C = (500) \left(\frac{2.4}{5.9} \right)$$

$$C = 203.38$$

$$S = 296.61$$

$$q = -Fh_1 + Mh_2$$

$$q = -(500)(110) + 500(-37.5)$$

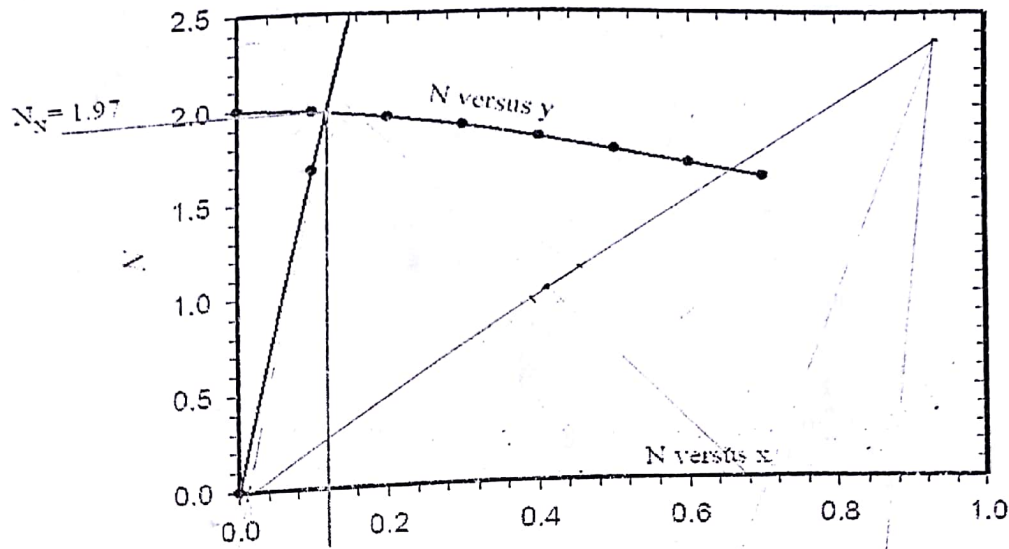
$$q = -78750$$

solubility of the solution:-

$$\frac{0.05}{0.05 + 0.44}$$

$$\frac{0.05}{0.05 + 0.44} = 0.1020$$

$$= 0.1020 \text{ kg Na}_2\text{SO}_4 \text{ / kg solution}$$



$$L_N = 1206$$

$$N = \frac{\frac{\mu_{inert}}{\mu_g}}{\frac{y_a \mu_{g oil}}{\mu_{g solut}}}$$

$$N_N = \frac{\mu_{g solut}}{\mu_{g solut}} = \frac{\mu_{g sol}}{\mu_{g solut}} y_N$$

$$\frac{\mu_{g sol}}{\mu_{g solut}} y_N$$

$$\frac{\mu_{g sol}}{\mu_{g sol}} = y_N$$

$$N_N = \frac{2000}{178} y_N$$

$$N_N = 16.67 y_N$$