



Madarju.com



Thermodynamics 2

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(eq) equilibrium : شرط واحد في جميع أجزاء النظام لا يوجد فرق في

- Thermal equilibrium: The Temp equal at every part of the system
- Mechanical eq → ضغط متساوي

Pressure equal at every part of the system

$$P_{\text{room}} = \left(\frac{3 \times 1 \times 10}{2 \times 9} \right) \text{ Pa} = 30 \text{ Pa} \text{ و } 0.9 \text{ bar} = 90000 \text{ Pa}$$

لو بنينا زغرة = لا يوجد eq (لا يوجد مقاومة) للزغرة لا يوجد فرق كبير

chemical or material equilibrium :

heat
work
mass } → sys ← تغير الحالة

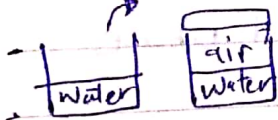
Gibbs energy for pure component, or, fugacity for mixture for each component for each phase equal

fugacity

⊗ how much the component in specific phase (مركبة) in that phase !!

مثال: خليط (ماء + هواء) في كاسة فتحتناها للهواء ، ماذا يحدث ؟

هواء ال fugacity مع ماء = هواء في خليط



ال air يقل fugacity

فإن component تبقي مركبة ، لا مركبة في phase معين

If there is a chemical eq., fugacity for each component must be equal for each phase
What does that mean?

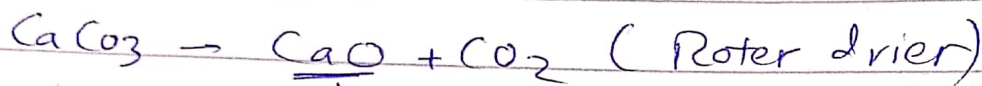
النوع ال eq :

① Phase eq (more than Phase) → physical eq.

② Chemical eq → Rxn

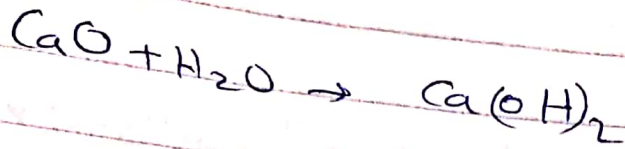
Cancellation Rxn → $\text{CaCO}_3 \rightarrow \text{CaO} + \text{CO}_2$

Calcium Carbonate

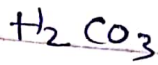
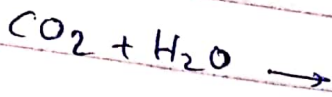


↓
البيكار
↓
البيكار





اُکس + طار ← طبر وکس
سب (طفر)
(اکسیر (طفر)



طعم لخص فی سب → کاربونیک اسید



No:

Date: 11 Feb 2020

MM SCFD
M SCFD

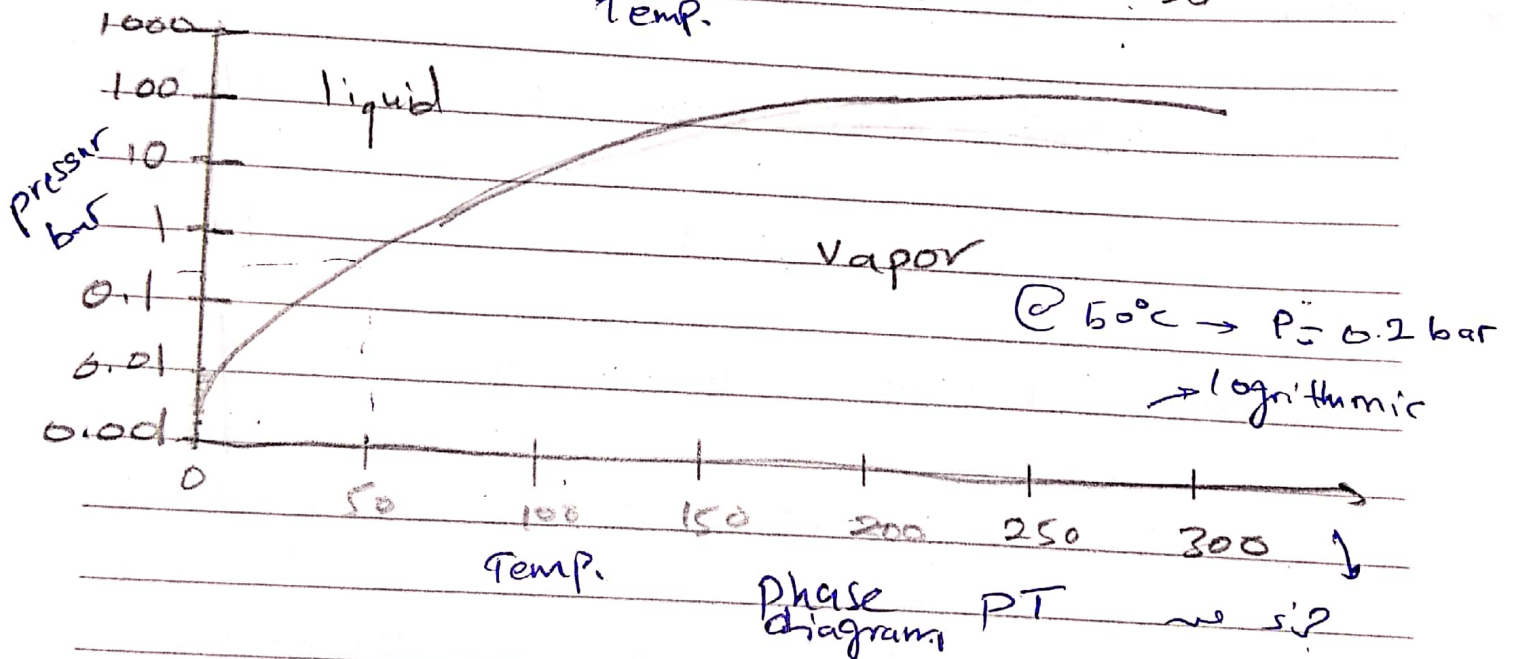
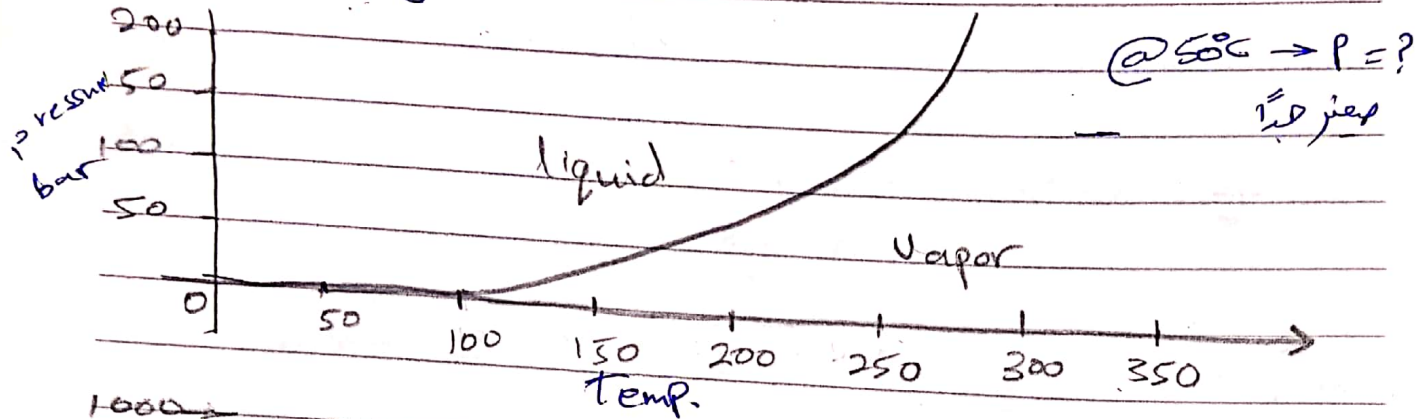
standard cubic feet per day

1000,000
1000

decatherm

وحدة الطاقة

Phase diagram



logarithmic unit = logarithmic scale

we use log-log scale ← Rang wide

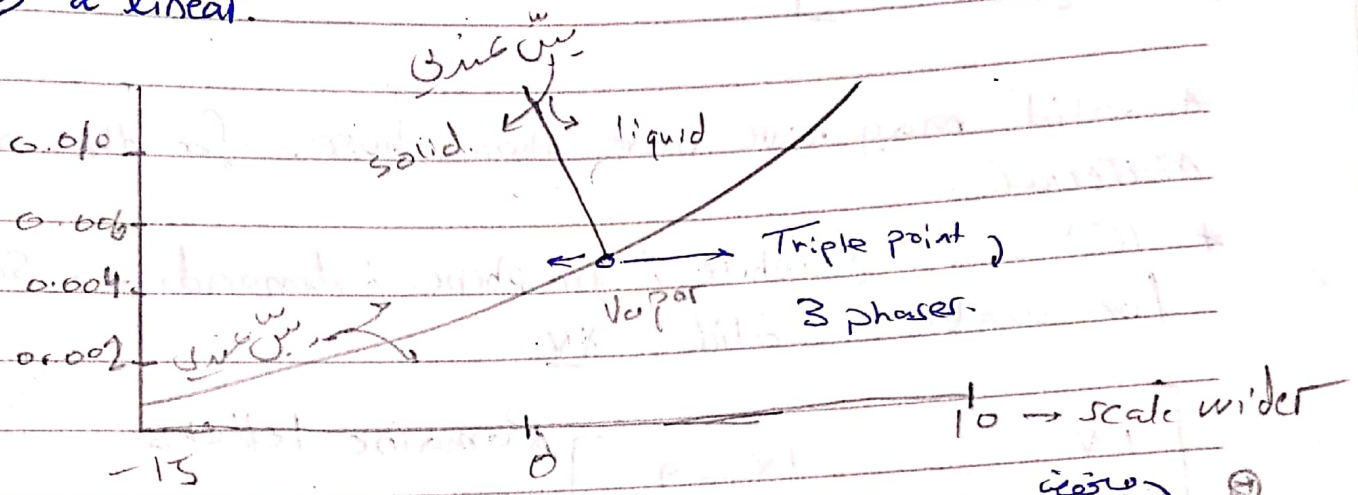
نقطة، القيمة log-log scale
cycles = logarithmic scale

digits

ask : believe & recieve

in log-scale → $\log$ scale is easier to use

✓ $\log$ → $\log 10 = 1$ → take it as interpolation don't take it as a linear.



Solid → Vapor = sublimation
 Vapor → Solid = deposition

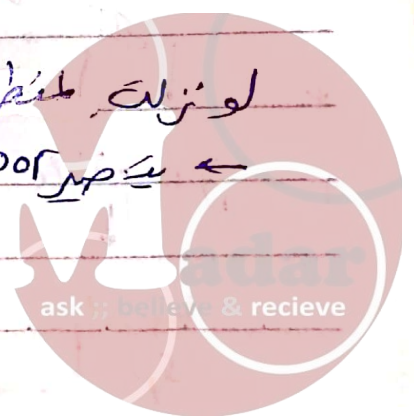
* Vapor - liquid - solid (coexistence) @ Triple Point

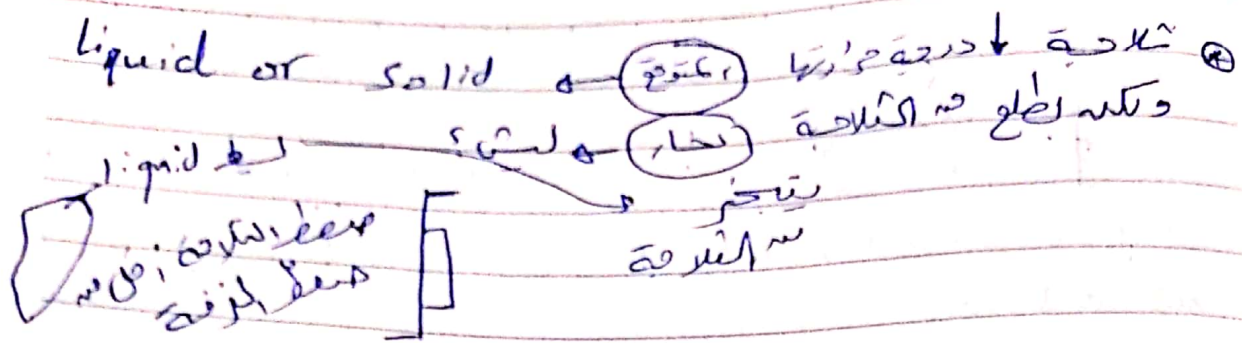
Vapor at low pressure or Temp low.
 @ lower Temp doesn't mean there are just liquid and solid

* Temp ↓ & P ↓ → There is vapor phase

cloud is what is phase?
 liquid + vapor

cloud is what is phase?
 liquid + vapor





* solid may have more than phase for the same material

* (C) → graphite / graphene / diamond. → Solid
 for water Solid XV

Romaine letters	
I V	IX → 9
V → 5	X → 10
VI → 6	XI → 11
VII → 7	XII → 12
VIII → 8	XIII → 13

Millennium: الألفية
 أكبر حرف للعدد الروماني

ملون = (الف, ا, ب)

* Solid phases → الطور

difference between different solid phase
 → structure

* snow of wether → more liquid content

* in Ref. → more solidity → Pressure of liq.
 (liquid) فوق بقاء

* graphite diamond
 ↓ ↓
 Sheet Pyramids
 (SP) → shear // surface
 structure

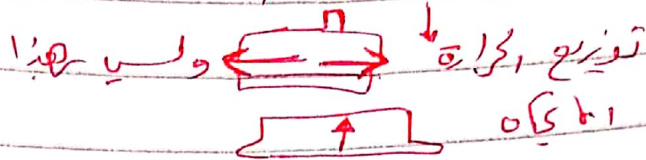
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Date:

graphite application? + Battery

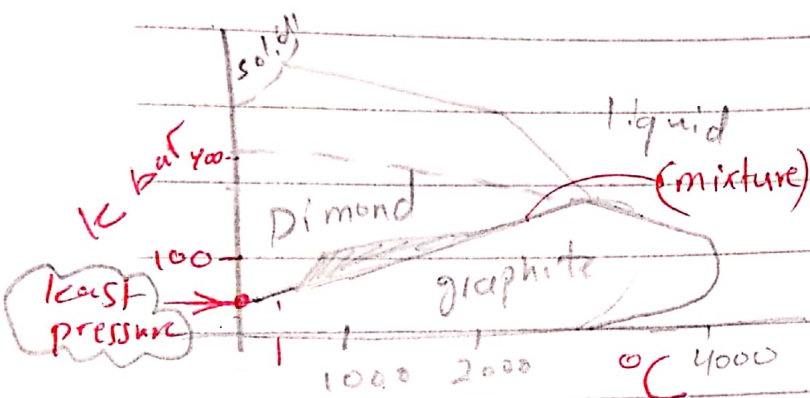
shear γ $\bar{\epsilon}$
heat $\bar{q}$ $\bar{\epsilon}$

* car breaks
+ clothes iron



+ heat exchanger $\rightarrow$ $\bar{q}$ $\bar{\epsilon}$
inert for corrosion materials.

Hf / H_2SO_4 $\bar{q}$ $\bar{\epsilon}$



$\rightarrow$ (least pressure) to make
diamond from graphite?
20 Kbar

* $\bar{q}$ $\bar{\epsilon}$ $\rightarrow \frac{1}{8}$ gram $\rightarrow$ diamond



No: App. of buckyballs Date: 16th Feb. 2020

* Gibbs energy $\Delta G \rightarrow$ thermodynamic $\rightarrow$ graphite
 $\rightarrow$ graphite $\leftarrow$ diamond
Rate of conversion $\leftarrow$ kinetic $\rightarrow$ equilibrium

* انتاج الكربون:

Bucky balls $\downarrow$ Single-walled CNT $\downarrow$ multiwalled CNT
buckminsterfullerene $\downarrow$ Carbon nano tube
(C_{60}) $\downarrow$ Graphene

* what is the significant about that materials?

$\rightarrow$ Cruel material, very cruel material
for example: (CNT) $\rightarrow$ fibers shape $\rightarrow$ Stronger by six times than iron.

$\rightarrow$ Very high thermal conductivity.

most common: copper

$\rightarrow$ Very high electric conductivity

The loss in our electricity in our common copper wires about 5 % in the whole world

* Why not to use?

(END)

Because these materials on development, not exist as a product ready to use

$\rightarrow$ Using as an alternative to Silicone material

The first computer $\rightarrow$ 1940 it used light bulb

Instead of resistors $\rightarrow$ 1 megahertz

→ Catalists in Rxn,

we use material of non-affected surface of catalysts.

* example of used catalysts:

Platen, gold, Pd →

not to enter rxn, but may be deactivated

→ molecular gear → and many part of things to be in molecular level

(bottom-up) → no wast of materials

→ no need to repair parts because it already had the repairing molecules

→ Minimizing the manufacturing space.

* Even though these applications have militarily, ethical and political problem:

[إعادة التركيب الجيني]

↓
Biostasis

↓
using so preci
weaponry

↓
ex: artificial flies.

top-down → as usuall with nano technology it will become (down-top.)

* elevator to moon!!!

* 11 km/sec



review Equilibrium: $\rightarrow$ ① Thermal Eq. $\rightarrow$ Temp.
 ② Mechanical eq $\rightarrow$ P.
 ③ Chemical $\rightarrow$ fugacity But as a pure component $\rightarrow$ Gibbs energy

Chemical Eq:

$\Rightarrow$ Gibbs energy:

$\Rightarrow$ From steam table:

@ 100°C for sat water $\rightarrow$ two phase

Gibbs energy for steam $\equiv$ Gibbs energy for liquid

$\Rightarrow$ Prove that:

$$G = H - TS \quad \text{in Kelvin}$$

* @ 100°C in water steam table:

$$h_g = 2676.1 \quad S_g = 7.3549 \text{ kJ/kg}\cdot\text{K} \quad T = 373\text{K}$$

$$h_L = 419.04 \quad S_L = 1.3069 \text{ kJ/kg}\cdot\text{K}$$

$$G^g = 2676.1 - 373 \times 7.3549 = -67.277 \text{ kJ/kg}$$

$$G^L = 419.04 - 373 \times 1.3069 = -68.4337 \text{ kJ/kg}$$

$$\Delta G = -68.4337 - (-67.277) \approx -1.16 \text{ (accepted)}$$

$$\rightarrow \boxed{G^g \approx G^L} \text{ Proved } \checkmark$$

And that Principle valid for (R-134) table.

$\Rightarrow$ Constraints for eq: $T_{\text{vapor}} = T_{\text{liquid}} = 100^\circ\text{C} \rightarrow$ Thermal.
 $P_{\text{vapor}} = P_{\text{liquid}} \rightarrow$ Mechanical
 $G_U = G_L \rightarrow$ what is proved

$\therefore$ The system is (eq).

No: ----- Date: 18th Feb - 2020

but superheated steam table, is eq. applied?

No, $G_v < G_L$

Gibbs energy when subcooled exist:

$$G_L < G_v$$

كيف اطلع Gibbs energy ل Two Phases حتى على ظروف غير موجودة فيه

phase @ Temp. higher than 100°C → superheated steam



100°C @ the same pressure

estimate [Gibbs energy]

110°C
120°C
140°C
⋮

at the same P



* Plot @ the same P for Gibbs energy

phase @ Temp. lower than 100°C → subcooled liquid

estimate Gibbs energy

* Plot @ The same (P) @ The same graph

90°C
80°C
⋮

intercept: equilibrium

extrapolation for liquid → @ high Temp. Gibbs energy for

liquid > Gibbs energy for vapor

extrapolation for vapor → phase stable = liquid

* Gibbs energy continuous fn:

no Discontinuity

→ specific volume → fn Discont.

→ specific enthalpy → " "

→ specific internal energy → fn Discont.

→ S → fn " "

⇒ from discontinuous fn you can find Cont fn
Gibbs fn

No:

Date: 18th - feb $\Rightarrow (C_p) (C_v) :$

$$\downarrow$$

$$\frac{\partial H}{\partial T} / P$$

its Derivative discont. $\therefore$ Discont. fn. C_p for vapor $\neq$ C_p for liquid

① liquid $\rightarrow$ vapour $\rightarrow$ [first order first transition]
 vapor $\rightarrow$ liquid $\rightarrow$ [Twist]
 solid $\rightarrow$ liquid $\rightarrow$ The single cont. fn. $\equiv$ Gibbs energy fn.

② Second order first transition

In solids $\rightarrow$ how diamond transitions to graphite and vice versa $\rightarrow$ There is a continuity fn.

③ $\rightarrow$ Table: (ice water - vapor) phase:@ -12°C : $\rightarrow$ ice $\rightarrow$ (safe side)

$$g^v = h^v - T s^v = 2478.4 - (261.15)(9.549) = \boxed{-15.32 \frac{\text{kJ}}{\text{kg}}}$$

$$g^s = h^s - T s^s = -358.17 - (261.15)(\boxed{-1.3130}) = \boxed{-15.28 \frac{\text{kJ}}{\text{kg}}}$$

minus! because of reference

Point: That the ref. point = 0.01 Triple point

NOTE :-

 $g_{\text{phase 1}} = g_{\text{phase 2}} \rightarrow$ Pure component* multi component system $\rightarrow$ fugacity $(-15.32 - -15.28) \neq 0$ (Not exactly 0! Why?)

* steam tables have percentage of error in comparison with experimental data; so range of accepted error

$$\pm 1 \frac{\text{kJ}}{\text{kg}}$$

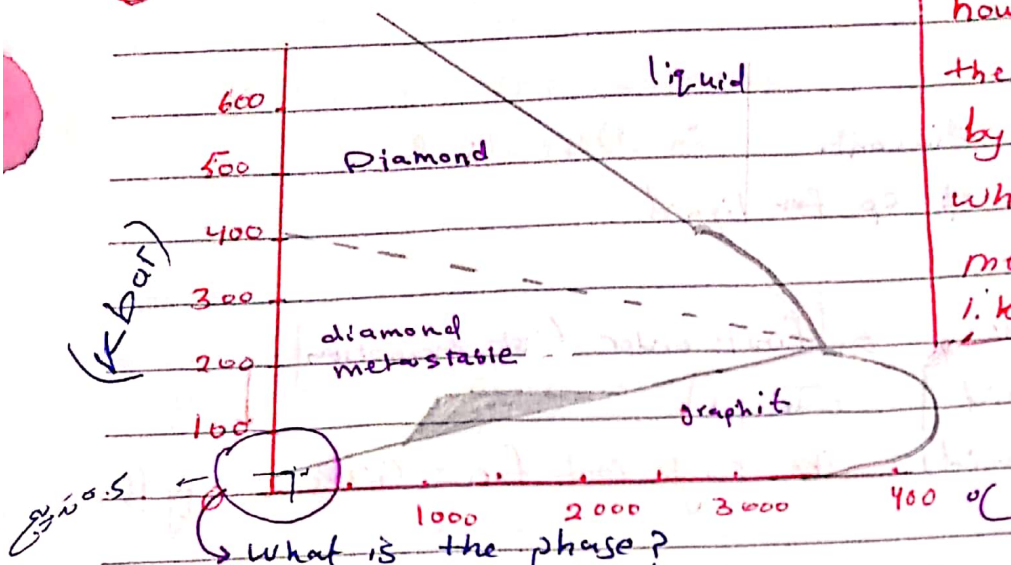
$$16.32 \quad -15.32 \quad -14.32$$

اي فقهه صفن لغري هادر لا تقوى عن -15.32

No: _____

Date: 18th Feb - 2020

④ Phase diagram of Carbon Idea!



how to express the transition curve by quantities, which can be measured experimentally like $P, V, h \dots$ etc.

what is the phase?
graphite or diamond or mixture
↳ saturation curve → 2 phase

$$\text{So; } g^{\text{graphite}} = g^{\text{diamond}} \rightarrow h^g - TS^g = h^d - TS^d$$

$$(h^g - h^d) = T(S^g - S^d)$$

we can estimate experimentally by DSC;

← Δh transition

* we face a problem, because we can't estimate experimentally!

(entropy) $\rightarrow$ ΔS (gibbs Energy) ΔG

$$\Delta G = -P \Delta V$$

g fcn of T and P

$$dg = \left(\frac{\partial g}{\partial T} \right)_P dT + \left(\frac{\partial g}{\partial P} \right)_T dP$$

from maxwell relations

two variable → moles change



$$\partial g = v dp - s dT \quad (7)$$

$$\left(\frac{\partial g}{\partial p}\right)_T = v \quad ; \quad \left(\frac{\partial g}{\partial T}\right)_p = -s$$

$$\left(\frac{\partial f}{\partial x}\right)_f = 0$$

[Clausius Clapeyron] الفكرة: العلاقة بين الضغط ودرجة الحرارة

$$\ln \left(\frac{P_1}{P_2}\right) = -\frac{\Delta H_{vap}}{R} \left(\frac{1}{T_2} - \frac{1}{T_1}\right) \rightarrow \text{Vapor pressure} \uparrow p$$

* Qualitative Q: ~~at~~ which circumstances can we convert the graphite to diamond?

from phase diagram; at normal Temp. and at about 20,000 bar, but if there is no phase diagram

⇒ specific volume for graphite, specific volume for diamond ⇒ v

⇒ $\Delta h \checkmark$ (diamond and graphite)

→ experimental

or

→ calculated from previous equations

* Back to phase diagram of water:

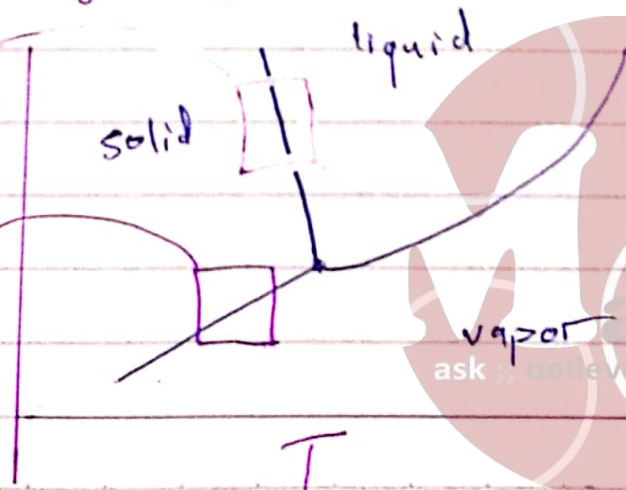
→ life application: P

Ice skating boots

* ΔV (solid, vapor)

Δh

أو بين أي متغيرين للحرارة



No:-----

Date:-----

$$h_v > h_L$$

$$V_L$$

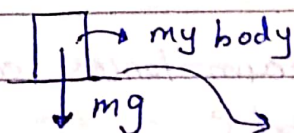
so $\Delta v (-)$

$$P_S < P_L \rightarrow \text{Just for water}$$

* sky skating $\rightarrow$ knife looklike ?? why ??

$$\uparrow \text{ pressure} = \frac{\text{Force}}{\text{Area} \downarrow} \quad \text{so; under high } P, \text{ the}$$

ice under ice skating boot's knife turns to liquid
so the friction becomes less $\rightarrow$ It's looklike water
skating



$$P = \frac{mg}{\text{Area}}$$

$\rightarrow$ Area of normal boot $>$ Area of knife

$\uparrow P$ (ice of water) turn to liquid, whereas
other material $\uparrow P$ (ice of other material $\rightarrow$ they
become more ice) and $\uparrow P \uparrow S$

* space equipment $\rightarrow$ space boot has big area.
 $\uparrow P \rightarrow$ the movement will be harder



$$\Delta S_{vap} = \frac{\Delta H_{vap}}{T} \quad \text{--- } \textcircled{*} \textcircled{*}$$

$$du = T ds - P dv \quad \text{--- } \textcircled{*} \rightarrow \text{Energy balance for closed system}$$

$$d(Pv) = P dv + v dp$$

$$d(Ts) = T ds + s dT$$

$$g = (u + Pv) - Ts$$

$$dg = d((u + Pv) - Ts) = \boxed{du} + P dv + v dp - T ds - s dT = dg$$

↓
substitute with $\textcircled{*}$

$$\cancel{T ds} - \cancel{P dv} + P dv + v dp - \cancel{T ds} - s dT = dg$$

$$\therefore v dp - s dT = dg$$

at equilibrium: $dg_v = dg_L$

$$dg_v = v^v dp - s^v dT$$

$$dg_L = v^L dp - s^L dT \quad \text{--- } \textcircled{-}$$

$$0 = \underbrace{(v^v - v^L)}_{\Delta V} dp - \underbrace{(s^v - s^L)}_{\Delta S} dT$$

$$\frac{dp}{dT} = \frac{\Delta S}{\Delta V} \rightarrow \text{substitute --- } \textcircled{*} \textcircled{*}$$

$$\frac{dp}{dT} = \frac{\Delta H}{T \Delta V} \rightarrow \begin{array}{l} H^v > H_L \rightarrow \textcircled{+} \\ V^v > V^L \rightarrow \textcircled{+} \end{array}$$

in Kelvin always $\textcircled{+}$

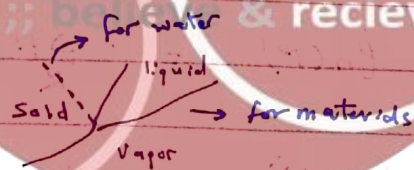
In (Solid - liquid) eq:

$$\Delta H_{\text{melting}} \textcircled{+} \quad H_L > H_S$$

$$\Delta V \textcircled{+} \quad \text{But for water}$$

$$\Delta V \textcircled{-} \rightarrow \rho_L > \rho_S, \quad \hat{v}_S > \hat{v}_L$$

ask :: for water & receive



Derivation

No: Clausius
Clapeyron

Date: 23th Feb

(solid)
(liquid)

* melting slope for water $\ominus$

$$\frac{\Delta S}{\Delta V} \rightarrow \text{clapeyron eq.}$$

Classify. at eq of (solid - Vapor) (liquid - vapor)

$$\frac{dP}{dT} = \frac{\Delta H}{T \Delta V} \approx \frac{\Delta H}{T V^v} \rightarrow \text{substitute with ideal gas law!!}$$

* because $\hat{V}_L$ very small
in compression with steam

$$V = \frac{RT}{P}$$

$$\frac{dP}{dT} = \frac{\Delta H}{T \frac{RT}{P}} = \frac{\Delta H}{T^2 R} P$$

$$\frac{dP}{P} = \frac{\Delta H}{T^2 R} dT$$

$$\frac{dx}{x} = d(\ln x)$$

$$d \ln(P) = \frac{\Delta H}{T^2 R} dT \quad [\text{clausius clapeyron eq.}]$$

constant

$(\Delta H) \rightarrow$ fcn of Temp.?

* assumes narrow Temp. range
so $\Delta H \approx$ constant so
our integration w.r.t T

$$\int d \ln(P) = \int \frac{\Delta H}{R} \frac{1}{T^2} dT$$

$$\ln(P) = -\frac{\Delta H}{R} \frac{1}{T} + C \quad \text{OR} \quad \text{because } (V_s \approx V_L)$$

$$\ln(P) = -\frac{\Delta H}{R} \left(\frac{1}{T_2} - \frac{1}{T_1} \right) + C$$

↓ assumption
Vapor $\equiv$ ideal gas
 $\hat{V}_v \gg \hat{V}_L$ or $\hat{V}_s$

* you can apply this eq
(V-s) eq (L-v) eq

* you can't apply for

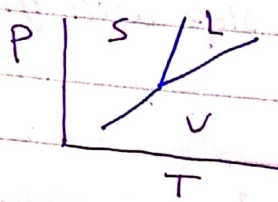
(s-L) eq

ask : believe & receive

No: Clausius
Clapeyron

Date: 23 - Feb - 2020

* we can apply this equation experimentally (P vapor pressure) and (Temp.)



→ then we can find $(\Delta H_{vap}) \rightarrow \Delta S??$

$$T \frac{\Delta S}{T} = \frac{\Delta H}{T}$$

$$\Delta S_{vap} = \frac{\Delta H}{T}$$

* Using this equation enables us to know the phase of material.

#

Q: Trimethyl gallium, $Ga(CH_3)_3$, can be used as a feed gas to grow films of $GaAs$. Estimate the enthalpy of vaporization of $Ga(CH_3)_3$ from the data of saturation pressure vs. Temperature given in the table.

T(K)	p^{sat} [kPa] →	$\ln p^{sat}$	$\frac{1}{T}$
250	2.04	0.7	0.004
260	3.3	1.2	0.0038
270	7.15	2	0.0037
280	12.37	2.5	0.0035
290	20.45	3.0	0.0034
300	32.48	3.5	0.0033
310	49.75	4.0	0.0032

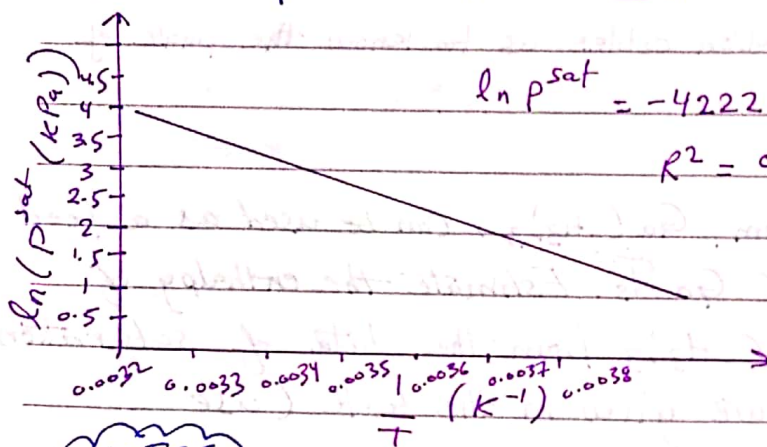
From Clausius - Clapeyron equation

$$\ln p^{sat} = \text{const} - \frac{\Delta h_{vap}}{RT}$$

* If we plot $\ln p^{\text{sat}}$ vs T^{-1} the slop will give $-(\Delta h_{\text{vap}} / R)$.

$$\frac{-\Delta h_{\text{vap}}}{R} = -4222.1 \text{ [K]}$$

$\rightarrow \Delta h_{\text{vap}} = 35.1 \text{ [kJ/mol]}$ constant. Its unit depends on R's unite



NOTES

* How to control P in lab? by weights

* If (ΔH) in $[\text{kJ/kg}]$

$\rightarrow$ conversion $\rightarrow$ molecular weight for common elements

Q: estimate ΔS in that range?!

$$\Delta S = \frac{\Delta H}{T}$$

$T \rightarrow$ at which T??

$$T(\text{K}) \approx 280 \text{ K}$$

$$\Delta S \approx \frac{35.1 \times 10^3 \text{ J/mol}}{280} = 125.38 \text{ J/mol K}$$

Q: the equation given and find: ΔH , or phase diagram

Q: ΔH is given Find: Vapor p or Temp.

* constraints to apply first and second law of thermodynamics?

assumptions: ① neglect electrical, nuclear, magnetic, Surface Tension } ideally

but when you apply 1st and 2nd law of thermodynamics on ↓
we can't neglect Surface tension (nanoparticle)

↓ size of particle ↑ Surface Tension

Henery's law and Raoult's law

25 / Feb

* Henery's law

* Raoult's law

* Limitation of Raoult's law

For a system composed of C component and p phases the following criteria must be simultaneously apply

1. Thermal equilibrium $T^{(1)} = T^{(2)} = T^{(p)}$
2. Mechanical eq. $P^{(1)} = P^{(2)} = P^{(p)}$
3. Chemical eq. $f_i^{(1)} = f_i^{(2)} = f_i^{(p)}$ $i = 1, 2, 3, \dots, C$
 $\mu_i^{(1)} = \mu_i^{(2)} = \mu_i^{(p)}$ $i = 1, 2, 3, \dots, C$
 ↓
 chemical potential = driving force

for mass transfer = concentration difference

If there is a driving force there is not eq.

for mass transfer = chemical potential main driving force

f and M for a component = G (gibbs energy)

Q: Composition of air and water at eq. at 20°C = 68°F
1.00 atm pressure.

	Gas phase	liquid phase
Mol fraction water	0.023	0.999985
Mol fraction Oxygen	0.205	5×10^{-6}
Mol fraction Nitrogen	0.772	10×10^{-6}
Sum of mol fraction	1.00	1.00

NOTE: This treats air as 21% oxygen, 79% nitrogen, ignoring its other minor species

*(Iso-fugacity condition)

$$f_{N_2}^{(air)} = f_{N_2}^{(w)} \quad f_{O_2}^{(air)} = f_{O_2}^{(w)} \quad f_{H_2O}^{(air)} = f_{H_2O}^{(w)}$$

Chemical equilibrium



NOTE: Ideal vapor phase $\rightarrow f = \text{mole fraction} \times \text{total pressure}$

$$T^{(air)} = T^{(w)} \rightarrow \text{Thermal eq}$$

$$P^{(air)} = P^{(w)} \rightarrow \text{Mechanical eq} \quad \left. \begin{array}{l} \text{Thermal eq} \\ \text{Mechanical eq} \end{array} \right\} \text{known } \checkmark$$

NOTE: we can make 3 material Balance $\rightarrow$ 3 material.

gas: $f_i^{(gas)} = y_i P$ (Ideal gas)

$y_{H_2O} P$
 $y_{O_2} P$
 $y_{N_2} P$

liquid: $\rightarrow$ (عارة مركزة سائلة) liquid phase $\rightarrow$ using Raoult's law

$\rightarrow$ (تركيز مقل من 1.000) $\rightarrow$ using Henry's law

Raoult's law

$$f_i \text{ (Liquid phase)} = x_i P_i^{\text{vap}}$$

$$\frac{y_{\text{H}_2\text{O}}}{P} P = x_{\text{H}_2\text{O}} \boxed{P_{\text{H}_2\text{O}}^{\text{vap}}} \rightarrow \text{anton eq.} \rightarrow \text{يعطى على حرارة وبتنوع}$$

NOTE: O_2 and N_2 not too soluble in water so we can't apply Raoult's law

* Sparingly soluble $\Downarrow \Downarrow \Downarrow$ قليلة ذائبة $\equiv$ Henry's law

Henry's law :

$$f_i \text{ (liquid)} = x_i \boxed{H_i} \rightarrow \text{Henry's law constant}$$

* Henry's law constant $\rightarrow$ fn of Temp., Its unit is (bar)

* Henry's law constant depend on :

① ON Temperature of component

② ON Solvent that component in

ex: $H(\text{O}_2 \text{ in } \text{H}_2\text{O}) \neq H(\text{O}_2 \text{ in acetone})$; (Solvent & solute)

$\text{H}_2\text{O} \equiv$ solvent $\text{N}_2 / \text{O}_2 \rightarrow$ solute

my equations
from Henry's
law

$$\begin{aligned} y_{\text{O}_2} P &= x_{\text{O}_2} H(\text{O}_2 - \text{H}_2\text{O}) \\ y_{\text{N}_2} P &= x_{\text{N}_2} H(\text{N}_2 - \text{H}_2\text{O}) \end{aligned}$$

$\rightarrow$ you can find
in tables

my eq. from
Raoult's law

$$y_{\text{H}_2\text{O}} P = x_{\text{H}_2\text{O}} \boxed{P_{\text{H}_2\text{O}}^{\text{vap}}} \text{ known}$$

$\Rightarrow$ 6 unknown $\rightarrow$ you have 3 eq.

Henry's law
Raoult's law

Date: 25th Feb-2020

$$\left. \begin{array}{l} \sum y_i = 1 \quad y_{O_2} + y_{H_2O} + y_{N_2} = 1 \quad \rightarrow \text{for vapor} \\ \sum x_i = 1 \quad x_{O_2} + x_{H_2O} + x_{N_2} = 1 \quad \rightarrow \text{for liquid} \end{array} \right\} \text{eq 5, 4}$$

$$\% O_2 : \% N_2 \rightarrow \frac{21}{79} \quad \text{eq 6}$$

Now you can solve the equation simultaneously
= system of linear equation

$$\begin{bmatrix} \quad \end{bmatrix} \begin{bmatrix} \quad \end{bmatrix} = \begin{bmatrix} \quad \end{bmatrix} \quad \boxed{Ax = b}$$

$$A^{-1} b = x \quad \checkmark$$

IN (AIR) (Gas phase)

Mol fraction of $O_2 \rightarrow 0.205$ $\downarrow$ (dissolving in water)

$N_2 \rightarrow 0.772$ $\downarrow$

IN WATER (LIQUID phase)

Mol fraction $\rightarrow O_2 = 5 \times 10^{-6}$ (saturation)

$N_2 = 10 \times 10^{-6}$

Solubility N_2 in water $>$ solubility O_2 in water

solubility $N_2 : O_2$ in air $\approx$

" $N_2 : O_2$ in water $\approx$

4:1 $\downarrow$?? why
2:1

$\uparrow$ soluble in water $\downarrow$ Henry's constant

ask & receive

if $\% N_2 = \% O_2$ in air $\rightarrow$ solubility of $O_2 \gg N_2$ in water !!

* Henry's law constant + vapor pressure $\rightarrow$ depending on Temp.

* H_i for gases $\uparrow$ Temp $\uparrow$ Solubility $\downarrow$
Gases

* Solubility $\propto \frac{1}{H_i}$

* $y_i P = x_i H_i$
 $\downarrow$ bar (Pressure unite) $\uparrow$ Solvent $\uparrow$ Temp.

Gas H_i (bar) for water at 25°C
 C_2H_2 1342.2 $\rightarrow$ (ethyne) mo soluble gas
 in water at 25°C

* using in welding

N_2 87365.0 $\rightarrow$ least soluble gas in water @ 25°C

Q: The highest concentration of CO_2 in water @ 25°C ??

$\uparrow$ concentration $\equiv$ solubility

$y_i P = x_i H_i \rightarrow \text{so; } x_i = \frac{y_i P}{H_i} = \frac{1 \times 1}{1651.9} \quad \begin{matrix} \text{CO}_2 \\ \text{water} \end{matrix}$

$x_i = 6 \times 10^{-4} \text{ mol CO}_2$

$\Rightarrow \frac{\text{mg}}{\text{L}} (\text{ppm}) = 6 \times 10^{-4} \frac{\text{mol CO}_2}{\text{mol sol}} \left| \frac{44 \text{ g CO}_2}{1 \text{ mol CO}_2} \right| \left| \frac{\text{mol solution}}{18 \text{ g sol}} \right|$

$\cdot$ لا يذوب في الماء CO_2 $\rightarrow$ water & sol $\rightarrow$ $\leftarrow$ to convert mg
 $= 6 \times 10^{-4} + \frac{44}{18} \times \frac{\text{g CO}_2}{\text{g sol}} = 1.48 \times 10^{-3} \frac{\text{g CO}_2}{\text{g sol}}$

(ppm) = $1.48 \times 10^{-3} \frac{\text{g CO}_2}{\text{g sol}} \left| \frac{1000 \text{ mg CO}_2}{1 \text{ g CO}_2} \right| \left| \frac{\text{g sol}}{10^{-3} \text{ L}} \right| = 1480 \text{ ppm}$
 $\downarrow$
 water $P = 1$

Is solution acidic or Basic? Acidic. $\text{CO}_2(\text{g}) + \text{H}_2\text{O}(\text{l}) \rightarrow \text{H}_2\text{CO}_3(\text{aq})$
 Carbonic acid

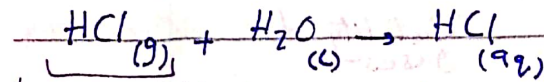
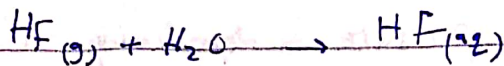
* Application on solution (gas-liquid (water))

* Most Acids are gases dissolved in water

No: _____

Date: 1st March - 2020

33:59



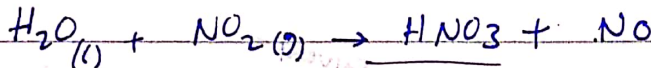
hydrogen chloride

it's not acid

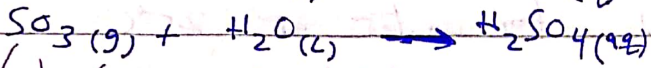
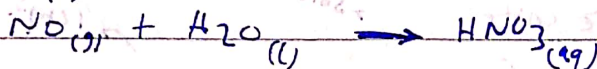
hydrochloric acid

highest concentration 36%

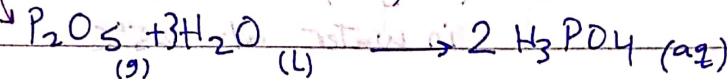
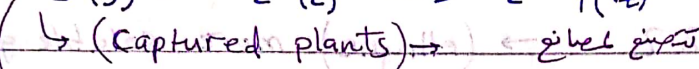
#



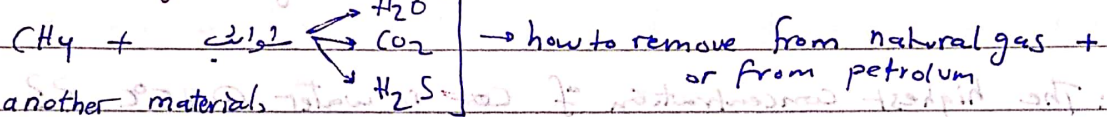
solubility 50%



solubility > 100 (drow)

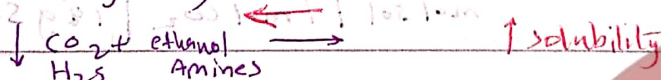


* Natural gas

* To remove CO_2 from natural gas or H_2S ?⇒ Find solvent that CO_2 has high solubility in it?

Ethanol Amines

why?? because such compounds react chemically not just dissolve physically



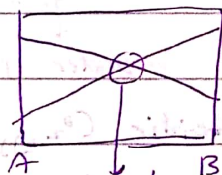
Ionic liquids

Ions without water @ 0°C It's vapor pressure = 0

It's still in its phase even with heating

Solute → vapor phase solvent → DES

or DES



eutectic point : lowest melting point of a mixture

Ions without water : electrostatic interactions → solutes removing

* solubility $\rightarrow$ Henry's law

* Raoult's law $\equiv$ gases Ideal

$$y_i P = x_i P_i^{vap}$$

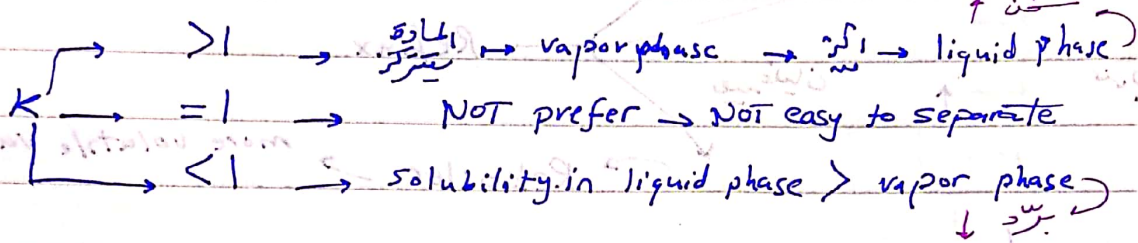
Fugacity Ideal gas or Ideal solution

distribution coeff. $\equiv$ No unite

$$k_i = \frac{y_i}{x_i} \rightarrow \text{mol fraction in vapor phase}$$

$$x_i \rightarrow \text{mol fraction in liquid or solid phase}$$

Solution $\rightarrow$ خاصية مادة ممتزجة في



* Separation: for example: distillation: most prefer

simple, available, NOT down stream processing

بسهولة عادة ما تكون مثل ما يدرج، فنتج ذائع أغل وزاد الشئ

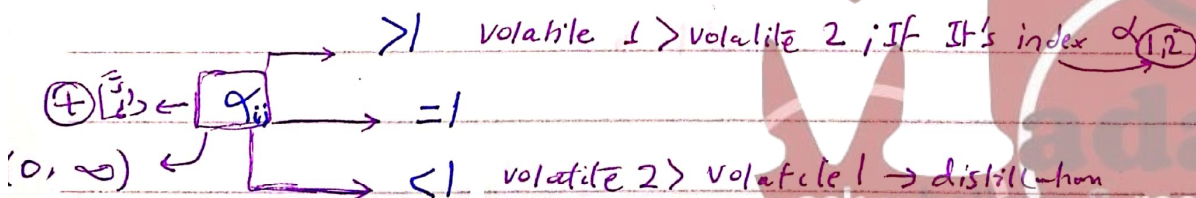
* ex: for down stream processing $\rightarrow$ فصل الكافيين من الشاي

solid $\rightarrow$ ما بقى / أغل distillation بطريقة ما شقة

* Relative volatility: $\alpha_{1,2} = \frac{k_1}{k_2} = \frac{(y_1/x_1)}{(y_2/x_2)}$

له معادلة بين مادتين

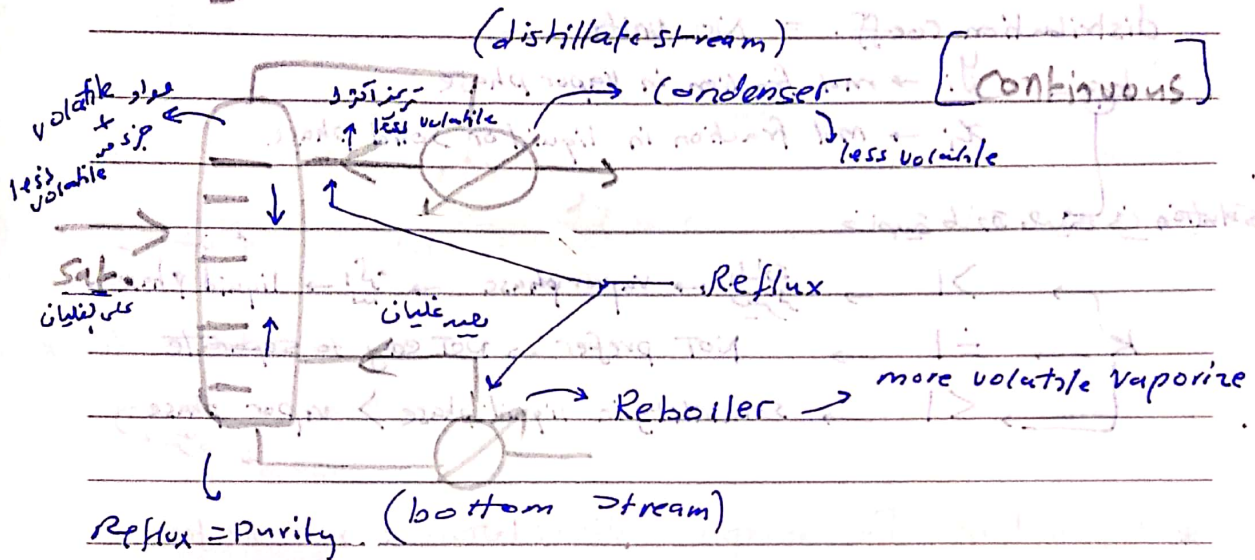
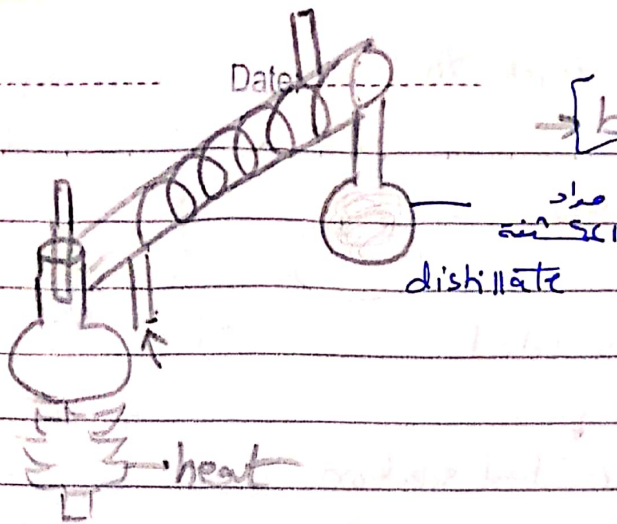
index $\rightarrow$ انتبه لا $\alpha_{2,1} = \frac{k_2}{k_1}$



vapor phase $\equiv$ distillate stream } in distillation process
liquid phase $\equiv$ bottom stream }

No:-----

Date:-----



⊗ $\alpha > 1$ $\frac{k_1}{k_2} > 1 \rightarrow k_1$ distillate stream
 $\rightarrow k_2$ bottom stream

⊗ $\alpha < 1$ $\rightarrow$ عكس

⊗ $\alpha = 1$ = impossible ; (normal distillation)

المزج فارة ثابتة

لنقل المواد

$\alpha \approx 1 \rightarrow$

ask ; believe & recieve

- * $0.95 \leq \alpha_{1,2} \leq 1.05 \rightarrow$ you can use distillation
- * $\alpha_{12} > 1 \rightarrow$ component 1 $\rightarrow$ distillate stream
- * $\alpha_{12} < 1 \rightarrow$ component 1 $\rightarrow$ bottom stream or residue
- * $\sum \text{fraction in each phase} = 1$

Note: * if there are three component $\rightarrow$ 3 α can be measured $\left. \begin{matrix} \alpha_{12} \\ \alpha_{23} \\ \alpha_{31} \end{matrix} \right\}$
one at least of them > 1 , and one at least < 1

- * $\alpha_{12} \neq \alpha_{21} \rightarrow$ It depends on what index ϕ needs.
- * Indexes α_{ϕ}

Exam:

* phase diagram $\rightarrow$ binary system $\equiv (y, x) \dots$

* pure component:

P vs T , T vs V , P vs V ... There is not a composition

* T_{xy} $\left[\begin{array}{l} T \text{ vs } x \rightarrow \text{mol. frxn} \rightarrow \text{liquid phase} \\ y \rightarrow \text{mol. frxn} \rightarrow \text{vapor phase} \end{array} \right.$
at constant P

* P_{xy} $\left[\begin{array}{l} P \text{ vs } x \\ y \end{array} \right.$
at constant T

* +ve deviation $\rightarrow$ Raoult's Law

-ve deviation $<$ Raoult's law

Raoult's law $\rightarrow$ Ideal

* Raoult's law $\rightarrow$ Vapor $\equiv$ Ideal gas mixture
liquid $\equiv$ Ideal soln.

liquid $\equiv$ Ideal soln.

Ideal soln ← system air $\rightarrow$ 50 g *
 or
 s.t. non-Ideal soln ← 3 constraints

note!

Note:
* non-Ideality in liquid phase $\gg$ vapor phase?

vapor phase has ρ much smaller, so there aren't interaction between the molecules.

Liquid phase $\rho \rightarrow$ much larger ; small distances between molecule $\rightarrow$ interaction $\rightarrow$ attraction
L $\rightarrow$ Repulsion

$\rightarrow$ Repulsion

Shap

Size

Chemical interaction
(specific interaction)

→ liquid phase → Component of liquid mixture

Sheep

Size

Specific interaction

functional group

To have Ideal solution

Size

Shape

specific interaction

Determine which is Ideal or non-Ideal of the following?

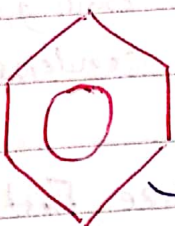
⊗ n-hexane
n-heptane
[Ideal soln]

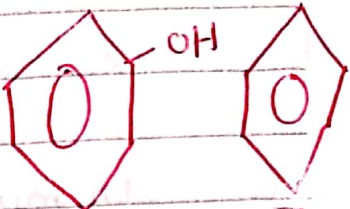
⊕ n-hexane
n-hexanol
[non-Ideal]
non polar → polar

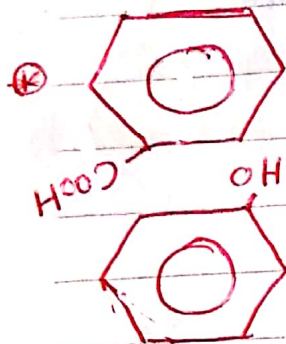
⊗ n-dodecane
n-hexanol
[non-Ideal soln.]

specific chemical interaction

⊗ n-hexane
n-dodecane
[non-Ideal (size)]

⊗  C₆H₆
Ring
n-hexyne → chain
[non-Ideal]

⊗ 
[non-Ideal]
specific chemical interaction

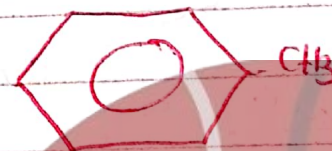


Shape, size, chemical interaction

bond → aromatic
→ triple

[non-Ideal → specific chemical]

⊗  CH₂CH₂CH₃
[non-Ideal], size



* Ideal soln. → 3 criteria applied

* $y_i P = \gamma_i x_i P_i^{vap}$
(fugacity coefficient) ↓ to express non-Ideality

gas mixt. (activity coefficient)

Ideal
= 1

non ideal
≠ 1

$\gamma_i > 1$ → + deviation

$\gamma_i < 1$ → - deviation

$\gamma_i = 1$ → Raoult's law

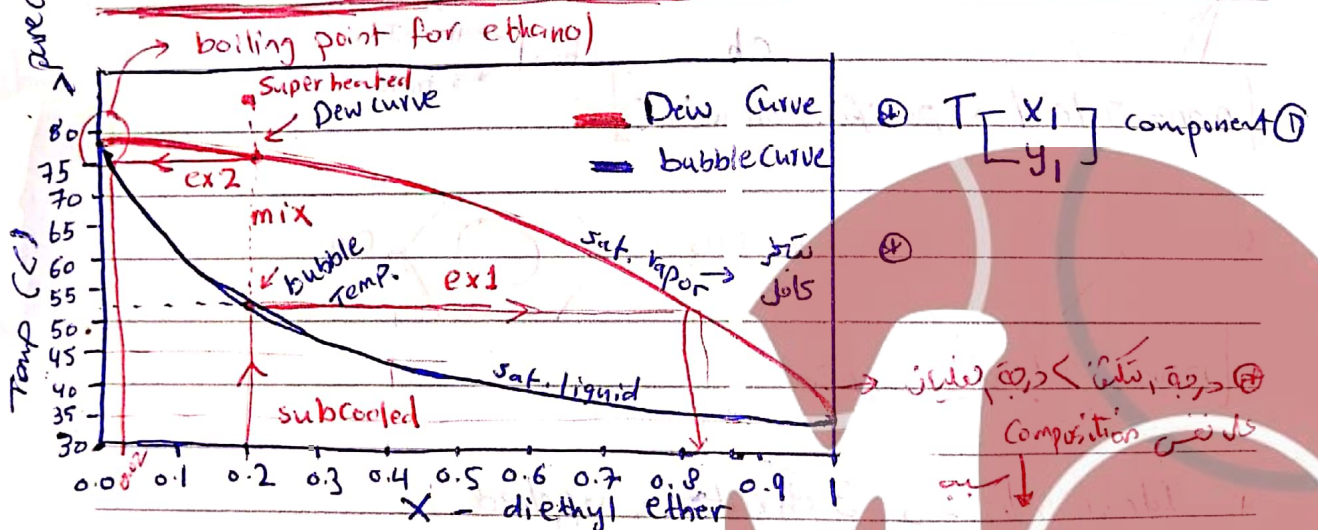
No: VLE Data Date: 8th Mar-2020

[0 - 1] → كان القياس
Curves.
Pure component limit

① $x_1=0$ boiling Temp for liquid or Condensation
 $x_2=1$ Temp for vapor $\equiv$ the same
 $x_1=1$ boiling Temp and $\rightarrow$ في نقطة $\rightarrow$
 $x_2=0$ condensation Temp

In mixture $\rightarrow$ vaporize first more volatile
 $\rightarrow$ condensate first less volatile

10th March - 2020



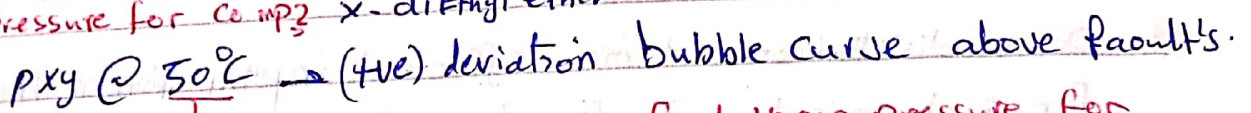
diethyl ether (1) ethanol (2) system

T_{xy} @ 0.1325 kPa $\rightarrow$ 1 atm

(+ve) deviation $\rightarrow$ bubble curve (P_{xy}) above Raoult's law line

② @ $x_1 = 0.2$

bubble Temp: Temp where the first bubble of vapor is formed
When heating a liquid consisting of two or more components
more volatile $\rightarrow$ vaporise more than less volatile component as
Temperature raises.



ethanol and diethyl ether $\rightarrow$ two point $\rightarrow$ Curve $\checkmark$

$T_{xy} \rightarrow$ bubble curve below Dew curve

② Quality $\rightarrow$ bubble curve = 0
Dew curve = 1

functional group not the same
chemical specific
system is not ideal

ex: 1: suppose mixture $x_1 = 0.2$ [diethylether]
 $p = 101.325$ (constant in T_{xy})

$[y_1]$ at equilibrium with that liquid?

at $e_2 \rightarrow$ bubble curve $\rightarrow$ e_2

$y_{12} = 0.7$ $T_{xy} = 0.5, 0.6$ for diethyl ether

$$\textcircled{*} k_1 = \frac{y_1}{x_1} = \frac{0.7}{0.2} = 3.5 \quad \textcircled{*} k_2 = \frac{y_2}{x_2} = \frac{0.3}{0.8} = 0.375$$

$$\therefore \alpha_{12} = \frac{k_1}{F_2} = \frac{3.5}{0.375} = 9.33$$

So, which material is more volatile? diethyl ether? why?

→ $\alpha > 1$

→ Boiling Temp 78°C for ethanol

" " 35°C for diethyl ether → more volatile

$B_p \downarrow$ volatility $\uparrow$

⊗ Does distillation column efficient separation method for such mixture? [yes]

→ $0.95 < \alpha_{1,2} < 1.05$ → not prefer distillation column

$\alpha_{1,2} = 9.33 \checkmark \checkmark$ → distillation column suitable

⊗ $\alpha = 1.1 \rightarrow 1.2$ → (distillation) جدا جدا

⊗ Bubble Temp? $\approx 55^\circ\text{C}$

ex 2: $y_1 = 0.2$ (vapor) Find x_1 that is at equilibrium?
جواب: $x_1 = 0.02$

⊗ $K_1 = \frac{0.2}{0.02} = 10$ ⊗ $K_2 = \frac{0.8}{0.98} = 0.81$

$\therefore \alpha_{12} = K_1/K_2 = 12.25$

* NOTE: α, K are fun. of composition
non-Ideal sys → K, α → aren't const.

⊗ Dew Point? 74°C

⊗ Dew point → نقطة الندى → liquid droplet

⊗ droplet → less volatile أقل تطاير

=

bubble point $\rightarrow$ more volatile

* P_{xy}

① bubble curve $\rightarrow$ indicator if our mixture applies Raoult's law or not

② vapor pressure $\uparrow$ Volatile $\uparrow$

③ prove that Raoult's line comes from Raoult's eq.?

$$y_i P_{total} = x_i P_i^{vap}$$

$$\begin{aligned} y_1 P &= x_1 P_1^{vap} \\ y_2 P &= x_2 P_2^{vap} \end{aligned} \quad \text{④}$$

$$(y_1 + y_2) P = x_1 P_1^{vap} + x_2 P_2^{vap}$$

for binary system $= 1$

$$P = x_1 P_1^{vap} + \frac{x_2}{(1-x_1)} P_2^{vap} \rightarrow P = x_1 P_1^{vap} + (1-x_1) P_2^{vap}$$

$$P = P_2^{vap} + (P_1^{vap} - P_2^{vap}) x_1 \rightarrow P = a + bx_1$$

$\downarrow$ intercept $\leftarrow$ عن العشر

$P_2^{vap} \rightarrow \text{constant} \rightarrow T \text{ constant}$

$$y_1 P = x_1 P_1^{vap} \rightarrow k_1 = \frac{P_1^{vap}}{P}$$

$$y_2 P = x_2 P_2^{vap} \rightarrow k_2 = \frac{P_2^{vap}}{P}$$

k_1 and k_2 fxn of T and P

$$\alpha_{12} = \frac{k_1}{k_2} = \frac{P_1^{vap}/P}{P_2^{vap}/P} \rightarrow \text{fxn of } T \rightarrow \text{Raoult's law}$$

No:----- Date:-----

* you don't improve distillation column by changing Pressure
From Raoult's law, change Temp!

ex: From Pxy curve:

$$y_1 = 0.7$$

$$x_1 \text{ at eq} = 0.175$$

$$k_1 = \frac{0.7}{0.175} = 4$$

$$k_2 = \frac{0.3}{0.025} = 0.36$$

$$\alpha_{1,2} = \frac{4}{0.36} = 11$$

Compare: $\alpha_{12} = 9.3$ $\alpha = 11$
(55°C) (50°C)

$$\alpha_{12} = \frac{P_1^{\text{vap}}}{P_2^{\text{vap}}}$$

→ vapor $\frac{\text{diethylether}}{\text{ethanol}}$

ask :: believe & recieve