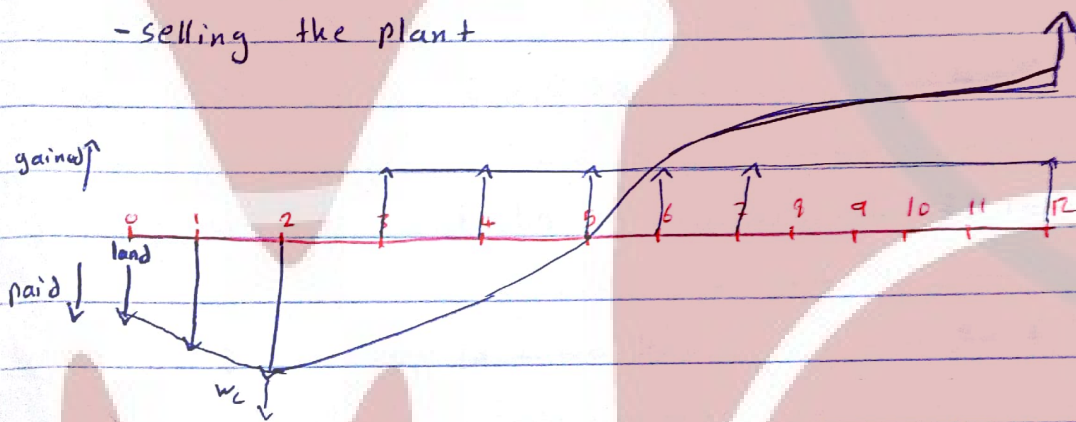


Plant :-

Estimation of capital cost :-

starting a plant you need :-

- purchasing of the land
- purchasing of the equipments and installation
- Running of the plant
- selling the plant



* classification of capital cost estimation

(1) order of magnitude

compare cost and size of your plant with existing one. $\Rightarrow$ [BFD]

(2) study estimate (major equipments should be included) $\Rightarrow$ [PFD]

(3) preliminary design (cost) estimate (scope) add. tubing, layout, electrical, $\dots \Rightarrow$ [PFD]

(4) Definitive estimate

Off-site, layout, instruments, utilities $\dots$

(5) Detailed estimate

(final PFD, P&ID, etc $\dots$)

These estimates are related to 5-classes

[Association for Advancement of cost Engineering] $\Rightarrow$ (AA CE)

Class	Level of project Definition	Expected accuracy rang	preparation effort w/ lowest cost index
Class 5	0 - 2 %	4 - 20 % $\pm$	1 unit
class 4	1 - 15 %	3 - 12 %	2 - 4 units
class 3	10 - 40 %	2 - 6 %	3 - 10 units
class 2	30 - 75 %	1 - 3 %	5 - 20 units
class 1	50 - 100 %	1	10 - 100 units

ask :: believe & recieve

* class 1: has a detailed estimate of $(+6\% \text{ to } -6\%)$
of accurate value $\Rightarrow$ the most accurate estimate

* class 5: has estimate EFORs to prepare this class in range
close to $0.015\% \text{ to } 0.3\%$ ^{cost} of total installed equipment
 $\Rightarrow$ least accurate

example:-

The estimated capital cost of a chemical plant using (class 4) is \$2M.
if the plant were to be built, over what range would you expect the actual
capital estimate to vary?

sol:

class 4 $\pm 12\%$ w/ to class 1:

* Lowest expected cost range:

- high value = $(\$2M) (1 + \frac{6}{100} \times 3) = \$2.36M$

- Low value = $(\$2M) (1 + (\frac{-6}{100}) \times 3) = \$1.76M$

* highest expected cost range:

- high value = $(\$2M) (1 + (\frac{6}{100}) \times 12) = \$3.44M$

- Low value = $(\$2M) (1 + (\frac{-6}{100}) \times 12) = \$1.04M$

ask :: believe & recieve

Example 2:-

compare the cost for performing an order of magnitude estimate and detailed estimate for a plant that costs \$5M to build?

sol:

Cost of C.O.M) 0.015% - 0.3%

Low value: $(\frac{0.015}{100})(\$5M) = \750

high value: $(\frac{0.3}{100})(\$5M) = \$15,000$

Detailed estimate (10-100) of C.O.M)

Lowest [lowest expected cost = $(\$5M)(0.015\% \times 10) = \7500

highest expected cost = $(\$5M)(0.3\% \times 10) = \$150,000$

highest [lowest expected cost = $(\$5M)(0.015\% \times 100) = 75,000$

highest expected cost = $(\$5M)(0.3\% \times 100) = \$1.5M$

Effect of capacity on purchased equipment cost:-

1. Matches [www.matches.com]

2. peter, Timmerhaus; plant design and economics

[www.mhhe.com/engineering/chemical/Peters/data]

equipments

$$C_{eq.2} = C_{eq.1} \left(\frac{A_2}{A_1} \right)^n$$

size, power, etc. of new equ. (points to A_2)
size of old one (points to A_1)
factor (points to n)
cost of new equ. (points to $C_{eq.2}$)
cost of existing equ. (points to $C_{eq.1}$)

* n: cost index

(if it is not specified, [use $n=0.6$]) $\rightarrow$ six-tenth rule

$$n = \frac{\log(C_1/C_2)}{\log(A_1/A_2)}$$

Equipment	Range	unit	n
- Respecating compressor (with motor drive)	0.7 - 1490	kw	0.84
- Heat exchanger (shell and tube, cs)	1.9 - 1890	m ²	0.59
- Vertical tanks, cs	0.4 - 76	m ³	0.3
- centrifugal blower	0.24 - 71	m ³ /s	0.6
- Jacketed kettle	0.2 - 3.8	m ³	0.48

Example:-

The cost of floating head tank (Base of $y = 2014$) has a size of 20,000 gallons (75.7 m³) and made up of cs, $C = \$84,400$ what will be the cost of 40,000 gallon given that $n = 0.5$.

sol:-

$$C_{40,000} = C_{20,000} \left[\frac{40,000}{20,000} \right]^{0.5} = \$119,359$$

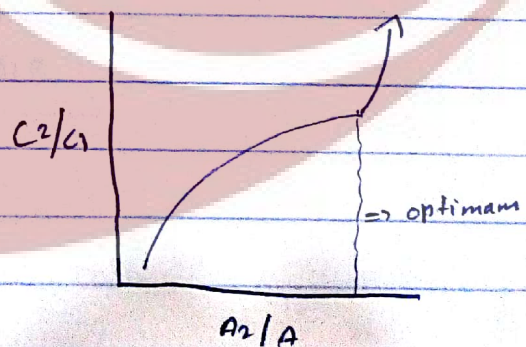
$$C_2 = 119,359$$

$$C_2/C_1 = 1.4$$

=>

$$C_1 = 84,400$$

A_2/A_1	C_2/C_1
2	1.4
4	2
8	2.8
12	3.46



* Effect of time on purchased cost equipment :-

$$C_2 = C_1 \left(\frac{I_2}{I_1} \right)$$

cost index at time 2
cost

Cost index

- (1) Marshall and swift cost index
- (2) chemical engineering plant cost index. (CEPCI)

<u>year</u>	<u>Marshall</u>	<u>CEPCI</u>
1936	817	318
1990	915	358
1995	1028	381
2005	1245	468
2016	—	541.7
2017 (march)	—	562.1
2017 (June)	—	566.6

example:-

The purchased cost of H.E (50 m²) in 2016 is \$ 35,200 Ccs, tolerate p=600 psi) use CEPCI to obtain cost of this equip. of year.

sol:

$$C_{2017} = C_{2016} \left(\frac{I_{2017}}{I_{2016}} \right)$$

$$= 35200 \left(\frac{566.6}{541.7} \right) = \$ 36,818$$

Estimation of capital cost of a plant:

The capital cost of a plant is a summation of many direct and indirect cost.

1- Direct project cost

(a) cost of equipment, C_p

(b) material required for installation, C_m
(piping, insulation, welding, fire protection, welding, instrumentation)

(c) Labor cost, C_L

2- indirect cost

(a) Taxes, insurance, etc...), C_{FIT}

(b) construction overhead, C_o

~~(c) contingencies and fees~~

~~(d) contingency factors and cover uniform circumstances
such as loss of time value, streams, small change in design)~~

3- contractor engineering expenses

(a) contingencies and fees

(b) contingency factors and cover uniform circumstances
such as loss of time value, streams, small change in design)

4- Auxiliary facilities

(a) site development, C_{site}

(purchased land cost, excavation smoothing, installation of hook up electricity, roads, walkway, parking, --- etc)

(b) Auxiliary building

(offices, board room, shop, cafeteria, etc...)

(c) off-site and utility, ~~etc~~ C_{off}

Long factor :

pto

it is used to estimate of building [major expansion] to an existing plant.

$$C_{TM} = F_{Long} \sum_{i=1}^{n=equip} C_{pi}$$

total module cost (capital cost of the plant) Long factor summation of equipment costs

Values of Long factor based on process :

	Long factor	updated value
Fluid - fluid	4.74	5.1
solid - fluid	3.63	4.1
solid - solid	3.10	3.2

example:

A young engineer with phillips petroleum has learned that on expansion of the solid-fluid process plant is expected to have delivered equipment cost of \$1.55 M, estimate the plant total cost.

$$C_{TM} = 4.1 \times \$1.55 = \$6.35 \text{ M.}$$

Bare module cost:-

This module is used to estimate the total cost of the plant based on direct and indirect cost of the equipments it is calculated based on BASE condition of equipment.

$$C_{BM} = F_{BM} C_p^0$$

Direct costs:

		Factor
- (01) Equipment	C_p^0	1
- (02) material	$C_m = \alpha_m C_p^0$	α_m
- (03) Labor	$C_L = \alpha_L (C_p^0 + C_m)$	$\alpha_L (1 + \alpha_m)$
- Total direct cost	$C_{DE} = C_p^0 + C_m + C_L$ $= C_p^0 + \alpha_m C_p^0 + \alpha_L (C_p^0 + \alpha_m C_p^0)$ $= C_p^0 [(1 + \alpha_m) (1 + \alpha_L)]$	

indirect cost:

		Factor
- a Freight	$C_{FIT} = \alpha_{FIT} (C_p^0 + C_m)$	$(1 + \alpha_m) \alpha_{FIT}$
- b over head	$C_o = \alpha_o C_L$	$(1 + \alpha_m) \alpha_L \alpha_o$
- c Engineering	$C_E = \alpha_E C_p^0 C_m$	$(1 + \alpha_m) \alpha_m$
- Total indirect cost	$C_{IDE} = C_{FIT} + C_o + C_E$ $C_{IDE} = \alpha_{FIT} (C_p^0 + C_m) + \alpha_o C_L + \alpha_E (C_p^0 + C_m)$	

$$C_{IDE} = (1 + d_m) [\alpha_{FIT} + \alpha_L d_o + \alpha_E] C_p^0$$

$$C_{BM} = C_{DE} + C_{IDE} = (1 + d_m) [1 + \alpha_L + \alpha_{FIT} + \alpha_L d_o + \alpha_E] C_p^0$$

$$F_{BM}^0 = (1 + d_m) [1 + \alpha_L + \alpha_{FIT} + \alpha_L d_o + \alpha_E]$$

$$\therefore C_{BM} = F_{BM}^0 C_p^0$$

Total module cost:

$$C_{TM} = C_{BM}^0 + C_{cont} + C_{fee}$$

$$* C_{cont} = \alpha_{cont} C_{BM}^0$$

$$* C_{fee} = \alpha_{fee} C_{BM}^0$$

$$\therefore C_{TM} = (1 + d_m) [1 + \alpha_L + \alpha_{FIT} + \alpha_L d_o + \alpha_E] (1 + \alpha_{cont} + \alpha_{fee}) * C_p^0$$

Example:-

The purchased cost for C_s heat exchanger operating at ~~ambient~~ ambient condition is \$100,000, the following % are related to direct and indirect cost of H.E,

item	%	calc. the Bare module cost factor	
Equipment	100	from F _{BM} and C _{BM} ⁰	
materials	71.4	sol:	
Labor	6.3	$\alpha_L = \frac{C_L}{C_p^0 + C_M} = \frac{0.6 C_p^0}{C_p^0 + 0.714 C_p^0} = \frac{0.63}{1 + 0.714} = 0.368$	
Freight	8		
overhead	63.4	$\alpha_{FIT} = \frac{C_{FIT}}{C_p^0 + C_M} = \frac{0.08 C_p^0}{C_p^0 + 0.714 C_p^0} = \frac{0.08}{1 + 0.714} = 0.047$	
Engineering	23.3		

$$d_o = \frac{C_o}{C_L} = \frac{0.634 C_p^0}{\alpha_L (C_p^0 + C_M)} = \frac{0.634 C_p^0}{0.368 C_p^0 + 0.714 C_p^0}$$

→

$$\alpha_E = \frac{C_E}{C_{P0} + C_H} = \frac{0.233 C_{P0}}{C_{P0} + 0.714 C_{P0}} = 0.136$$

$$\begin{aligned} \text{Then } \Rightarrow F_{BM} &= (1 + \alpha_L + \alpha_{FF} + \alpha_L \alpha_0 + \alpha_E) (1 + \alpha_H) \\ &= [1 + 0.368 + 0.047 + (1.009)(0.368) + 0.136] (1 + 0.714) \\ &= 3.291 \end{aligned}$$

$$\begin{aligned} C_{BM} &= F_{BM} C_{P0} = (3.291)(10000) \\ &= \$32,910 \end{aligned}$$

Bare module cost for non-base condition:-

(material of construction, high pressure)

~~Equation for~~

$$C_{BM} = F_{BM} C_{P0} = (B_1 + F_M F_P B_2) C_{P0}$$

F_M = factor related to MOC

F_P = factor relate to pressure.

$$\log_{10} F_P = C_1 + C_2 \log_{10} P + C_3 (\log_{10} P)^2$$

* to obtain $B_1, B_2 \Rightarrow$ من الأرقام التي كتبها

التي كتبها

* to obtain $F_M \Rightarrow$ table (A-3) = P: 1009
chart (A-18) = P: 1010

Equip	B_1	B_2
1- Exchanger (double pipe, multipipe--)	1.74	1.53
2- Fixed tube, floatinghead U-tube, kettle	1.63	1.66
3- Air cooler, plate plate	0.96	1.21
4- horizontal vessel	1.49	1.52
5- vertical "	2.25	1.82
6- pumps	1.89	1.35

Example:

What will be the Bare module cost of a floating head shell and tube H.E. ($A = 100 \text{ m}^2$) at the end of year 2016 operated at 1 bar, $CP^0(2000) = \$25,000$
sol:

$$* C_{BM} = C_{B1} + B_2 F_M F_P \quad CP^0$$

From table A-3? , $ID = 1 \Rightarrow$ use chart $\Rightarrow F_M = 1, F_P = 1$

$$C_{BM} = (1.63 + 1.66 \times 1 \times 1) (25,000)$$

$$= (3.29) (25,000)$$

$$= \$82,300$$

$$C_{BM_{2010}} = 82,300 \left(\frac{546.4}{304} \right) = \$118,353$$

(2) ~~fired~~ heater, Reboiler, Furnace:

$$C_{BM} = CP^0 F_{BM} F_P F_T$$

$F_T = 1$ For saturated condition

$$F_T = 1 + 1.84 \times 10^{-3} \Delta T - 3.35 \times 10^{-6} (\Delta T)^2$$

(3) Compressors, blowers, Evaporators, vaporizers.

$$C_{BM} = CP^0 F_{BM} F_P$$

as above

(4) sieve tray, valve tray, etc.

$$C_{BM} = CP^0 N F_{BM} F_q$$

$N = \text{No. of stages}$

$F_q = \text{quantity factor for trays} \Rightarrow N < 20 \Rightarrow$ ~~use chart~~

$$\Rightarrow \text{use } F_q = 0.4771 + 0.08516 \log_{10} N - 0.3473 (\log_{10} N)^2$$

$$N > 20 \Rightarrow F_q = 1$$

etermination of pressure correction for vessels.

$$F_p = \begin{cases} 1 & T < T_{min} & p > -0.5 \text{ bar} \\ 1.25 & & p < -0.5 \text{ bar} \\ \frac{(P+1)P}{(2)(944)(0.9) - 1.2(P+1)} & T > T_{min} & p > -0.5 \text{ bar} \end{cases}$$

(t_{min})
 thickness

$$t = \frac{PD}{2SE - 1.2P} + CA$$

$\Rightarrow$ p = pressure , D = diameter

S = max allowable pressure

E = weld factor , CA = corrosion allowance

ask :: believe & recieve

Total module :-

$$C_{TM} = \sum_{i=1}^n C_{TMi} = 1.18 \sum_{i=1}^n C_{BMi}$$

Gross Root :-

$$C_{GR} = C_{TM} + 0.5 \sum_{i=1}^n B_{Mi}$$

New chapter :-

Estimation of Manufacturing Cost :

$$C_{OM} = \underset{(DMC)}{\text{Direct cost}} + \underset{(GE)}{\text{General expenses}} + \underset{(FMC)}{\text{Fixed cost}}$$

* Direct cost :-

- 1- raw material, C_{RM}
- 2- utilities, C_{ut}
- 3- waste treatment, C_{wb}
- 4- operating labor, C_{OL}
- 5- direct supervision, $0.18 C_{OL}$
- 6- maintenance, repair, $0.06 [C_{GR} \text{ or } C_{TM}]$
- 7- supplies, $0.15 C_{OL}$
- 8- patents, $0.03 C_{OM}$

$$DMC = C_{RM} + C_{ut} + C_{wb} + C_{OL} + 0.18 C_{OL} + 0.06 \underset{GR}{C_{TM}} + 0.15 C_{OL} + 0.03 \underset{COM}{C_{OM}}$$

$$DMC = C_{RM} + C_{ut} + C_{wb} + 1.33 C_{OL} + 0.069 \underset{\substack{C_{TM} \\ C_{GR}}}{FCT} + 0.03 C_{OM}$$

* Fixed capital cost :-

1- Depreciation $\rightarrow 0.1 \text{ FCI}^{\text{TM}}$

2- Taxes, insurance $\rightarrow 0.032 \text{ FCI}$

3- overhead cost $\rightarrow 0.708 \text{ CoL} + 0.036 \text{ FCI}$

$$\text{FMC} = 0.708 \text{ CoL} + 0.168 \text{ FCI}$$

* General expenses (GE) :-

-1 Administrative cost $\rightarrow 0.177 \text{ CoL} + 0.009 \text{ FCI}$

-2 Distribution and selling cost $\rightarrow 0.11 \text{ CoM}$

-3 Research and Development $\rightarrow 0.05 \text{ CoM}$

$$\text{GE} = 0.177 \text{ CoL} + 0.009 \text{ FCI} + 0.16 \text{ CoM}$$

$$\text{CoM} = 1.235 [\text{CRM} + \text{C}_{ut} + \text{C}_{wt}] + 2.73 \text{ CoL} + 0.303 \text{ FCI}$$

ask ;; believe & recieve

* Operating Labor Cost:-

$$N_{OL} = [6.29 + 31.7p^2 + 0.23 \frac{N_{np}}{I}]^{0.5}$$

N_{OL} : Number of Labors
 p : no. of processing steps for solids
 N_{np} : no. of equipments that are related to non solid
 I : [Towers, reactors, heat exchangers, heaters, compressors, transportation, distribution, particulate sizing, control...]

* each Labor Requires \$50,000 - 60,000

- A labor works 49 weeks/year

- 3 weeks vacation

- each week $\rightarrow$ 5-shifts

$\therefore$ Labor works = $5 \times 49 = 245$ shifts

A plant operates 365 days/year, this requires 365 (3-shift)
 = 1095 shifts/year

$$N_{\text{Labor}} = \frac{1095}{245} = 4.5 \Rightarrow \text{so I need } [4-5] \text{ Labors to work in this plant/day}$$

$$\text{Cost } (4-5) (50,000) = (\$200,000 - \$250,000)$$

Labors:-

1-engineer

2-Forman

3-board man

4- 1st operator

5- 2nd 11 (2)

6- 3rd 11 (3)

7- 4th 11 (4)

Example:-

(Refere to hydro dealkylation process (Turton book))

Toluene $\rightarrow$ benzene

Number of major Equipments = 11

What is the number of operating labor for this process.

sol:

$$N_{OL} = [6.29 + 3.17 p^2 + 0.23 N_{up}]^{0.5}$$

$$N_{OL} = [6.29 + 0.23 (11)]^{0.5} = 2.97 = 3$$

$$\text{Total } (4.5)(3) = 13.4 = 14$$

$$C_{OL} = (14)(50,000) = \$700,000$$

<http://data.bls.gov> $\Rightarrow$ يعطي معلومات عن الlabors في USA

ask :: believe & recieve

Utilities:- (how much fuel that we used?!)

- utility cost = \$ (prices of fuel)

The cost of utility is directly proportional with the source:

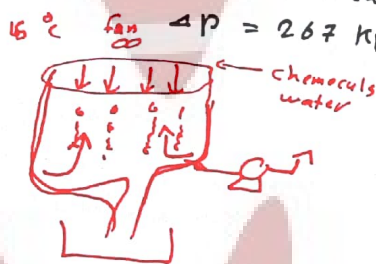
- 1- if it is purchased from public or private sector
- 2- supplied by the company
- 3- generated by the process.

example:-

estimate the utility cost for production a circulating water stream using a mechanical draft cooling tower consider a base case and only 1 GJ/h of energy reused from the process

given that: fan power = 1.31 kw

cost of chemical being used = \$ 0.165 / 1000 kg water
from heuristic $\Rightarrow \Sigma = 0.75$



$$q = c_p m \Delta T$$

$$1 \times 10^9 \text{ J/h} = m (4180 \text{ J/kg}) (45 - 15^\circ)$$

$$m = 7974 \text{ kg/hr} \Rightarrow \text{water circulating}$$

water evaporated??

$$\rho_{\text{water}} = 2417 \text{ kJ/kg}$$

$$m_{\text{evaporate}} = \frac{1 \times 10^9}{2417 \times 10^3} = 41307 \text{ kg/h}$$

$$W_{\text{pump}} = \dot{V} \Delta p$$

this assuming 100% efficient pump

$$W_{\text{pump}} = \frac{\dot{V} \Delta p}{\Sigma} = \frac{\dot{m}}{\rho} \frac{\Delta p}{\Sigma} = \frac{7974}{1000} \times \frac{267}{0.75} \cdot \frac{1}{3600} = 0.79 \text{ kw}$$

kw is per 1 GJ



cost of electricity = \$0.06 / kw from table

total cost of electricity

$$= [0.79 \text{ kw} + 1.31 \text{ kw}] \times 0.06$$

$$= \$0.125 / \text{GJ}$$

$$\text{cost total of chemicals} = \frac{\$0.165 \times 413.7}{10000 \text{ kg water}}$$

$$= \frac{\$0.068}{1 \text{ GJ}}$$

$$\text{cost of makeup water} : \frac{\$0.354}{1 \text{ GJ}} \div 1 \text{ GJ} = \$0.354$$

$$\begin{aligned} \text{total cost} &= \text{cost makeup water} + \text{cost of chemicals} + \text{cost of electricity} \\ &= 0.354 + 0.068 + 0.125 \\ &= \$0.54 / \text{GJ} \end{aligned}$$

Cost of raw material:

[chemical market Reporter]

$$\text{stream factor} = \frac{\text{No. of days}}{365} < 1$$

$$\text{S.F} \approx 0.95 - 0.98$$

Example: -

or Toluene-benzene process

$$\text{flow rate of toluene} = 10,000 \text{ kg/hr}$$

$$\text{Benzene} = 8210 \text{ kg/hr}$$

$$\text{stream factor} = 0.95$$

what are the yearly cost/rate of both reactant and products

$$\text{given that cost of toluene} = \$0.322 / \text{kg}$$

$$\text{Benzene} = \$0.349 / \text{kg}$$

Sol:

yearly consumption of toluene =

$$\text{flow rate} = \frac{10,000 \text{ kg}}{\text{hr}} \times \frac{24 \text{ hr}}{1 \text{ day}} \times \frac{365 \text{ day}}{1 \text{ year}} \times 0.95 = 83,200,000 \text{ kg/year}$$

$$\text{toluene} = 0.322 \times 83,200,000 = \$26,773,600 / \text{year}$$

H.w + ملاحظات: 7/11/2017

H.w: problems 3, 4, 5,

station rate of Benzene

$$= 8210 \frac{\text{kg}}{\text{hr}} \times \frac{24 \text{ hr}}{1 \text{ day}} \times \frac{365 \text{ day}}{1 \text{ year}} \cdot 0.95$$

$$= 68,323,620 \text{ kg/year}$$

$$\begin{aligned} \text{price of benzene} &= 68,323,620 \times 0.349 \\ &= \$23,844,443 / \text{year} \end{aligned}$$

your process is not feasible

example:-

estimation the cost of manufacturing for plant with the following given information

equipment	utility used	efficiency η	(use) usage	Annual cost	you should be able to calculate
E-201					
E-202	Lps		3800	10,800	
E-203		-	5550	270,000	
E-204	CW				
E-204	Lps	-	4200	11,900	
E-204	electricity	-	3090	150,000	
E-205	electricity	0.8	1.6 kw	786	
		0.8	1.5 kw	726	

Raw materials is not give, $C_{RM} = \$898,000$

$$C_{OM} = 0.303 FCI + 2.73 C_{OL} + 1.235 (C_{RM} + C_{ut} + C_{wt})$$

$$N_{OL} = [6.29 + 31.7 \frac{\text{p}}{\text{h}} + 0.23 \frac{\text{M}}{\text{h}}]^{0.5} = 2.77$$

$$\text{operator} = 2.77 \times 4.5 = 13$$

$$C_{OL} = \$60,000 \times 13 = \$650,000$$

$C_{RM} =$

$$\begin{aligned} C_{ut} &= 10,800 + 270,000 + 11,900 + 150,000 + 786 + 726 \\ &= \$443,312 \end{aligned}$$

$C_{wt} = 0$

see waste treatment cost

$$\begin{aligned} C_{OM} &= 0.303 \times 898,000 + 2.72 (650,000) + 1.235 [C_{RM} + 444,212 + 0] \\ &= \$2483,000 + 1.235 C_{RM} \end{aligned}$$

you pay even plant is non operating.

int:

Engineering Economic and Analysis:

①

2-11-2017

الضيف

* Invest $\rightarrow$ Bank $\rightarrow$ profit

Value of money $\rightarrow$ (Company Project) $\rightarrow$ profit

* money (if invested) $\rightarrow$ generate money

present value $\xrightarrow{\text{interest}}$ new value

present value of money

future value //

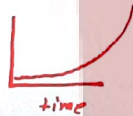
Life time (* of year)

interest

* The yearly interest rate = $\frac{F-P}{n}$

* Future value:

$$F = (1 + ni) P$$



types of interest:

1- simple $F = P(1 + ni)$
Future value $\leftarrow$ P (present value) $\leftarrow$ n (year) $\leftarrow$ i (interest rate)

2- compound interest $\Rightarrow F = P(1+i)^n$ $\leftarrow$ this is the standard

3- interest is changing w/ time $\Rightarrow F = P \prod_{k=1}^n (1+i_k)$
copy

example:-

How much you need to invest in saving account based on 6% interest rate to have \$5000 in 5 years??

sol:

$$F = \$5000$$

$$F = P(1+i)^n = P(1+0.06)^5 \Rightarrow P = 3,736$$

base for compound interest:

- yearly
- monthly
- daily
- continuous

$$r = \frac{i_n}{m} \quad \begin{matrix} \text{number} \\ \text{of} \\ \text{periods} \end{matrix}$$

$\Rightarrow$

example:

i - per year
needed per month $\Rightarrow r = \frac{i}{12}$

example:

for the case $i = 12\%$, what will be the interest per month?

sol:

$$r = \frac{12}{12} = 1\%$$

Effective interest rate:

$$i_{\text{eff}} = \left(1 + \frac{i_n}{m}\right)^m - 1$$

$$F = P \left(1 + \frac{i_n}{m}\right)^m$$

example:-

what is the effective annual interest for nominal rate of 8% per annum when compounded monthly?

sol:

$$i_n = 8\%; \quad m = 12$$

$$i_{\text{eff}} = \left(1 + \frac{8\%}{12}\right)^{12} - 1 = 8.3\%$$

for given $P = 1000$

$$F = P \left(1 + i_{\text{eff}}\right)^n$$

$$= 1000 \left(1 + \frac{0.08}{12}\right)^{12}$$

$$= 1083$$

Continuous compound interest:

3

$$i_{eff} = e^{in} - 1$$

Example:

How much you would have to invest
at 6% for 6 years to obtain \$1791

Assume Basic interest.

soln

$$P = F \left(\frac{1}{(1+i)^n} \right) = 1791 \left(\frac{1}{1+0.06} \right)^6 = 1263$$

adardar

ask ;; believe & recieve

Cash Flow diagram:-



x-axis → time

y-axis → cash flow

Upward → earned money

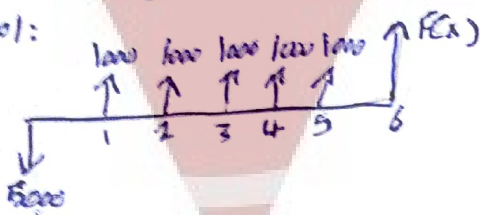
down word ⇒ lost money

Example:-

You invest today, withdraw \$1000 at the end of each year, how much you have at the end of 6 years.

$$i = 6\%$$

sol:



$$P_1 = \frac{F_1}{(1+0.06)^1} = \frac{1000}{1.06} = 943.4$$

$$P_2 = \frac{F_2}{(1+0.06)^2} = \frac{1000}{1.1236} = 890$$

$$P_3 = 839.6$$

$$P_4 = 792.1$$

$$P_5 = 747.3$$

$$P_x = \frac{x}{(1+0.06)^6} \Rightarrow 5000 = 943.4 + 890 + 839.6 + 792.1 + \frac{x}{(1+0.06)^5} \Rightarrow x = \$1117.2$$

sol 2: bring all money till the end

$$F_p = 5000(1+0.06)^6 = 7092.6$$

$$F_1 = 1000(1+0.06)^5 = 1339.2$$

$$F_2 = 1000(1+0.06)^4 = 1265.5$$

$$F_3 = 1000(1+0.06)^3 = 1191$$

$$F_4 = 1123.6$$

$$F_5 = 1060$$

$$F_p - \sum_{i=1}^5 F_i = x = 1117.2$$

A uniform series of cash transaction

(2)

$$F_n = A [(1+i)^1 + (1+i)^2 + \dots]$$

$$* F_n = A \left[\frac{(1+i)^n - 1}{i} \right]$$

$$F_n = P(1+i)^n$$

$$F_n = A \left[\frac{(1+i)^n - 1}{i} \right]$$

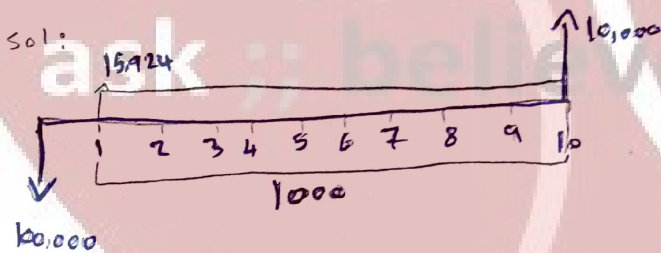
$$A = \frac{F_n}{\frac{(1+i)^n - 1}{i}}$$

$$A = \frac{P(1+i)^n \cdot i}{(1+i)^n - 1}$$

$$P = A \left[\frac{(1+i)^n - 1}{i(1+i)^n} \right]$$

Example:-

A piece of equipment costs \$100,000 - if a Vot Engineer is borrowed this amount from a bank with 9% interest and should these amount be paid within 10 years, with a fixed payment yearly. The equipment needs \$1000/^{year} for operation and yield a profit of \$15,924 ^{yearly}, She was expecting to sell this equip. at the end with \$10,000. Do you think this engineer learn something from economy??



$$A = 15,924 - 1000 = 14,924$$

$$P = 100,000$$

$$F = 10,000$$

$$A = \frac{P(1+i)^n \cdot i}{(1+i)^n - 1} = \frac{100,000 (1+0.09)^{10} \cdot 0.09}{(1+0.09)^{10} - 1}$$

$$= 15,582$$

$$A = \frac{F \cdot i}{(1+i)^n - 1} = \frac{10,000(0.09)}{(1+0.09)^{10} - 1} = 658.2$$

$$IAR = 14,924 + 658.2 - 15,582 = \$0.2$$

solve based on $i = 0.08$

$$\sum A_i = 14,924 + 690.3 - 14,902$$

$$= \$ 712$$

~~interest~~

adar

ask ;; believe & recieve

Plant :-

7-11-2017

Depreciation :-

1- straight line :-
$$dk^{\text{sl}} = \frac{FCI - sv}{n}$$

2- Declining balance method :-
$$V_{\text{at present}} = V_{\text{original}} (1-f)^n$$

$$f = 1 - \left(\frac{s}{v}\right)^{1/n}$$

no. of years
at year 2 as 2
at year 3 as 3

Example :-

original price of equipment \$22,000, used for 10 years, sold for \$2000. what is the price of this equipment after 5 years?

sol:

- straight line
$$d = \frac{FCI - sv}{n} = \frac{22,000 - 2,000}{10} = 2,000$$

$$V_5 = FCI - ad = 22,000 - 5 \times 2,000 = 12,000$$

- Declining balance :

$$f = 1 - \left(\frac{s/v}\right)^{1/n} = 1 - \left(\frac{2,000}{22,000}\right)^{1/10} = 0.2131$$

$$V_5 = v(1-f)^5 = 22,000(1-0.2131)^5 = \$6,650$$

3- Sum of year Digits method :-

$$dk^{\text{syd}} = \frac{[n+1-k](FCI-s)}{n/2(n+1)}$$

total no. of years the year I want

why syd:

$$n/2(n+1)$$

year 1: 1	1
year 2: 2	3
year 3: 3	6
year 4:	

4- Double declining balance method:-

$$d_k^{DD} = \frac{2}{n} \left[FCI - \sum_{i=0}^{k-1} d_i \right]$$

example:-

$$FCI = 150,000,000$$

$$S = 10,000,000$$

$$n = 7 \text{ years}$$

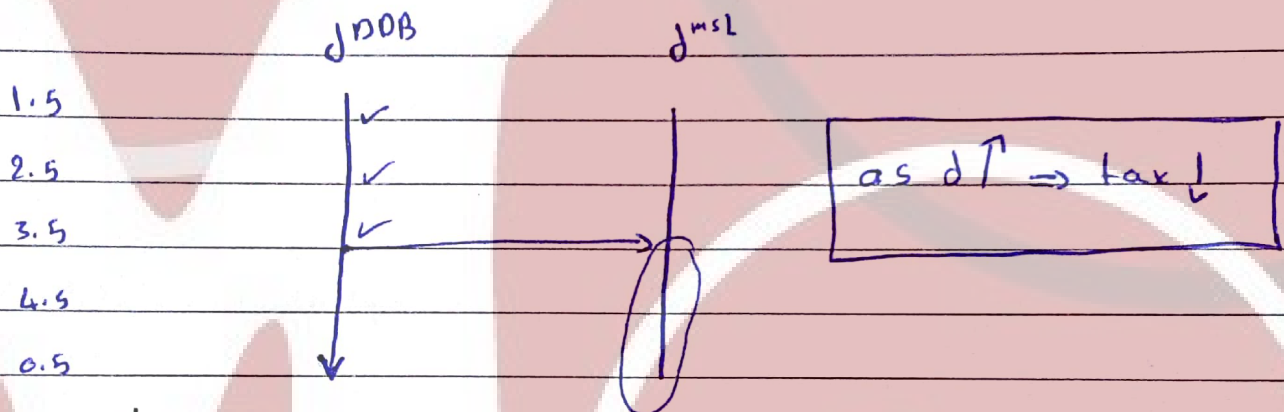
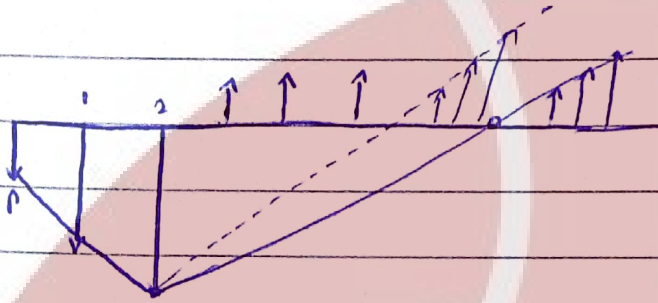
depreciation comparison ??

year	d_k^{SL}	d_k^{SYD}	d_k^{DD}	$BV = FCI - \sum d_i$ $= FCI - 8d_i$ $\times 10^{-6}$
0	—	—	—	150
1	$\frac{150-10}{7} = 20$	$\frac{(7+1-1)(150-10)}{28} = 35$	$\frac{2(150-0)}{7} = 42.9$	$150 - 42.9 = 107.1$
2	20	= 30	$\frac{2}{4}(150 - 42.9) = 30.6$	$107.1 - 30.6 = 76.5$
3	20	= 25	$\frac{2}{4}(76.5) = 21.9$	$76.5 - 21.9 = 54.6$
4	20	= 20	15.6	39
5	20	= 15	11.1	27.9
6	20	= 10	8	19.9
7	20	= 5	4.9	10
			$FCI - \sum d_i - S$	
	140	140	140	10

Current depreciation method:-

Modified accelerated cost recovery system [MACRS]

=> starting with DDB ending with msl. => work for 5 years.



example :-

consider an equipment that has a FCI = 100000\$

calculate the modified accelerated cost recovery system.

$$d_k^{DD} = 2/5 \left[FCI - \sum_{i=0}^{k-1} d_i \right], \quad d_k^{SL} = \frac{FCI - \sum_{k=1}^{n-1} d_k}{(n-k)}$$

gear	d_k^{DD}	d_k^{SL}
1/2	$2/5 [100 - 0] \times 1/2$ $= 20K$	
1.5	$2/5 [100 - 20]$ $= 32$	$(100 - 20) / 4.5 = 7.78$
2.5	$2/5 [100 - 52] = 19.2$	$(100 - 52) / 3.5 = 13.71$
3.5	$2/5 [100 - 71.2] = 11.52$	$(100 - 71.2) / 2.5 = 11.52$
4.5	$2/5 [100 - 82.7] = 6.91$	$(100 - 82.7) / 1.5 = 11.52$
0.5		dep for last 0.5 year $= 0.5 \left(\frac{100 - 82.7}{1.5} \right) = 5.76$

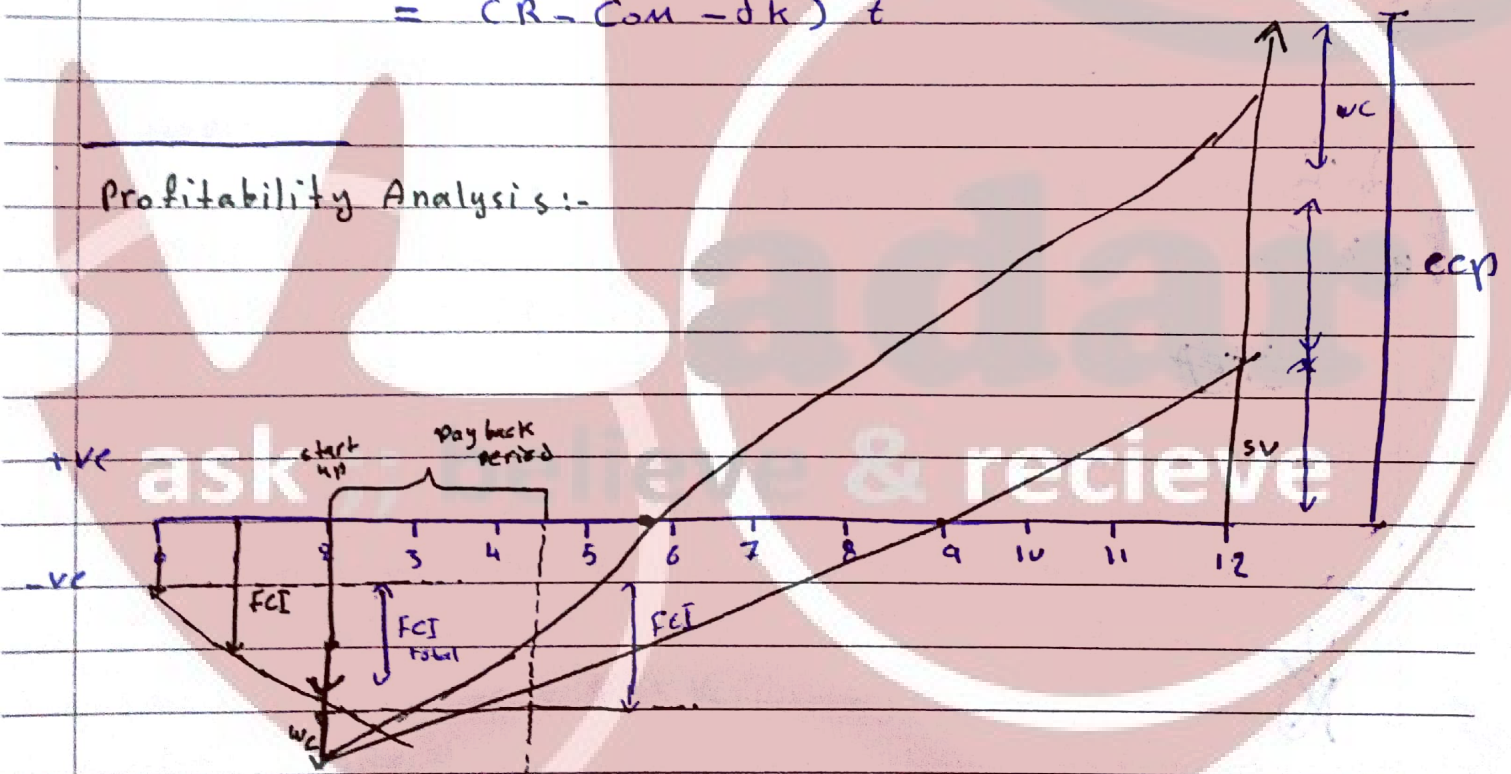
Depreciation

year	dm
0.5	20
1.5	32
2.5	19.5
3.5	11.52
4.5	11.52
5.5	8.76

Taxation, cash flow, profits:-

$$\text{income tax} = (\text{Revenue} - \text{expenses}) \cdot \text{tax rate}$$

$$= (R - \text{Com} - dk) \cdot t$$

Profitability Analysis:-

- * Criteria:
- [1] time $\rightarrow$ Payback period
 - [2] net positive value
 - [3] rate of return

1- time criteria:-

pay back period: time from start up, to recover the FCI

2- cash criteria:-

cumulative cash position (CCP)

cumulative cash Recovery (CCR) , $\frac{\sum \text{of all positive values}}{\sum \text{of all negative cash}}$

$$CCR = 1 + \frac{CCP}{\text{land} + Wc + FCI}$$

3- Interest Rate criteria:-

Rate of return on investment (RoROI)

$$RoROI = \frac{\text{Avg annual net profit}}{FCI} \Rightarrow \frac{\text{slope}}{FCI} \cdot \frac{1}{n} \text{ service life [10 years] from start up}$$

Example:-

A new chemical plant is going to be built with the required capital investment:

1)- cost of land = \$10M

2)- FCI = \$150M

FCI₁ = \$90M

FCI₂ = \$60M

* plant starts up after 2 years from installation.

Wc = 20% of FCI = $0.2 \times 150 = \$30M$

yearly sales revenue = \$75M

COM = \$30M

Taxation = 45%

salvage value = \$10M

Depreciation based on 5 years MACRS

project life = 10 years.

* calculate, PBP, RoR, Net positive cash flow.

Cash Flow

net cash flow

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