

Q1 (15 POINTS)

Calculate the heat that must be transferred in each of the following cases assuming ideal gas behavior

1. Nitrogen gas contained in a 5-liter flask at an initial pressure of 3 bar is cooled from 90 °C to 30°C.
2. A stream of nitrogen flowing at a rate of 100 mol/min is heated from 20°C to 100°C.

Remark: For the C_p use only the first two terms (a and b) of the polynomial of Table B.2



ideal

$V = 5 \text{ L}$

$T_1 = 90^\circ\text{C}$

$p = 3 \text{ bar}$

$T_2 = 30^\circ\text{C}$

$C_p = C_v + R$

$Q = ?$

closed



$\cancel{\Delta KE} + \cancel{\Delta PE} + \Delta \hat{U} = Q$

$\Delta U = n \Delta \hat{U} = Q$

$\Delta \hat{U} = \int_{T_1}^{T_2} C_v dT$

$\Delta \hat{U} = \int_{90}^{30} (2.9 \times 10^{-3} + 0.2199 \times 10^{-5} T) dT$
 $= [2.9 \times 10^{-3} T + 0.2199 \times 10^{-5} \frac{T^2}{2}]_{90}^{30}$
 $= 0.879 - 2.6189 = -1.739$

$C_v = C_p - R$

$R = 8.314 \text{ J/mol K}$

$C_p = C_v + R$

$C_v = C_p - R$

[15 mol K]

$\int_{90}^{30} (2.9 \times 10^{-3} - 8.314 \times 10^{-3} + 0.2199 \times 10^{-5} T) dT$
 $= 0.029 T + 0.2199 \times 10^{-5} \frac{T^2}{2}$

$\int 0.029 T + 0.2199 \times 10^{-5} \frac{T^2}{2} \Big|_{90}^{30}$

$\Delta U = -1.739$

$= 0.879 - 2.6189 = -1.739 \text{ kJ}$

$\Delta U = Q$

$Q = -1.739 \text{ kJ}$

$$\Delta \hat{U} = Q$$

Q_2

$$V = 5L$$

$$= 5 \text{ mol}$$

~~$V = 5L$~~
 ~~$= 5 \text{ mol}$~~

$$\Delta \hat{U} = \Delta U n$$

$$= -1.319 \text{ KJ}$$

$$\times 5 \text{ mol}$$

$$= -6.595 \text{ KJ}$$

(2)



$$\Delta \cancel{KE} + \Delta \cancel{PE} + \Delta \overset{\text{open}}{H} = Q - W$$

$$\Delta H = Q$$

$$\Delta H = \int_{T_1}^{T_2} C_p dT$$

$$= \int_{20}^{100} 29 \times 10^{-3} + 0.219 \times 10^{-5} T$$

$$= \left[29 \times 10^{-3} T + 0.219 \times 10^{-5} \frac{T^2}{2} \right]_{20}^{100}$$

$$2.910995 - 0.5804 = 2.3305 \text{ KJ/mol}$$

$$\Delta \hat{H} = \frac{\Delta H}{\cancel{H}} n = 2.3305 \frac{\text{KJ}}{\text{mol}} \times 100 \frac{\text{mol}}{\text{min}}$$

$$\Delta \hat{H} = Q = 233.06 \frac{\text{KJ}}{\text{min}}$$

$$Q = 233.06 \frac{\text{KJ}}{\text{min}}$$

- ④ steam tables are most accurate because data come from experiments not from estimations ~~the heat capacity~~

Q2 (15 POINTS)

A stream of water vapor flowing at a rate of 250 mol/h is cooled from 600 °C and 10 bar to 100 °C and 1 atm. Calculate the cooling duty (kW) using: $Q = ?$

1. Steam Tables
2. Table B8
3. Heat capacity data for water reported in Table B2
4. Which of the answers in 1, 2, and 3 above is most accurate, and why?

Ans: most accurate

① $\Delta \hat{H} = Q$

$$\Delta \hat{H} = 32676 - 3697 = -1021 \frac{\text{kJ}}{\text{kg}}$$

$$\Delta \hat{H} = -1021 \frac{\text{kJ}}{\text{kg}} \times \text{mass flow}$$

$$= -1021 \frac{\text{kJ}}{\text{kg}} \times 1.251 \frac{\text{kg}}{\text{s}} \times 10^{-3}$$

$$= -1.277 \frac{\text{kJ}}{\text{s}} = \text{KW}$$

$$250 \frac{\text{mol}}{\text{h}} \times \frac{1 \text{ h}}{3600 \text{ s}} = 0.06944 \frac{\text{mol}}{\text{s}}$$

$$0.06944 \frac{\text{mol}}{\text{s}} \times 18.016 \frac{\text{g}}{\text{mol}}$$

$$\dot{m} = 1.251 \frac{\text{kg}}{\text{s}} \times 10^{-3}$$

② $\Delta \hat{H} = \dot{Q}$

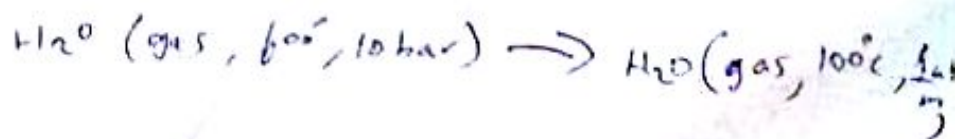
ref H_2O (Gas, 25°C, 1 atm)

$$\Delta \hat{H} = 2.54 - 20.91 = -18.37 \frac{\text{kJ}}{\text{mol}}$$

$$\Delta \hat{H} \times n = \Delta \hat{H}$$

$$-18.37 \frac{\text{kJ}}{\text{mol}} \times 0.06944 \frac{\text{mol}}{\text{s}}$$

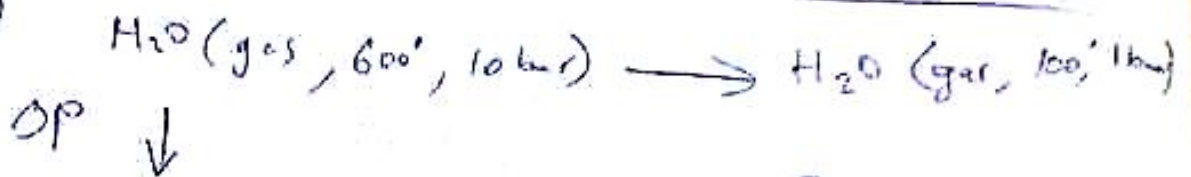
$$= -1.2756 \frac{\text{kJ}}{\text{s}}$$



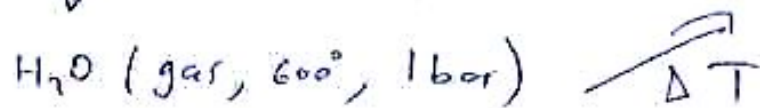
③

$$\Delta \hat{H} = \int_{T_1}^{T_2} C_p dT$$

③



OP $\downarrow$



$\Delta P \approx \Delta \hat{H} = 0$ for gases ✓

DT:

$$\Delta \hat{H} = \int_{T_1}^{T_2} C_p dT$$

$$= \int_{600}^{100} 33.46 \times 10^{-3} + 0.685 \times 10^{-5} T dT$$

$$= 33.46 \times 10^{-3} (T) + 0.685 \times 10^{-5} \frac{T^2}{2} \Big|_{600}^{100}$$

$$= 3.38025 - 21.309$$

$$= -17.92875 \text{ kJ/mol}$$

$\Delta \hat{H} = \Delta H_m$

$$\Delta H = -17.92875 \frac{\text{kJ}}{\text{mol}} \times 0.06944 \frac{\text{mol}}{\text{s}}$$

$$= -1.209 \text{ kJ/s}$$

h ✓

- _____

$$hA : \text{inlet} = 0.014 \frac{\text{kg H}_2\text{O}}{\text{kg DA}}$$
$$h_A : \text{inlet} = 0.014 \frac{\text{kg H}_2\text{O}}{\text{kg DA}}$$