

Q1: In the circuit shown, prove that $\sum P = 0$.

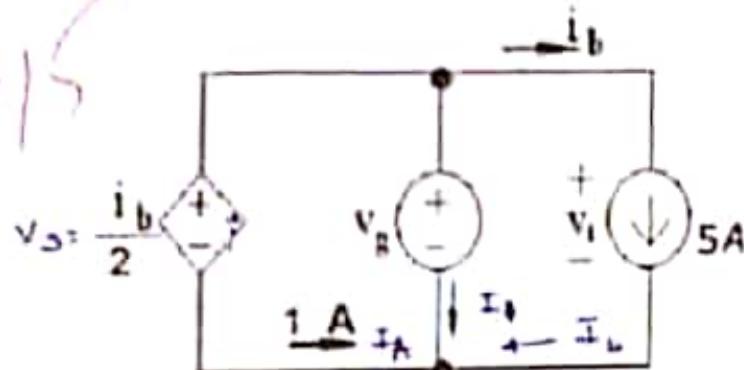


Fig. 1

$$i_b = 5 \text{ A}$$

$$v_a = \frac{i_b}{2} = \frac{5}{2} = 2.5 \text{ V}$$

$$v_g = 2.5 \text{ V}$$

$$v_i = -2.5 \text{ V}$$

$$I_{h1} + I_{b1} + I_{i1} = 0$$

$$I_{h1} + 5 + 1 = 0$$

$$I_{h1} = -6$$

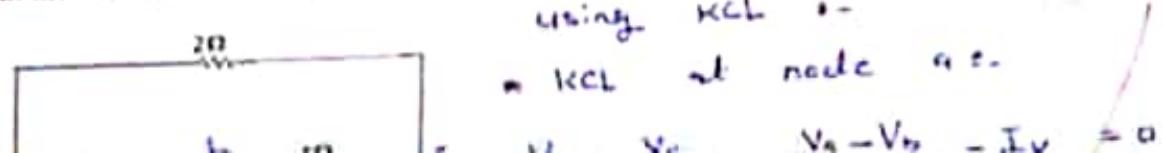
$$\begin{aligned} P_1 &= V_i I \\ &= (2.5)(1) \\ &= +2.5 \text{ Watt} \end{aligned}$$

$$\begin{aligned} P_2 &= V_i I \\ &= (-2.5)(-4) \\ &= 10 \text{ Watt} \end{aligned}$$

$$\begin{aligned} P_3 &= VI \\ &= (2.5)(5) \\ &= -12.5 \text{ Watt} \end{aligned}$$

$$\begin{aligned} \sum P &= 0 \\ 2.5 + 10 - 12.5 &= 0 \end{aligned}$$

Q2: In the circuit shown in Fig. 2, use nodal analysis method to find the current I_L



using KCL :-

* KCL at node "a"

$$V_a - V_b - I_L = 0$$

Q1.

$$i_b = 5A$$

$$V_s = 25V$$

$$V_g = 2.5V$$

$$V_i = 2.5V$$

$$i_a + i_s + i_b = 0$$

$$i_a + 2.5 + 5 = 0$$

$$i_a = -6.5$$

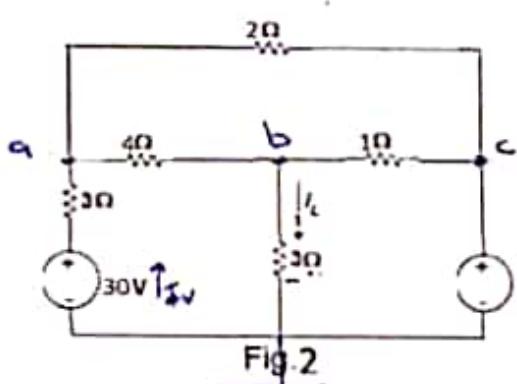
$$\begin{aligned} P_s &= V I \\ &= (25)(-6) \\ &= -15 \text{ Watt} \end{aligned}$$

$$\begin{aligned} P_{V_s} &= V I \\ &= 2.5(1) \\ &= 2.5 \text{ Watt} \end{aligned}$$

$$\begin{aligned} P_R &= V I \\ &= 2.5(5) \\ &= 12.50 \text{ Watt} \end{aligned}$$

$$\begin{aligned} \Sigma P &= -15 + 2.5 + 12.5 \\ &= 0 \end{aligned}$$

Q2: In the circuit shown in Fig. 2, use nodal analysis method to find the current I_L



Using KCL :-

* KCL at node a :-

$$\frac{V_a - V_c}{2} + \frac{V_a - V_b}{4} - I_v = 0$$

* KCL at node b :-

$$\frac{V_b - V_c}{1} + \frac{V_b - V_a}{4} + \frac{V_b}{3} = 0$$

$$\frac{3}{4}V_a - \frac{V_b}{4} - I_v = 10 \quad \text{--- (1)}$$

$$-\frac{V_a}{4} + \frac{19}{12}V_b = 20 \quad \text{--- (2)}$$

$$V_a + 3I_v = 30 \quad \text{--- (3)}$$

$$V_a = 2640/119$$

$$V_b = 1920/119$$

$$I_v = 310/119$$

~~$$V_c = 0 = 20V \rightarrow V_c = 20V$$~~

$$V_a = 30 - 3I_v$$

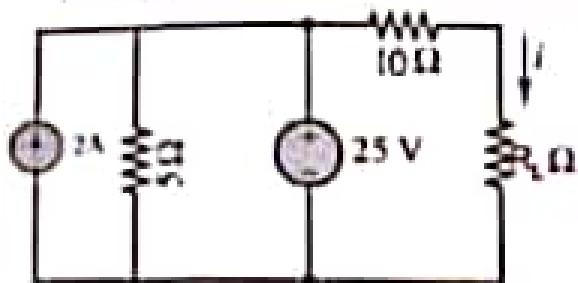
$$V_a + 3I_v = 30$$

$$i_L = \frac{V_b}{3}$$

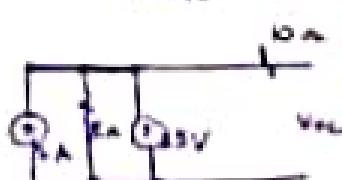
$$= \frac{640}{119}A$$

$$= 5.378A$$

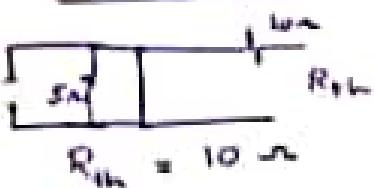
Q3: Find R_L to transfer the maximum power and the power in the Fig. 3.



$$R_L \rightarrow V_{oc}$$



$$V_{oc} = 25 \text{ V}$$



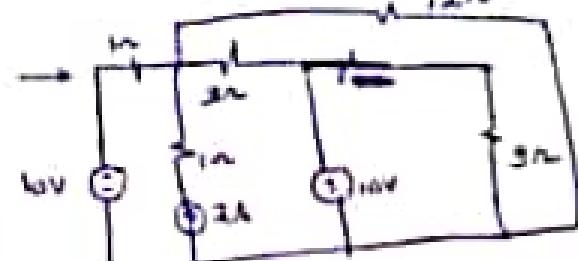
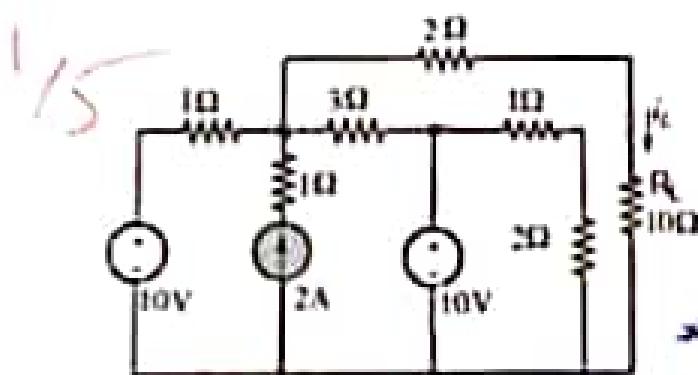
$$R_{th} = 10 \Omega$$

$$\begin{aligned} P_{max} &= \frac{V_{th}^2}{4R_{th}} \\ &= \frac{25^2}{4 \times 10} \\ &= \frac{25}{4} \text{ W} \\ &= \frac{12.5}{8} \text{ W} \end{aligned}$$

$\therefore R_L = R_{th}$ to trans for the max. power

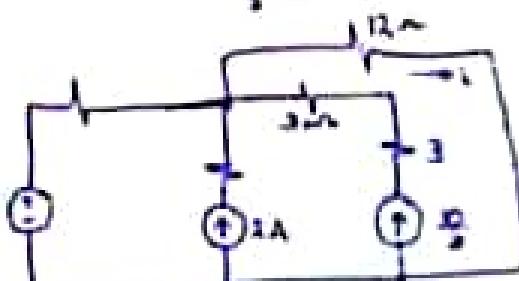
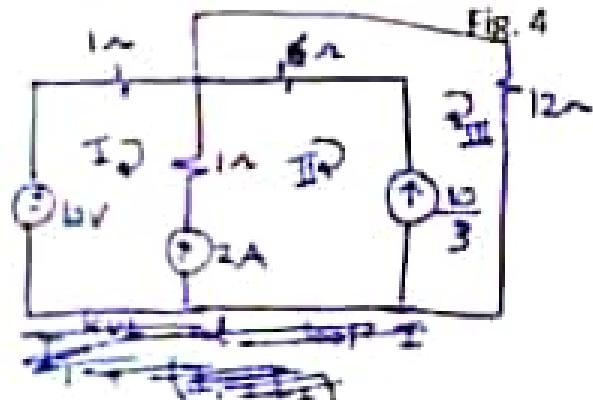
$$R_L = 10 \Omega$$

Q4: In the circuit shown in Fig. 4, using mesh analysis method to find the current i_{12n} .



\therefore Using node transformation

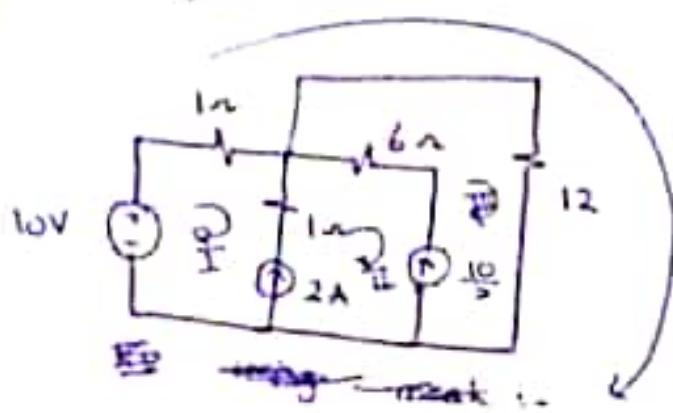
$$I = \frac{10}{3} \text{ A}$$



$\leftarrow J_1$

Q4

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by mesh

$$-10 + I_1 + 12 I_2 = 0 \quad \text{--- (1)} \quad \checkmark$$

$$I_2 - I_1 = 2 \quad \text{--- (2)} \quad \checkmark$$

$$I_3 - I_2 = \frac{10}{2} = 5 \quad \text{--- (3)} \quad \checkmark$$

$$I_1 + 12 I_2 = 10$$

$$-I_1 + I_2 = 2$$

$$-I_2 + I_3 = 5$$

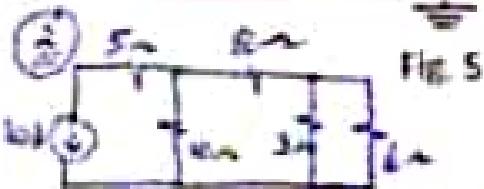
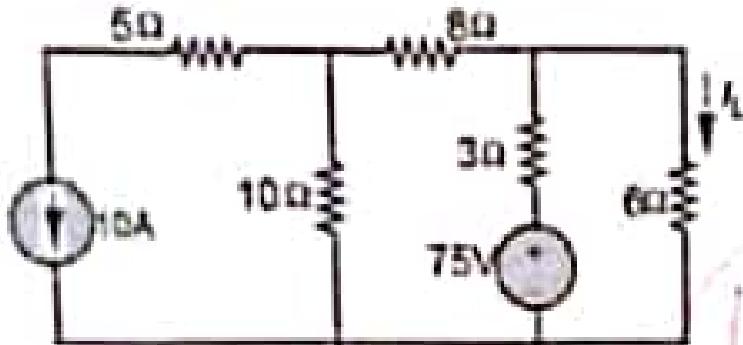
$$I_1 = -\frac{54}{13} A$$

$$I_2 = -\frac{28}{13} A$$

$$I_3 = \frac{46}{13} A$$

$$I_3 = i = \frac{46}{13} A$$

Q5. In the Fig. 5, find I_1 by using superposition Principle.



$$R_{eq} = \frac{5}{2} + \frac{5}{3} = 2.5 \Omega$$

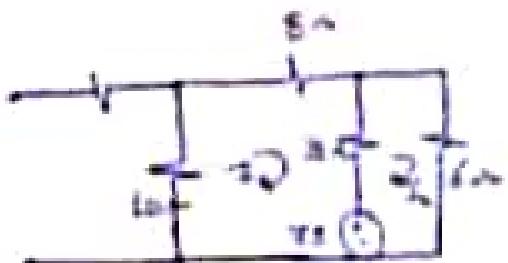
$$I_2 = 2 + 8 = 10 \text{ mA}$$

$$I_3 = \frac{10 \times 5}{15} = 5 \text{ mA}$$

$$R_{eq} = 5 + 5 = 10 \Omega$$

~~Now to solve for I_1~~

$$\begin{aligned} I_1 &= 10 + 5 \\ I_1 &= 15 \text{ mA} \end{aligned}$$



VL at Loop 1

$$10I_1 + 5I_2 + 3(I_1 - I_2) = 75$$

$$6I_1 + 2(I_2 - I_1) = 75 = 0$$

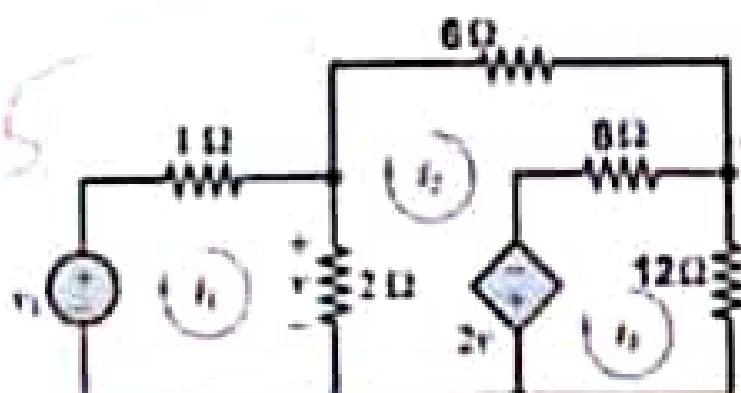
$$2I_1 - 1I_2 = -25$$

$$-2I_1 + 9I_2 = 25$$

$$\begin{cases} I_1 = -4 \\ I_2 = 15 \end{cases}$$

$$\begin{cases} I_1 = I_2 = 5 \end{cases}$$

Q6. In the circuit shown in Fig. 6, write a set of equations according to mesh current method to solve the unknown currents.



Then we get equations :-

$$1I_1 - 2I_2 = V_1$$

$$-6I_1 + 20I_2 - 8I_3 = 0$$

$$-4I_1 - 4I_2 + 20I_3 = 0$$

$$1I_1 + 2(I_2 - I_3) = V_1 = 0$$

$$3I_1 - 2I_2 - V_1 = 0 = 0$$

* VL at I_1 (loop 1)

$$6I_2 + 8(I_2 - I_3) - 2V_1 = 0$$

$$+ 2(I_2 - I_3) = 0$$

$$+ V_1 = 2(I_2 - I_3)$$

$$+ 14I_2 - 4I_3 + 1(2 - 1) - 4(I_2 - I_3)$$

$$20I_2 - 9I_3 - 6I_1 = 0$$

* VL at Loop 2 :-

$$8(I_2 - I_3) - 12I_2 + 2(2I_2 - I_3) = 0$$

$$20I_2 - 4I_1 - 8I_2 = 0 = 0$$