

Why control?

Control :- operate under known & specified conditions.

① **Safety** :- (environment, process, ---)

② **operability** :- certain conditions are required by chemistry & physics for the desired reactions.

③ **Economic** :- $\rightarrow$ plants are expensive & intended to make money
 $\rightarrow$ final products must meet market requirement of purity otherwise they will be un-saleable.

$\rightarrow$ Conversely the manufacture of an excessively pure product will involve unnecessary cost.

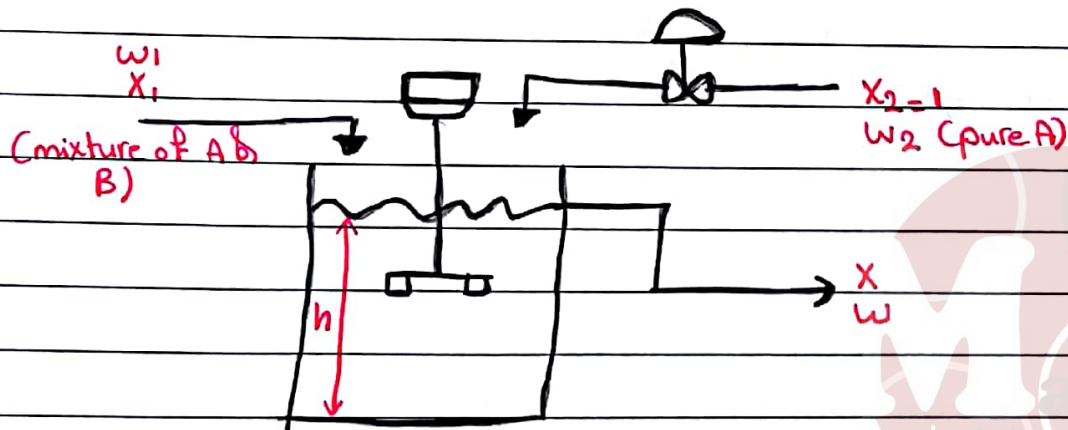
process :- refers to a physical or chemical change of matter or conversion of energy.

Process Variables :-

- Inputs

- outputs

* Any thing const. it's not our objective in control, but we can use them in our calculations.



w_1, w_2 & $w \rightarrow$ mass flow rate

X_1, X_2 & $X \rightarrow$ mass fraction of component A

* Speed of mixing: could be variable or not

* Height: constant

Outlet flow is as an over flow

* Cross sectional area: constant

* mass flow rate: variable ~~(w_1, w_2)~~

* mass fraction: variable (x_1, x) while x_2 is constant.

* We always concern with variables not with constants!

* we call constants $\rightarrow$ "process parameters".

$w_1 \rightarrow$ inlet flow
(w_2, w) should be
overall balance

Inputs :- $x_1, w_1, w_2 \rightarrow$ they are variables.

Outputs :- x, w .

what should we control?

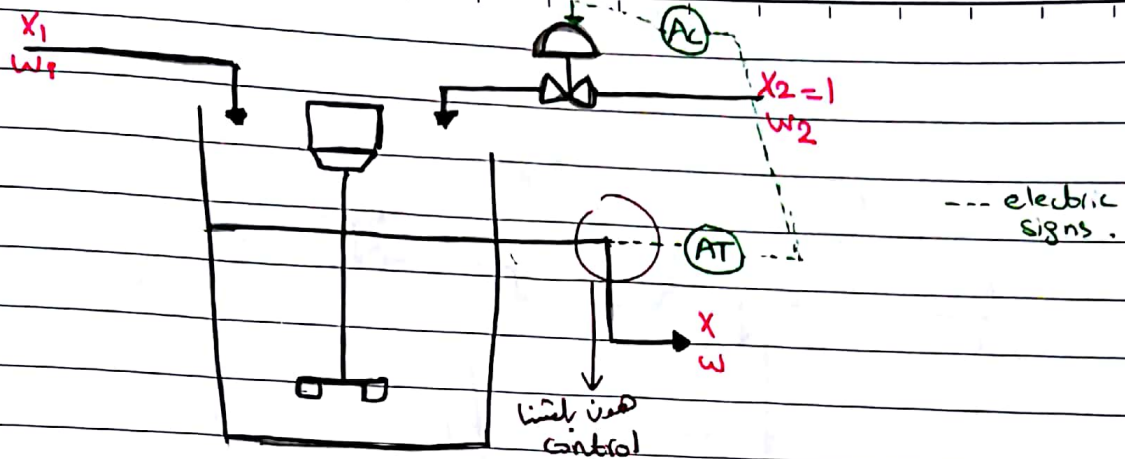
our control objective is x or w

(Outputs) x or w

our objective is to maintain

our process (target) at a certain

(My control system)



AC: composition controller

AT: composition analyzer / transmitter.

المفروض يقارن القراءة التي مسجلة في desired أو required value
it's call (set point) → the value you sit it!

We should :-

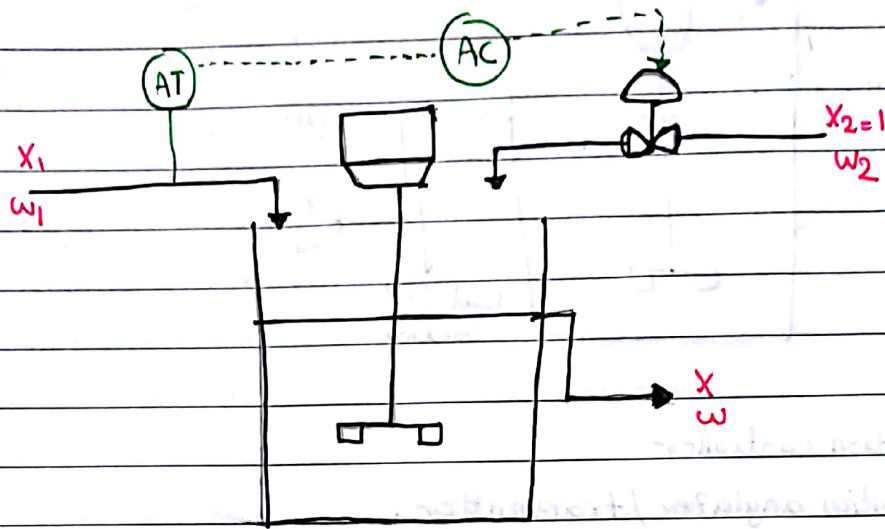
- ① identify our control variables
- ② our measuring device.
- ③ أداة قراءة لـ element آخر
- ممانج دة Control

* Elements of our control system :-

- ① control variables w
- ② measuring devices AT
- ③ Controller AC
- ④ Final control element . Valve
- ⑤ manipulated variable w_2 → الذي بتغيره احنا .

دائماً يكون واحد من inputs

There is a deviation of conc. occurred → so I should do correction.



* Elements of control system :-

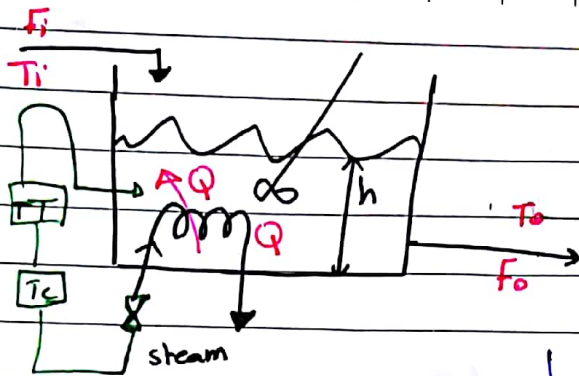
- ① Control variable W_1, X_1 → المفروضات (X) بس هو
- ② measuring device AT indirect.
- ③ Controller AC ↓ depends on
- ④ final control element control valve
- ⑤ manipulated variable W_2 Calculated value of outputs.

فان كان الـ manipulated variable هو الـ output فانه prevention action !

Here it (A PREVENTION ACTION)

Feed Forward :- monitors & correct the changes according its measures !

Feed back :- monitors & correct the changes according its sources.



well stirred tank.
Outlet = Inlet.

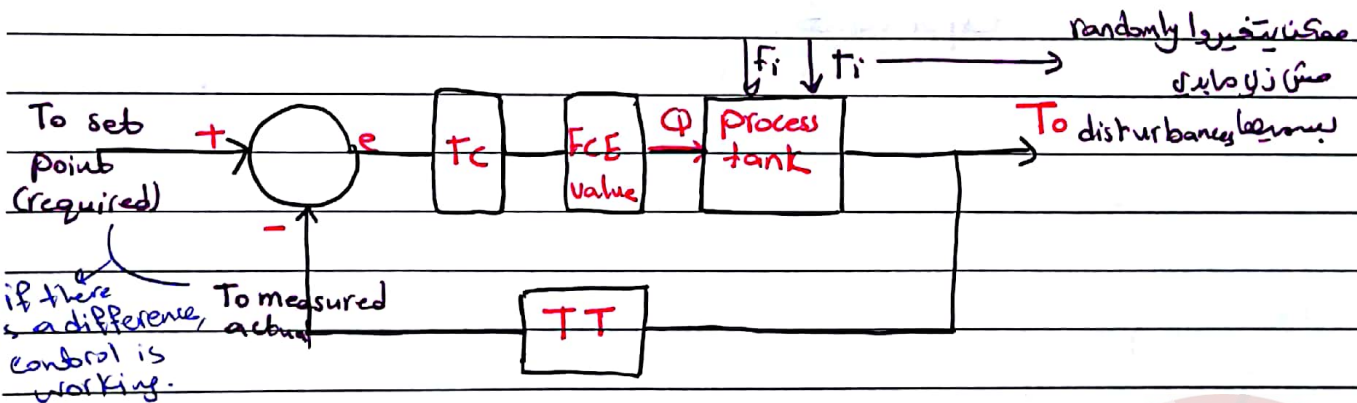
(h) من أجل أن يكون
flow
تدفق
Outlet من أجل أن يكون
overflow
h → const.

Control variable → T

Process & Instrument
(piping) Design..... pg. 11
Block diagram من أجل أن يكون

Variables من أجل أن يكون Control
Control affect من أجل أن يكون Control (Block) من أجل أن يكون
(as output) Variable

Block diagram for temperature control for this system.



Q : manipulated variable

T_o : control variable من أجل أن يكون T_o Control
(Q) من أجل أن يكون

model of
ProcessControl Q & T in a process

Kinds of models

- steady state → (design) Q & T in a process
- unsteady state (Volume) Q & T in a process

Ways to get dynamic models

- Experiment
- Theoretical

① Theoretical → (analytical)

based on basic equations (mass, energy & momentum balances)

- make equations

general model. Q & T in a process

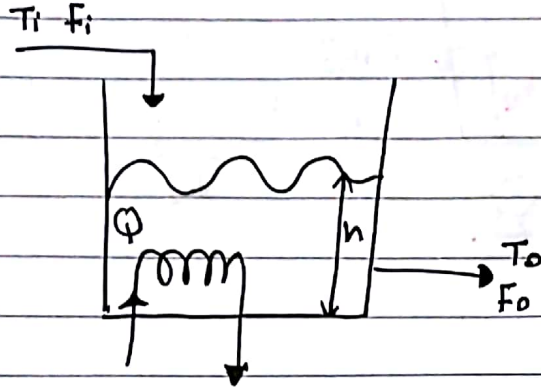
② Theoretical Experimental (Imperical model)

some of parameters → may not be in basic equation (mass, energy, & momentum)

→ some of lack in information

Valid just for this experiment. Q & T in a process

* un steady state modeling:-



$$\frac{d(\rho V)}{dt} = \rho F_i - \rho F_o$$

$\frac{\rho_0 \times \rho L^3}{\rho L^3} \times \frac{L^3}{\text{time}}$

$$\frac{dV}{dt} = F_i - F_o$$

$F_i \rightarrow$ volumetric flow rate.

Let $\rho \rightarrow \text{const}$

$$V = Ah \Rightarrow \frac{dAh}{dt} = F_i - F_o$$

$A \rightarrow \text{const}$

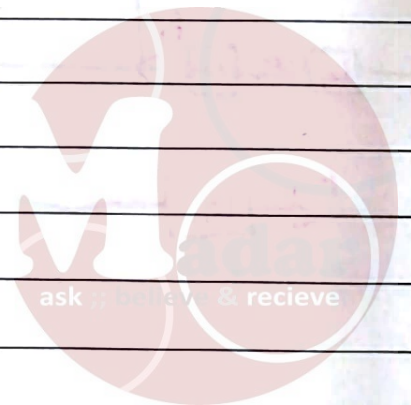
$$A \frac{dh}{dt} = F_i - F_o$$

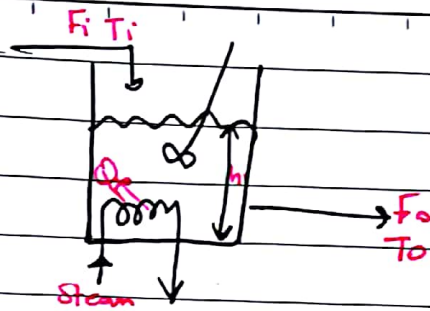
aim $(F_o) = \frac{h \rightarrow \text{driving force}}{R \rightarrow \text{resistance to flow}}$
 $(h) \rightarrow \text{driving force}$

$$A \frac{dh}{dt} + h = R F_i$$

is a function in the (h) change in F_i

نسب (F_i) الى h





$$AR \frac{dh}{dt} h + h = RF_i$$

Energy Balance (Enthalpy Balance)

$$\frac{d [\rho V c_p (T_o - T_{ref})]}{dt} = \rho c_p F_i (T_i - T_{ref}) - \rho c_p F_o (T_o - T_{ref}) + Q$$

const. ρ, c_p بفرض

Zero = T_{ref} مرجع

$$V = Ah$$

$$F_o = \frac{h}{R}$$

$$\rho c_p A \frac{dh T_o}{dt} = \rho c_p F_i T_i - \rho c_p F_o T_o + Q$$

$$F_o = \frac{h}{R}$$

$$\frac{dh T_o}{dt} + \frac{h}{AR} T_o = \frac{1}{A} F_i T_i + \frac{Q}{\rho c_p A}$$

$$\frac{h dT_o}{dt} + T_o \frac{dh}{dt} + \frac{1}{AR} h T_o = \frac{1}{A} F_i T_i + \frac{Q}{\rho c_p A}$$

بفرض h متغيرة

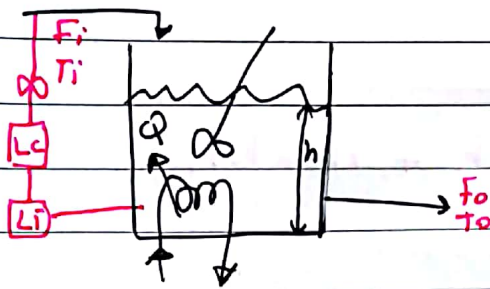
$$AR \frac{dh}{dt} h = RF_i$$

المفروضات

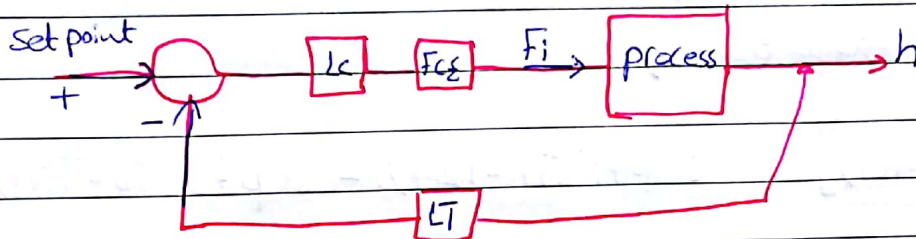
$$\frac{dT_o}{dt} + T_o = \frac{F_i T_i}{A} + \frac{Q}{\rho c_p A}$$

- Q, T_i, F_i

في T_o المتغير



$$AR \frac{dh}{dt} + h = R F_i$$



Manipulated $\rightarrow F_i$

Control variable $\rightarrow h$

جریان ورودی و خروجی و دما و سطح
Variable F_i و Variable h
steady state / رابطه

بزرگ بین F_i level
inlet flow rate

$$AR \frac{dh}{dt} + h = R F_i$$

$$\neq \frac{dh}{dt} \text{ at steady state} = 0$$

* deviation from steady state. (steady state, دینامیک)

$$AR \frac{dh}{dt} + h = R F_i$$

$$0 + h_{ss} = R F_{ss}$$

$$AR \frac{d(h)}{dt} + (h - h_{ss}) = R (F_i - F_{ss})$$

دینامیک $\leftarrow (h - h_{ss})$

$$h - h_{ss} \rightarrow h'$$

$$F_i - F_{ss} \rightarrow F'$$



$$AR \frac{dh'}{dt} + h' = R f_i'$$

← مستوى اللي بترتبه التغير في level
التغير في Flow rate
← deviation! process controller

↳ transfer function: Function which transfers the change in inputs with the transfer in the outputs.

laplace transform:-

(linear differential equation to Algebraic)

$t \rightarrow t$ domain

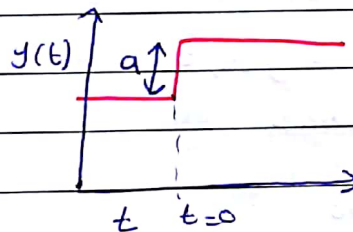
$s \rightarrow$ imaginary domain

$$\mathcal{L} y(t) = y(s)$$

$$\mathcal{L}^{-1}(y(s)) = y(t)$$

1 * STEP function:-

$$y(t) = \begin{cases} 0 & t < 0 \\ a & t \geq 0 \end{cases}$$

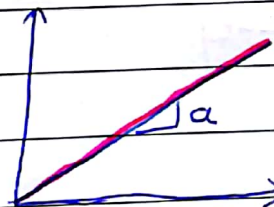


$$\mathcal{L} \text{ step function} = \frac{a}{s}$$

2 * Ramp function:-

$$y(t) = at$$

gradually increasing
as temp or pressure

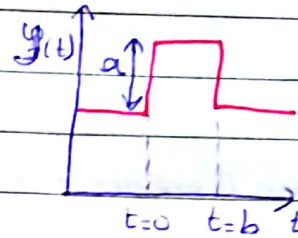


$$\mathcal{L}(at) = \frac{a}{s^2}$$

3. Pulse Function.

Integral of control system

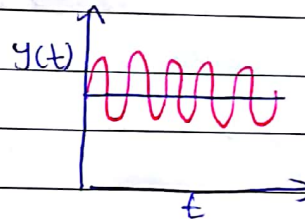
$$y(t) = \begin{cases} 0 & t < 0 \\ a & 0 < t < b \\ 0 & t > b \end{cases}$$



$$\mathcal{L}(\text{pulse}) = \frac{1 - e^{-bs}}{s}$$

4. Sin function

$$y(t) = a \sin \omega t$$



$$\mathcal{L}(\sin) =$$

$$\mathcal{L}^{-1}(y(s)) = y(t) = \dots$$

Final value Theorem:

$$y(t)_{\infty} = \lim_{s \rightarrow 0} s y(s)$$

$$y(s) = \frac{k}{s(as+1)}$$

$$y(t) = \mathcal{L}^{-1}(y(s)) = \mathcal{L}^{-1} \left(\frac{k}{s(as+1)} \right)$$

$$y(t) = k(1 - e^{-at})$$

$$y(t)_{\infty} = k$$

$$y(t) = \lim_{s \rightarrow 0} s y(s) = \lim_{s \rightarrow 0} s \left[\frac{k}{s(as+1)} \right] = k$$

④ Initial value theorem

$$y(t) \Big|_{t=0} = \lim_{s \rightarrow \infty} s y(s)$$

$$y(t) = k [1 - e^{-at}]$$

$$y(0) = 0$$

$$\lim_{s \rightarrow \infty} s y(s) = \lim_{s \rightarrow \infty} s \left[\frac{k}{s(as+1)} \right] \Rightarrow \frac{k}{\infty} = 0$$

at initial always the initial value of deviation = 0



* First order system *

What is first order system?

It is a system described by first order differential equation.

differential $\rightarrow$ linear $\rightarrow$ deviation $\rightarrow$ Laplace.

$$\begin{aligned} a_0 \frac{dy(t)}{dt} + a_1 y(t) &= b x(t) \\ \text{deviation} \end{aligned}$$

$$a_0 \frac{dy}{dt} + a_1 y_{ss} = b x_{ss}$$

$$a_0 \frac{dy}{dt} + a_1 y' = b x'$$

$$y' = y - y_{ss}$$

$$x' = x - x_{ss}$$

$$\frac{a_0}{a_1} \frac{dy}{dt} + y = \frac{b}{a_1} x(t)$$

Laplace $\frac{a_0}{a_1} [s y(s) - y(0)] + y(s) = \frac{b}{a_1} x(s)$
 because all the initial values of the deviation is equal zero



$$\frac{a_0}{a_1} s y(s) + y(s) = \frac{b}{a_1} x(s)$$

$$y(s) \left[\frac{a_0}{a_1} s + 1 \right] = \frac{b}{a_1} x(s)$$



$$\frac{y(s)}{x(s)} = \frac{b/a_1}{\frac{a_0}{a_1}s + 1}$$

transfer function = $\frac{\text{laplas transform of the change in the output}}{\text{laplas transform of the change in the input}}$

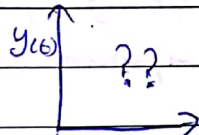
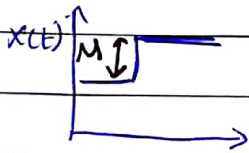
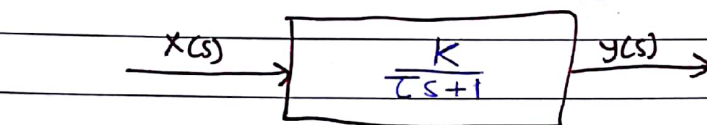
$$\frac{y(s)}{x(s)} \rightarrow \frac{\text{laplas transform of output}}{\text{input}} \neq \frac{y(t)}{x(t)}$$

$$\frac{y(s)}{x(s)} = \frac{k}{\tau s + 1}$$

k : steady state gain = b/a_1

τ : time constant = a_0/a_1

First order system : is a system can be identify by k & τ .



Reli is a system in the time domain.

$$y(s) = \frac{k}{\tau s + 1} * x(s)$$

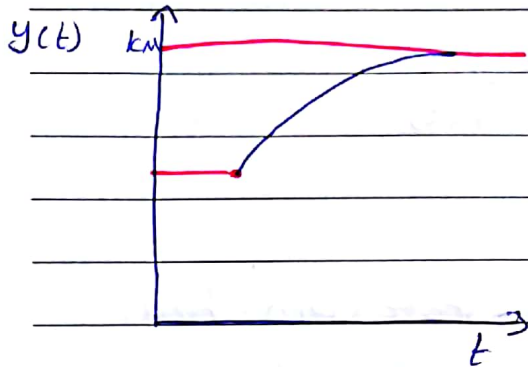
$$y(s) = \frac{k}{\tau s + 1} * \frac{M}{s}$$

$$y(s) = \frac{kM}{(\tau s + 1)s}$$

$$y(t) = \mathcal{L}^{-1} y(s) = \mathcal{L}^{-1} \frac{kM}{s(\tau s + 1)}$$

$$\frac{1}{s(s+a)} = \frac{1}{a} (1 - e^{-at})$$

$$y(t) = KM [1 - e^{-t/\tau}]$$



Final value $\downarrow$ $\lim_{t \rightarrow \infty} y(t) = KM$

$$y(t) \text{ at } t=0 = KM (e^{-0/\tau}) = KM$$

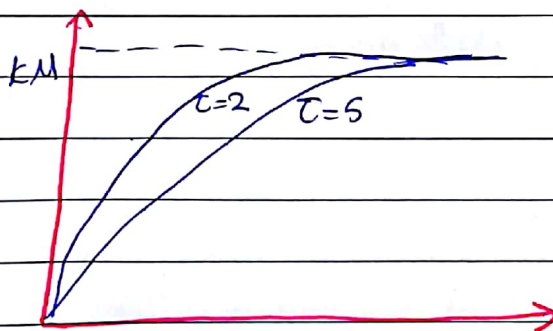
$$KM [1 - 0] = KM$$

$0 =$ initial value $\downarrow$ $\lim_{t \rightarrow 0} y(t)$

Final is determined by K only

large, small, steady state value

$K \rightarrow$ is a parameter of my system
but M is not a parameter



$\tau=2$ $\tau=5$ $\rightarrow$ steady state value

τ determines Final value

$\tau \rightarrow$ residence time

$\tau \uparrow$ response time

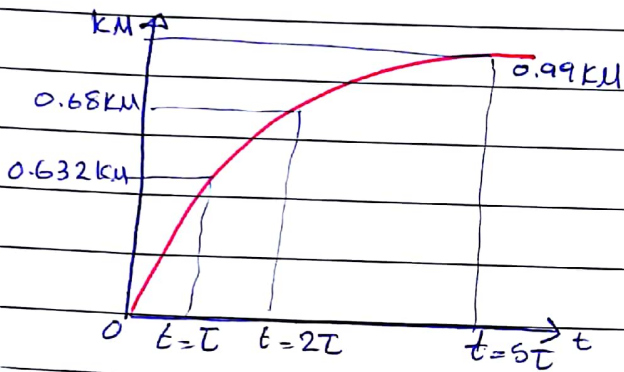


$T \rightarrow$ dynamic behavior

$K \rightarrow$ steady state value

$$\frac{Y(s)}{X(s)} = \frac{K}{Ts + 1}$$

حوضون الناتج ← K
 حوضون المدام ← $Ts + 1$



τ is a time

$$y(t) = k_M \left[1 - e^{-t/\tau} \right]$$

$$t = T$$

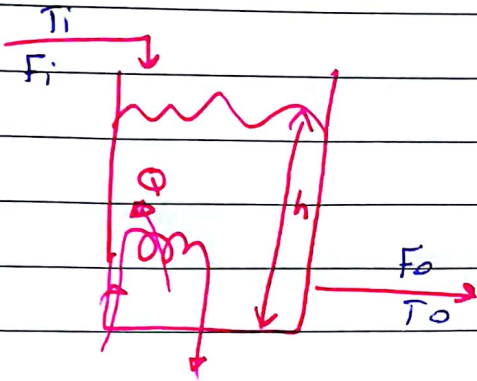
$$\frac{t}{\tau} = 1$$

* response of step change

لما يكون $[t = 1T]$ - هو واحد، لنقله (لاي صفة) الحرف صفة J System
من عرجية .

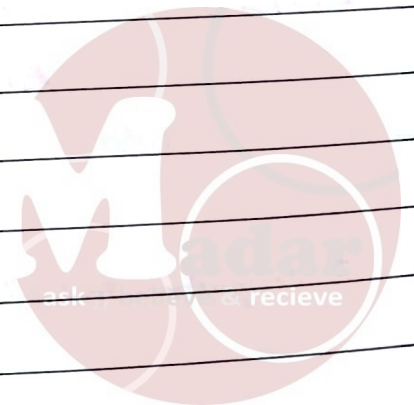
First order system is linear system.

* response to steady state at time $5T$



$$AR \frac{dh}{dt} + h = R F_i$$

$$G(s) = \frac{h(s)}{F_i(s)} = \frac{R}{ARs+1} = \frac{k}{Ts+1}$$



Second order system.

its a function described by 2nd order differential equation.

$$a_0 \frac{d^2 y(t)}{dt^2} + a_1 \frac{dy(t)}{dt} + a_2 y(t) = b x(t).$$

laplace transform

transfer Function

$$a_0 [s^2 y(s) + s y(0) - y'(0)] + a_1 [s y(s) - y(0)] + a_2 y(s) = b x(s)$$

$$a_0 s^2 y(s) + a_1 s y(s) + a_2 y(s) = b x(s)$$

$$y(s) \left[\frac{a_0}{a_2} s^2 + \frac{a_1}{a_2} s + 1 \right] = \frac{b}{a_2} x(s)$$

$G(s) = \frac{y(s)}{x(s)} = \frac{b/a_2}{\frac{a_0}{a_2} s^2 + \frac{a_1}{a_2} s + 1}$	Standard Form of second order system.
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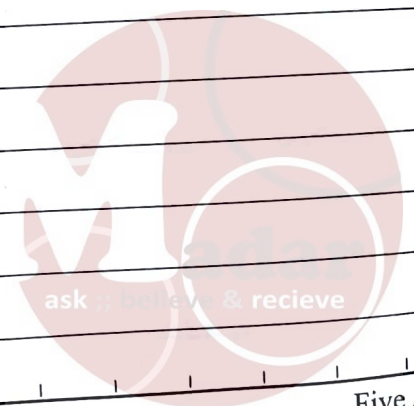
system 1st order 2nd order all, as transfer function

$$G(s) = \frac{y(s)}{x(s)} = \frac{k}{T^2 s^2 + 2 \xi T s + 1}$$

$k \rightarrow$ steady state gain

$T \rightarrow$ time constant

$\xi \rightarrow$ damping factor



* Second order is identified by three parameters,

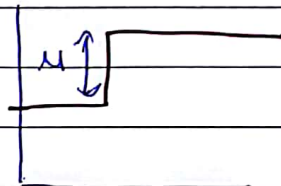
* Final value theorem $\rightarrow$ Final value of the system depends on (k) just

* Transient response depends on (τ)

$$\frac{Y(s)}{X(s)} = \frac{k}{\tau^2 s^2 + 2\zeta\tau s + 1}$$

$$Y(s) = \frac{k}{\tau^2 s^2 + 2\zeta\tau s + 1} \cdot X(s)$$

$$Y(s) = \frac{k}{\tau^2 s^2 + 2\zeta\tau s + 1} \cdot \frac{M}{s}$$



Step $\frac{M}{s}$

$$Ay^2 + by + c = 0$$

$$\tau^2 s^2 + 2\zeta\tau s + 1 = 0$$

$$y_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2A}$$

$$s_{1,2} = \frac{-2\zeta\tau \pm \sqrt{4\zeta^2\tau^2 - 4\tau^2}}{2\tau^2}$$

$$s_{1,2} = \frac{-\cancel{2}\zeta\tau \pm \cancel{2}\tau \sqrt{\zeta^2 - 1}}{\cancel{2}\tau^2} \Rightarrow \frac{-\zeta}{\tau} \pm \frac{\sqrt{\zeta^2 - 1}}{\tau}$$

The roots depends on ζ

$\zeta > 1 \rightarrow$ 2 real different roots

$\zeta = 1 \rightarrow$ 2 imaginary roots

$\zeta < 1 \rightarrow$ 2 real equal roots

بالطبع $\rightarrow$ iablace $\rightarrow$ Sin $\rightarrow$ $\frac{1}{s^2 + 1}$
(cos)

$$y(t) = \dots \sin, \cos$$

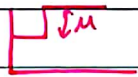
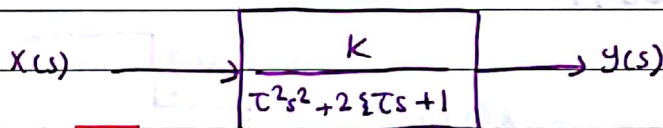
$\zeta < 1 \rightarrow$ oscillation response, $\zeta > 1 \rightarrow$ no oscillation response

$$G(s) = \frac{k}{\tau^2 s^2 + 2\zeta\tau s + 1}$$

$0 < \zeta < 1$ under damped (response).

$\zeta = 1$ critically damped

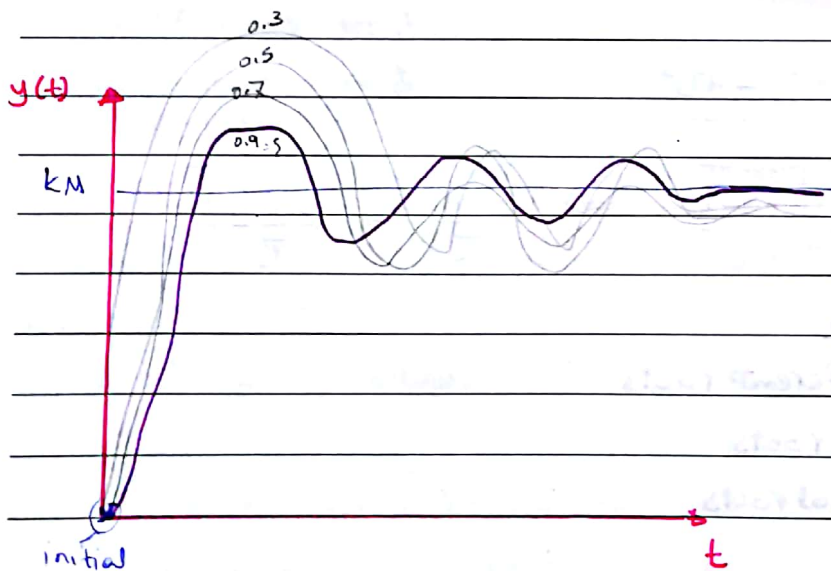
$\zeta > 1$ over damped



$$X(s) = \frac{M}{s}$$

$$Y(s) = \frac{k}{\tau^2 s^2 + 2\zeta\tau s + 1} \cdot \frac{M}{s}$$

$$Y(t) = \mathcal{L}^{-1} \frac{kM}{s(\tau^2 s^2 + 2\zeta\tau s + 1)}$$



$y(t)$ is the output in the deviation form.

$$\begin{aligned} y(t) &= \lim_{s \rightarrow 0} s Y(s) \\ &= \lim_{s \rightarrow 0} \frac{s kM}{s(\tau^2 s^2 + 2\zeta\tau s + 1)} \\ &= kM \end{aligned}$$

response $\zeta < 1$

$$y(t) = \dots \text{ (oscillation)} \dots$$

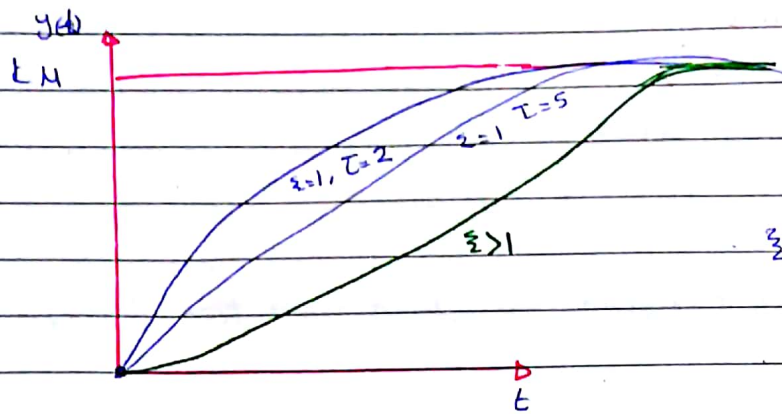
$$t \quad y(t)$$

oscillation //

popular, just

ask, relieve

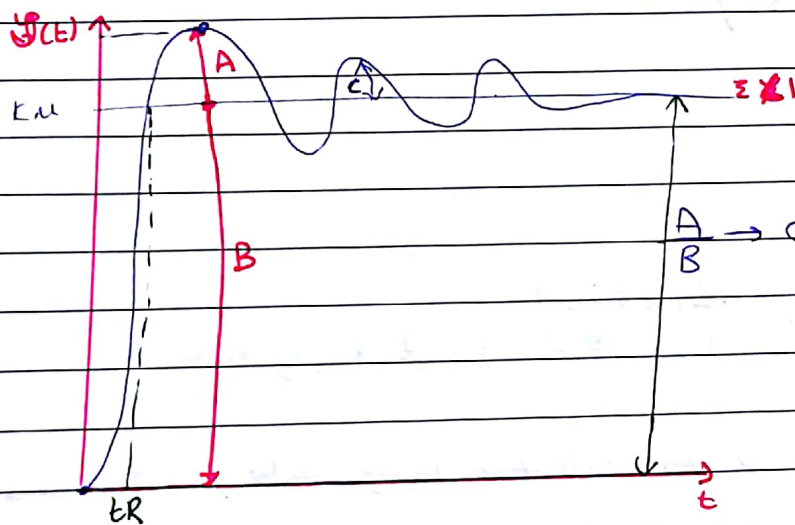
Second order



$\uparrow \zeta \rightarrow$ response is slower
 ζ is nature of response

K is final value
 ζ, T are parameters

maximum deviation, frequency of oscillation, period
 From steady state



A $\rightarrow$ overshoot

B $\rightarrow$ steady state

$$y(t) = \dots$$

$$\frac{dy}{dt} = \dots$$

$$\frac{dy}{dt} = 0 \rightarrow \text{maximum (t)} \text{ or minimum}$$

maximum of oscillation



$$\# \text{Overshoot} = \exp\left(\frac{-\pi \xi}{\sqrt{1-\xi^2}}\right)$$

The only parameter which affects is ξ

$k, T \rightarrow$ not affect

- # Overshoot gives the maximum deviation from the steady state.

$\frac{C}{A}$: (decay ratio)

(to the rate at which the oscillation is disappeared). oscillation / regular

$$D.R = \exp\left(\frac{-2\pi \xi}{\sqrt{1-\xi^2}}\right) \rightarrow \text{over shoot}$$

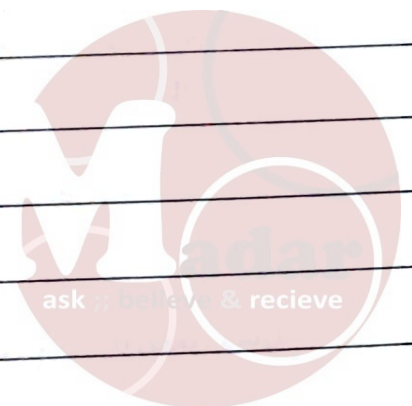
$$D.R = (0.5)^2$$

Settling time :- steady state. الوقت المستقر

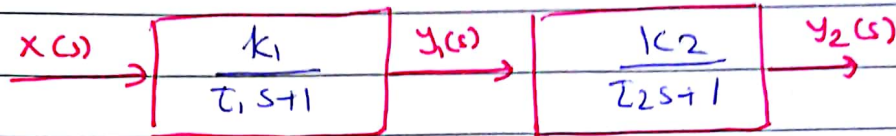
time at $\pm 5\%$ of the final steady state

Risetime : time required to reach the steady state first time

(initial response) الاستجابة الأولية



!! Second order system due to 2 tanks in series.

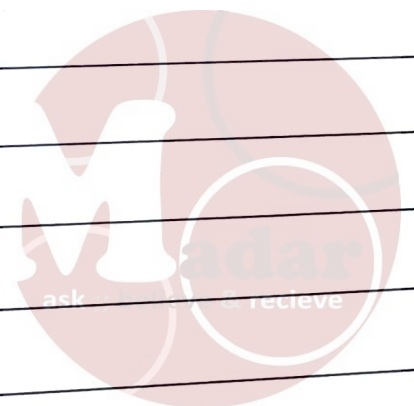


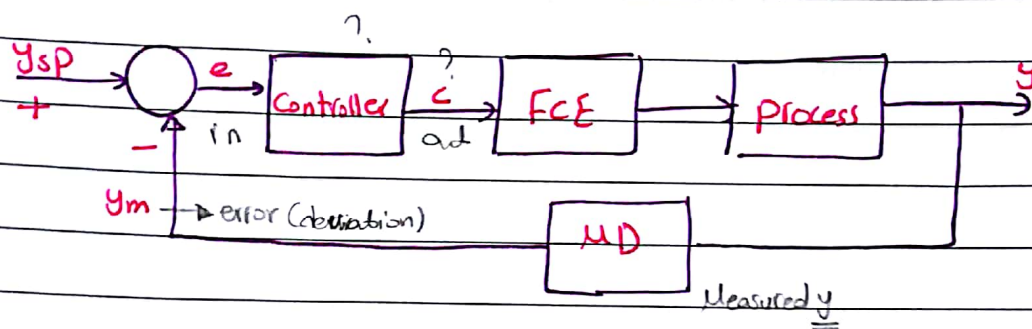
$$\frac{y_1}{x} = \frac{k_1}{\tau_1 s + 1}$$

$$\frac{y_2}{y_1} = \frac{k_2}{\tau_2 s + 1}$$

$$\frac{y_1}{x} \times \frac{y_2}{y_1} \Rightarrow \frac{k_1}{\tau_1 s + 1} \times \frac{k_2}{\tau_2 s + 1}$$

$$\Rightarrow \frac{k_1 k_2}{\tau_1 \tau_2 s^2 + (\tau_1 + \tau_2) s + 1}$$





Types of controller :-

based on signal :-
 - Electrical ----- Electrical signal
 - Pneumatic ----- pneumatic signal

based on Action - Model of the Controller

II Proportion controller

out of C = $K_c e_{in}$ ----- deviation Form $C_{ss} = 0$

$C = K_c e + C_{ss}$ ----- non deviation Form

$$C(s) = K_c e(s)$$

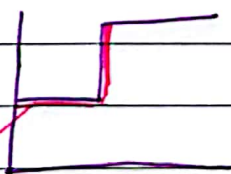
$$G_c(s) = \frac{C(s)}{e(s)} = K_c$$

no dynamics, no transient behavior

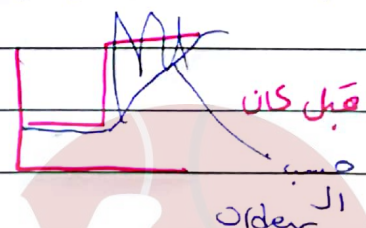
polynomial is zero order

Zero order

initial steady state
 به حالت پایداری

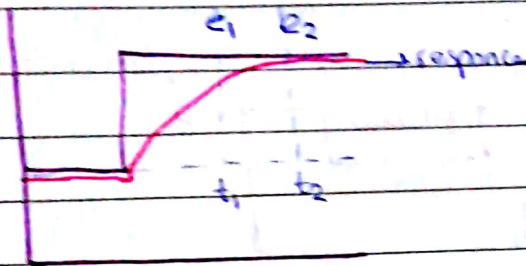


بدون دینامیک و رفتار گذری



Simple, Fast, cheap

ask : help & recieve



Steady state deviation between
Setpoint & measured = 0

القيمة المقاسة (measured) والقيمة المطلوبة (setpoint) هما نفس الشيء (deviation, error) في

if at time $t_1 \Rightarrow e_1$ & $t_2 \Rightarrow e_2$ & $e_1 = e_2$

$$C_1 = K_c e_1$$

$$C_2 = K_c e_2$$

Final s.s.

deviation بين القيمة المقاسة
Steady state error = offset

if $e_1 = e_2$ then $C_1 = C_2$ at this moment the Controller is
stuck

why?

you can't $\rightarrow$ to analyze
بأنفسه

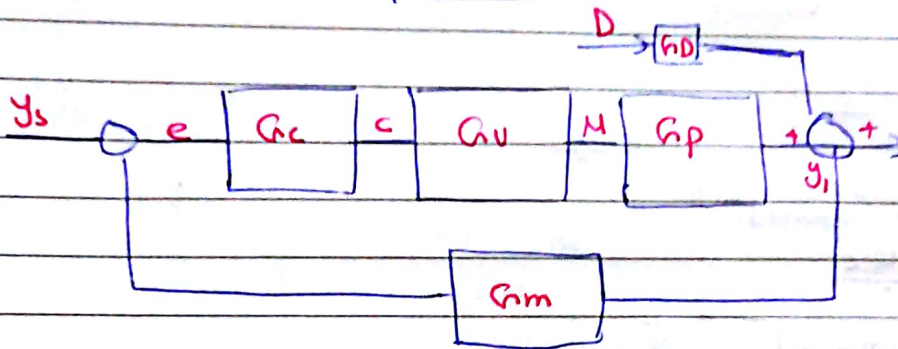
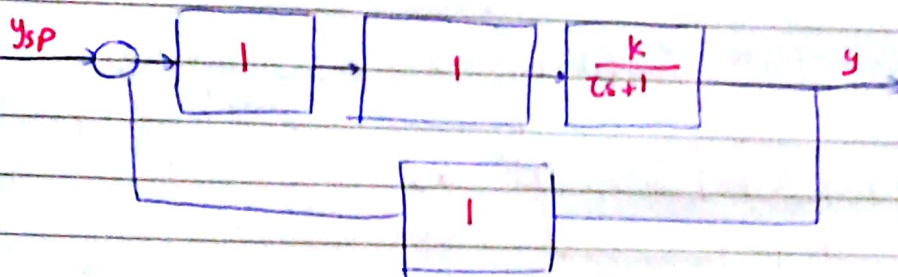
because $\downarrow$ within resolution of the measured value.
the change is

Ex: $y_{m1} = 0.007$
 $y_{m2} = 0.0075$

$\rightarrow$ Small value can't measure by device
القيمة المقاسة لا يمكن قياسها بدقة
- lack detection devices



* closed loop transfer function:-



$$y = y_1 + y_2$$

$$\Rightarrow G_p \times M + G_D \times D$$

$$\Rightarrow G_p (G_u \times C) + G_D \times D$$

$$\Rightarrow G_p (G_u) \cdot G_c \cdot e + G_D \times D$$

$$\Rightarrow G_p G_u G_c [y_{sp} - y_m] + G_D \times D$$

$$\Rightarrow G_p G_u G_c y_{sp} - G_p G_u G_c y_m + G_D \times D$$

$$y + G_p G_u G_c y_m \Rightarrow G_p G_u G_c y_{sp} + G_D \times D \quad \rightarrow y_m = G_m \times y$$

$$y [1 + G_p G_u G_c G_m] = G_p G_u G_c y_{sp} + G_D \times D$$

$$y = \frac{G_c G_u G_p}{1 + G_u G_c G_p G_m} y_{sp} + \frac{G_D}{1 + G_c G_u G_p G_m} D \quad \text{closed loop transfer function}$$

$$1 + G_c G_u G_p G_m = 0$$

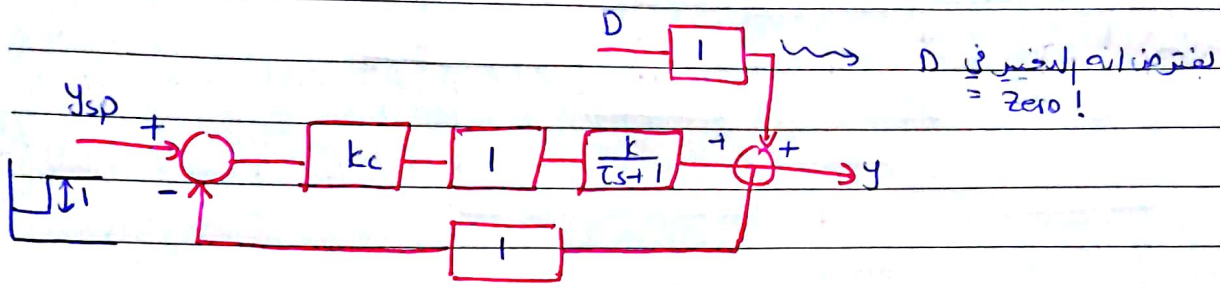
Characteristic equation
Forward path of the system.

(Characteristic eq) of the system

closed loop transient response

(P) controller :-

$$G(s) = K_c$$



$$y = \frac{K_c [1] \left[\frac{k}{Ts+1} \right]}{1 + K_c [1] \left[\frac{k}{Ts+1} \right] [1]} \times \frac{1}{s}$$

مخرج النظام ←

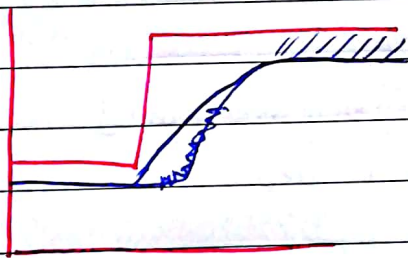
$$y = \frac{\frac{K_c k}{Ts+1}}{\frac{Ts+1 + K_c k}{Ts+1}} \times \frac{1}{s}$$

صافي (1 + Kck)

$$y = \frac{K_c k / (1 + Kck)}{\frac{Ts}{Kck} + 1} \times \frac{1}{s} \rightarrow$$

First order system
but with
smaller time
constant

((Time constants loop)) في ال
((time constant process)) ال



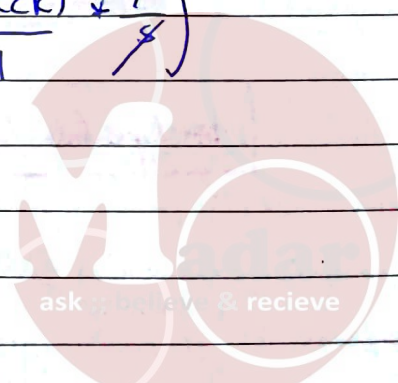
$$\text{offset} = \text{New steady state} - y(t)$$

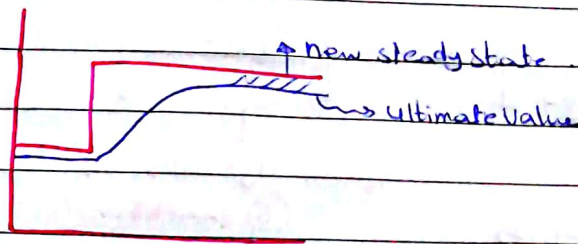
ultimate value of the response

$$y(t) \rightarrow \lim_{s \rightarrow 0} s Y(s) \rightarrow \lim_{s \rightarrow 0} s \cdot \left(\frac{K_c k / (1 + Kck)}{\frac{Ts}{Kck} + 1} \times \frac{1}{s} \right)$$

$$\rightarrow \frac{K_c k / (1 + Kck)}{1} =$$

$$y(t) = \frac{K_c k}{1 + Kck}$$





$$\text{offset} = 1 - \frac{k_c k}{1 + k_c k} \Rightarrow \frac{1 + k_c k - k_c k}{1 + k_c k}$$

$$\text{offset} = \frac{1}{1 + k_c k}$$

$$\text{offset} \propto \frac{1}{k_c}$$

offset $\propto \frac{1}{k_c}$ (offset) $\propto \frac{1}{k_c}$
Steady state $\propto \frac{1}{k_c}$

unstable. $\frac{1}{k_c} \rightarrow \infty$ $k_c \rightarrow 0$ $\frac{1}{k_c} \rightarrow \infty$

!! Zero-offset $\rightarrow$ $k_c \rightarrow \infty$ $\frac{1}{k_c} \rightarrow 0$

* Proportional and Integral controller (PI):-



instant error $\rightarrow$ $e(t)$
Cumulative error $\rightarrow$ $\int e(t) dt$
Controller $\rightarrow$ (integral element) $\rightarrow$ $\int e(t) dt$

$$C = k_c e + \frac{k_c}{T_I} \int_0^{\infty} e(t) dt + \bar{C}$$

2 parameters (k_c, T_I)
signal at S.S.

$\rightarrow$ deviation form:- $C = k_c e + \frac{k_c}{T_I} \int_0^{\infty} e(t) dt$

$$C(s) = k_c e(s) + \frac{k_c}{T_I} \frac{1}{s} e(s) \Rightarrow C(s) = k_c \left[1 + \frac{1}{T_I s} \right] e(s)$$

ask & recieve

$$G(s) = \frac{C(s)}{E(s)} = K_c \left[1 + \frac{1}{T_I s} \right] \Rightarrow K_c \left[\frac{T_I s + 1}{T_I s} \right]$$

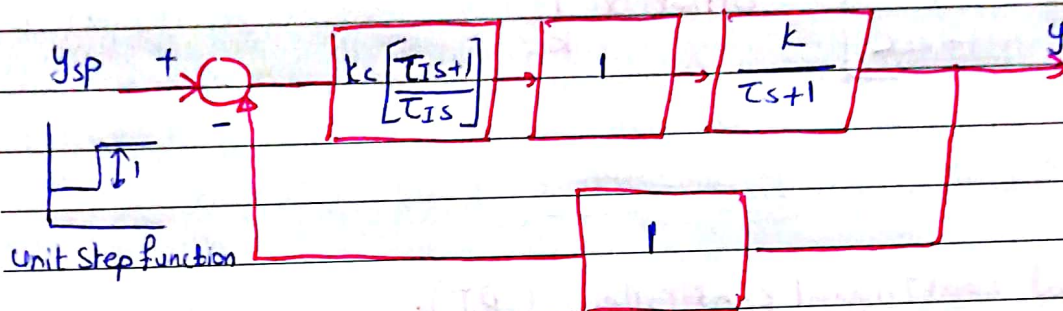
by adding dynamics

(S) derivative

④ we use (PI) to eliminate the offset

response

P controller



$$Y(s) = \frac{K_c \left[\frac{T_I s + 1}{T_I s} \right] [1] \left[\frac{k}{T_s + 1} \right] \times \frac{1}{s}}{1 + K_c \left[\frac{T_I s + 1}{T_I s} \right] [1] \left[\frac{k}{T_s + 1} \right] [1]}$$

$$Y(s) = \frac{K_c k (T_I s + 1)}{(T_I s)(T_s + 1) + K_c k (T_s + 1)} \times \frac{1}{s}$$

First order in dynamics, 2nd order
oscillation free system

$$y(t) = \lim_{s \rightarrow 0} s Y(s) \Rightarrow \lim_{s \rightarrow 0} \frac{K_c k (T_I s + 1)}{T_I s (T_s + 1) + K_c k (T_s + 1)} \times \frac{1}{s}$$

$$\Rightarrow \frac{K_c k}{K_c k} = 1$$

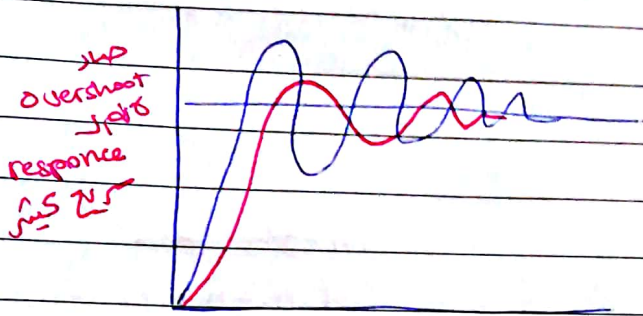
$$\text{offset} = 1 - 1 = 0$$

we add the integral term to eliminate the offset

ask

recieve

the problem on PI controller → introduce oscillation

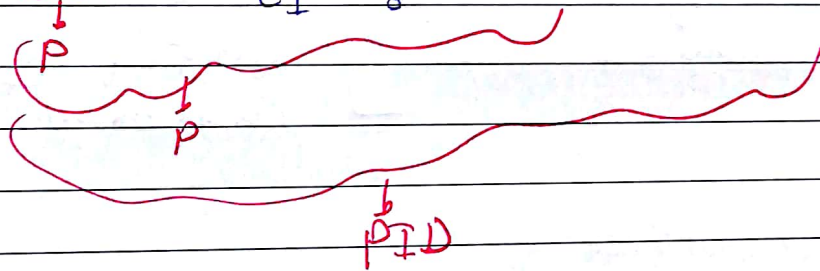


لا يطلع على صافي الخطأ
فقط الخطأ اللحظي

(P) → instant error
(PI) → cumulative error

PID :- proportional Integral derivative Controller

$$C = k_c e + \frac{k_c}{T_I} \int_0^{\infty} e(t) dt + k_c T_D \frac{de(t)}{dt}$$



to reduce the oscillation caused by Integration term.
It's a predictive element!

في النظام المتحكم فيه، إذا كان هناك تذبذب في إشارة الخطأ، فإن هذا يشير إلى أن النظام غير مستقر أو أن هناك مشكلة في التصميم.

في النظام المتحكم فيه، إذا كان هناك تذبذب في إشارة الخطأ، فإن هذا يشير إلى أن النظام غير مستقر أو أن هناك مشكلة في التصميم.

$$\frac{C(s)}{e(s)} = k_c \left[1 + \frac{1}{T_I s} + T_D s \right]$$

practical
Applicable PID

$$G(s) = \frac{C(s)}{e(s)} = k_c \left[\frac{T_D T_I s^2 + T_I s + 1}{T_I s} \right] \times \left[\frac{1}{\lambda s + 1} \right] \rightarrow \text{filter}$$

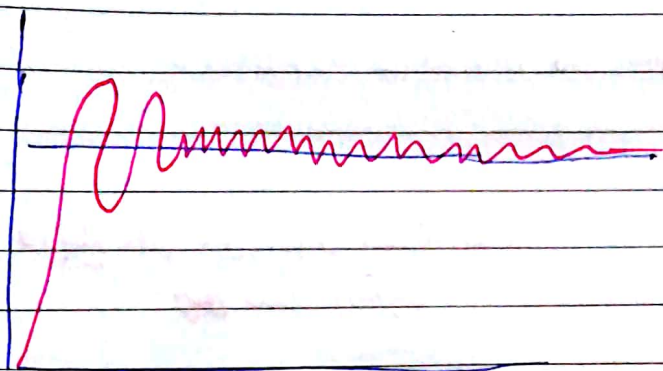
3 parameters

(predicting capability)

هو النظام المتحكم فيه، الذي يمكنه التنبؤ بالخطأ المستقبلي، وبالتالي يمكنه تعديل إشارة التحكم مسبقاً، مما يقلل من التذبذب في إشارة الخطأ.

physically realizable
(unilateral controller)

Five Apple



noisy signal
(PID) is sensitive

$$C = K_c e(t) + \frac{K_c}{\tau_I} \int e(t) dt + \tau_D \frac{de}{dt}$$

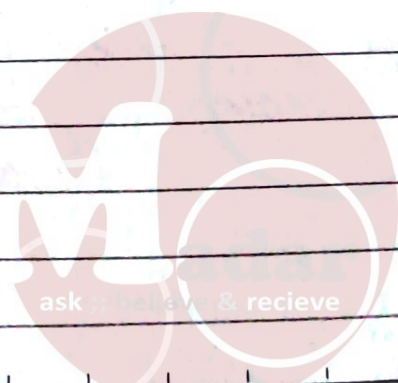
- error + error is now

in the case
of high frequency
oscillation

oscillation driving the controller
not element the oscillation

we can't deal of
high frequency noise.
(oscillation).

(PI) is not a derivative

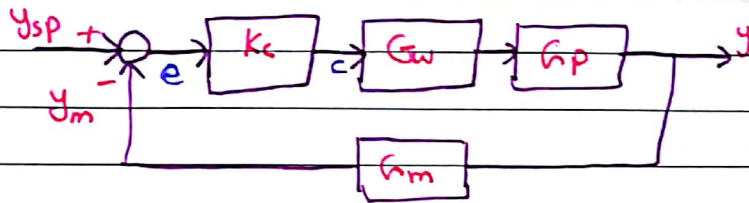


Control Mode :-

how it's acting :-

→ Direct mode

→ Reverse mode



* Direct mode :-

If the measured controlled variable increased and the output of the Controller increased, then the controller in direct mode.

$y_m \uparrow, c \uparrow \rightarrow \text{direct}$

How to set the controller in the direct mode? put K_c less than zero

$$c = (K_c) [y_{sp} - y_m]$$

with y_{sp} is $+ve$ and y_m is $-ve$

input $\rightarrow$ Gain $\rightarrow$ output

$$\text{Gain} = \frac{\Delta \text{output}}{\Delta \text{input}}$$

$$K_c < 0$$

* Reverse mode :-

If the measured controlled variable increased and the output of the Controller decreased, then the controller in reverse mode.

$y_m \uparrow, c \downarrow \rightarrow \text{reverse}$

How to set the controller in the direct mode

$$c = (K_c) [y_{sp} - y_m]$$

with y_{sp} is $+ve$ and y_m is $-ve$

$$K_c > 0$$

ask & receive

Five Apple

Control valve

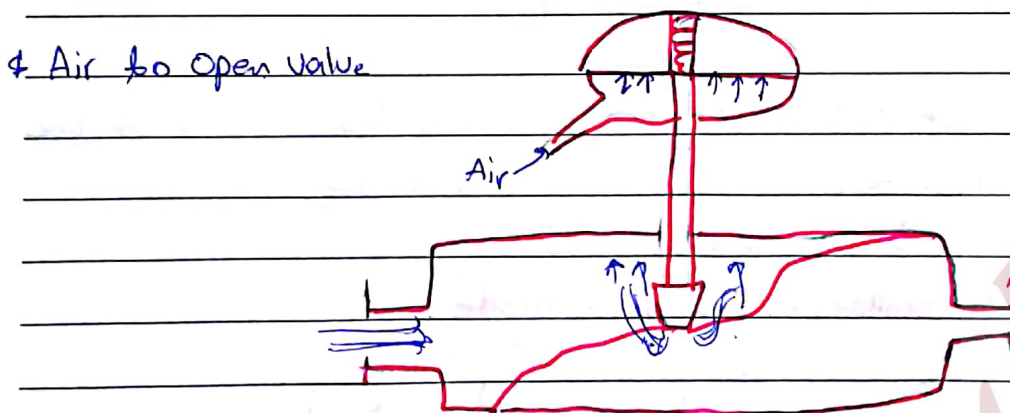
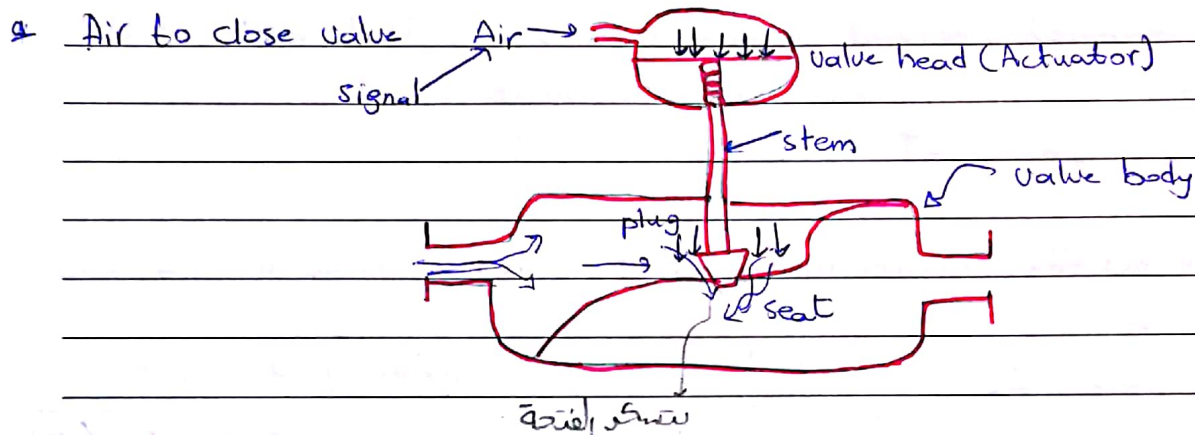
⊛ To have synchronization between the controller & the valve:-



- Air to open valve (Fail close)
- Air to close valve (Fail open) } *Signal for safety of the process*

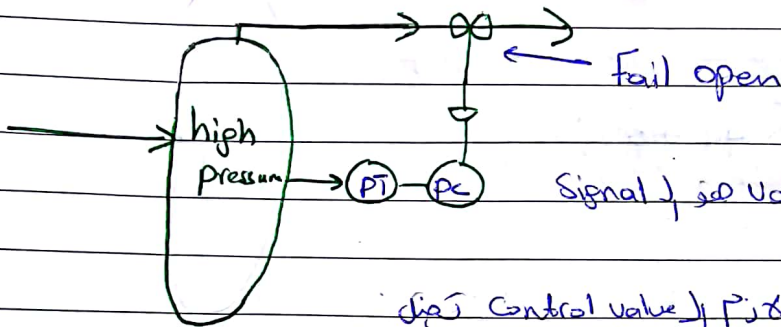
→ Pneumatic valve (Pneumatic signal : Compressed Air)

→ Electric valve



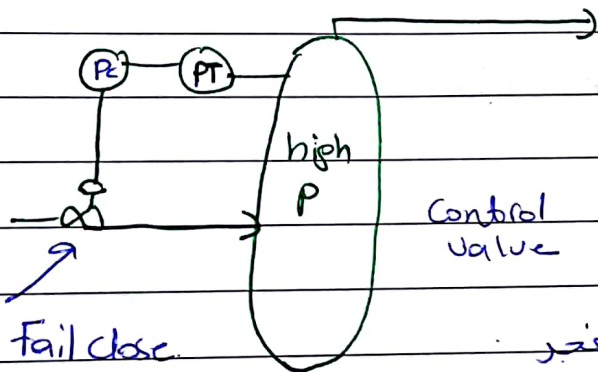
why Fail open ?
Fail close :

↳ safety



Signal value of the process

إذا زاد Signal ← PC في Control value
موجة كذا كانت مسرر زحيز في pressure
open في safety في open

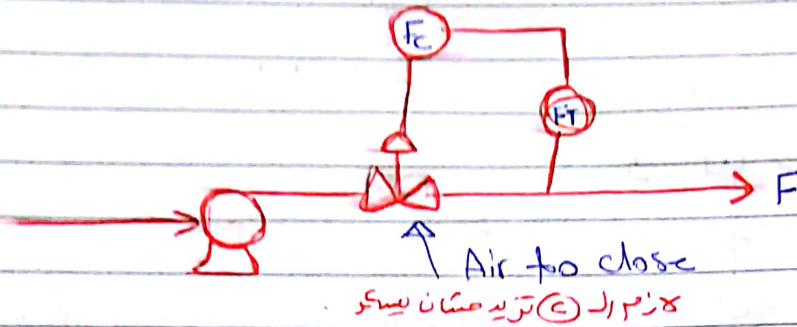


إذا زاد Signal ← PC في Control value

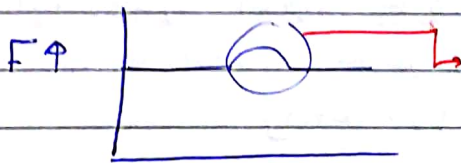
إذا زاد Signal ← PC في Control value
Close في safety في close



Is it direct or Reverse ?



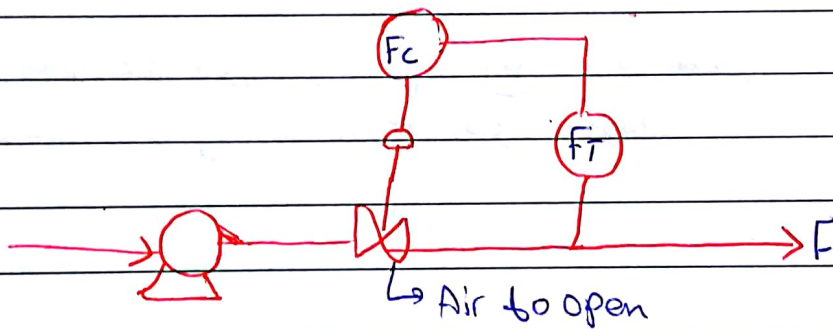
Control variable: Flow



مکان یسر
قیمة آزمایش
Signal
تریه

$c \uparrow \rightarrow y_m(F \uparrow)$

(Direct) مکان یسر



لایزیدیل Flow بوسیله القیة آزمایش یسر
بوسیله آزمایش (ت) نقل مکان یسر

$\downarrow c \uparrow y_m \rightarrow$

Reverse

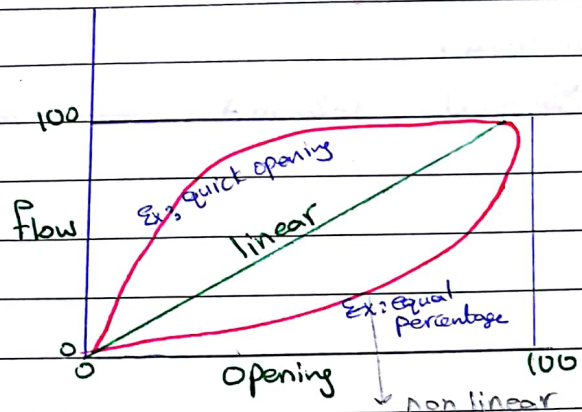
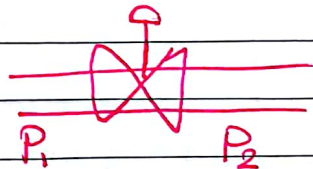
* Flow characteristics of the valve :-

Valve opening flow Q_v

Valve closing flow Q_{vc}

$$F = C_v f(x) \sqrt{\frac{\Delta P}{\rho}}$$

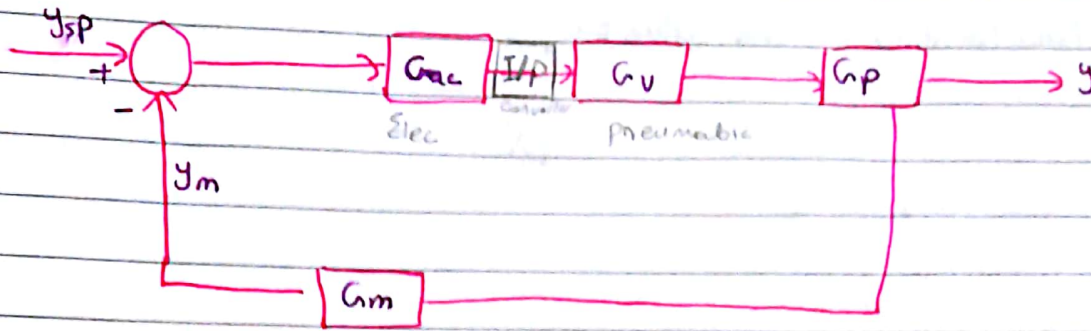
C_v → const
 Represent mechanical design of the valve
 $f(x)$ → pressure drop across the valve ($P_1 - P_2$)
 ρ → density of the fluid



When I choose linear, quick opening or equal percentage?

للإختيار





Control signals .

① Electrical 4-20 mA $\longrightarrow$ Air to open $\leftarrow$ Gu
 4 = Signal completely closed
 20 = Signal completely open

② pneumatic 3-15 psi .

if Gu $\rightarrow$ Air to open

Signal = 3 $\rightarrow$ completely closed

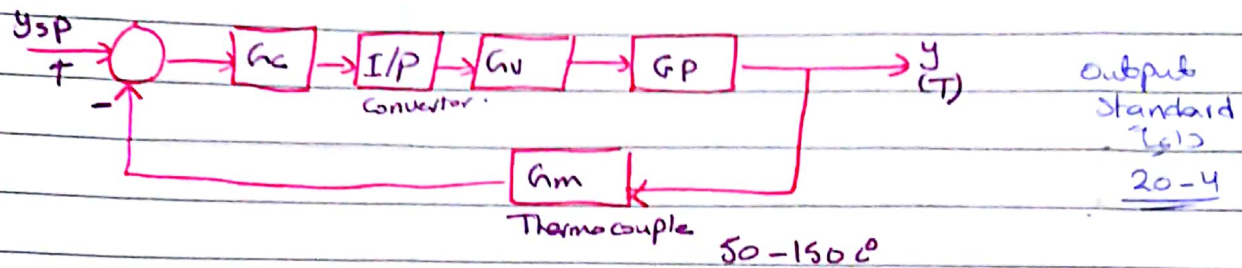
Signal = 15 $\rightarrow$ completely opened

pneumatic Gu 1,2 elect $\leftarrow$ Gu $\rightarrow$ I/P Converter $\rightarrow$ Gu
 $G = \frac{12}{16}$ $\leftarrow$ I/P $\rightarrow$ Gu $\rightarrow$ P/I $\rightarrow$ Gu
 $G = \frac{16}{12}$ $\leftarrow$ P/I $\rightarrow$ Gu

Thermo Couple $\rightarrow$ electrical $\rightarrow$ Gu
 output J1

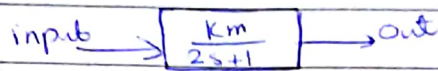


First order system has a time const = 2 & input range of 50-150°C



Gain = ??

$$\text{Gain} = \frac{\Delta \text{Output}}{\Delta \text{Input}}$$



$$= \frac{20-4}{150-50} = \frac{16}{100} = 0.16$$

* Design of control system.

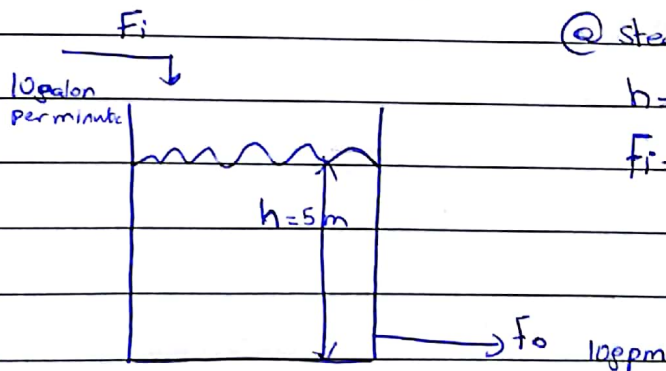
- Control loop configuration.
- Dynamics of the system.
- Controller type : P, PI, PID. k_c, t_i, t_d
- Control valves

* controller mode

* Air to open, Air to close

* linear, quick opening, Equal percentage.

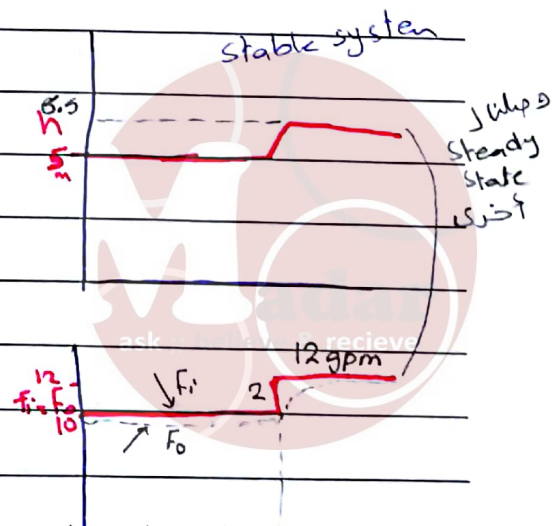
① stability of control system.



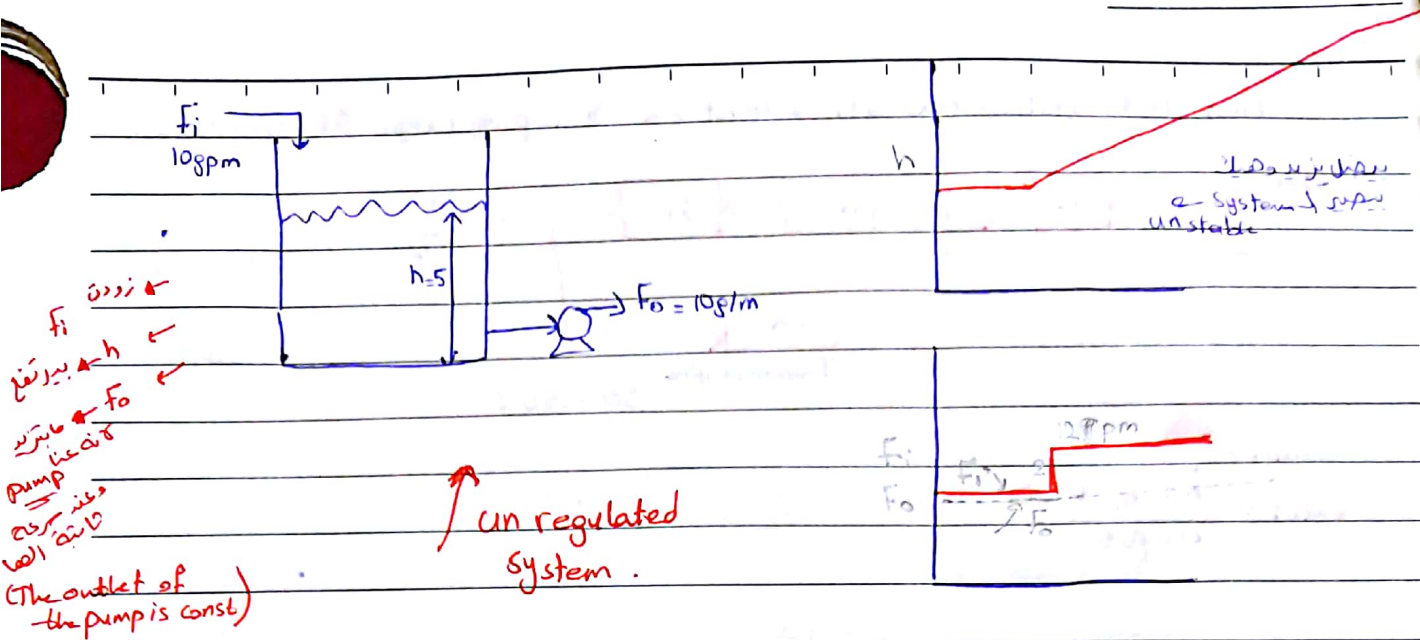
@ steady state.

$h = \text{const}$

$$F_i = 2 F_o$$



→ self regulated system



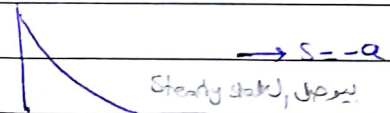
اگر ایک ایسی کاپی ہو جس کا input bounded ہو اور output unbounded ہو تو یہ system unstable ہے۔
 Output unbounded → unstable

- If the response of a system to bounded Input is bounded, Then the system is stable.
- If the response of a system to bounded Input is unbounded, Then the system is unstable.

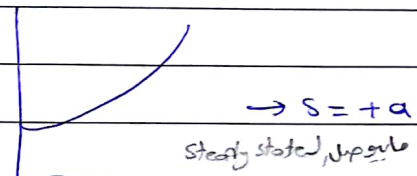
$$y = \frac{G_c G_v G_p}{1 + G_c G_v G_p G_m} y_{sp} + \frac{G_D}{1 + G_c G_v G_p G_m} D$$

$$0 = 1 + G_c G_v G_p G_m \quad \text{characteristic eq.} \quad \text{اولی شرط پایداری (Stability)}$$

(A) $\rightarrow y(s) = \frac{1}{s+a}, \quad y(t) = \frac{-ae^{-at}}{e}$



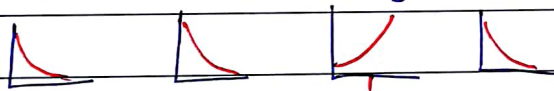
(B) $\rightarrow y(s) = \frac{1}{s-a}, \quad y(t) = \frac{ae^{at}}{e}$



* Example.

$$y(s) = \frac{1}{(s+a_1)(s+a_2)(s+a_3)(s+a_4)}$$

$$\Rightarrow \frac{C_1}{s+a_1} + \frac{C_2}{s+a_2} + \frac{C_3}{s+a_3} + \frac{C_4}{s+a_4}$$



محدود می شود
 ∞

⊕ در صورتی که تمام پoles پایدار باشند یعنی $\lim_{t \rightarrow \infty} y(t) = 0$

و اگر یکی از پoles ناپایدار باشد $\lim_{t \rightarrow \infty} y(t) = \infty$

پoles ناپایدار $\lim_{t \rightarrow \infty} y(t) = \infty$

System goes to instability.

Stable System, پایداری

(A) $\rightarrow$ (-ve) roots, p, δ

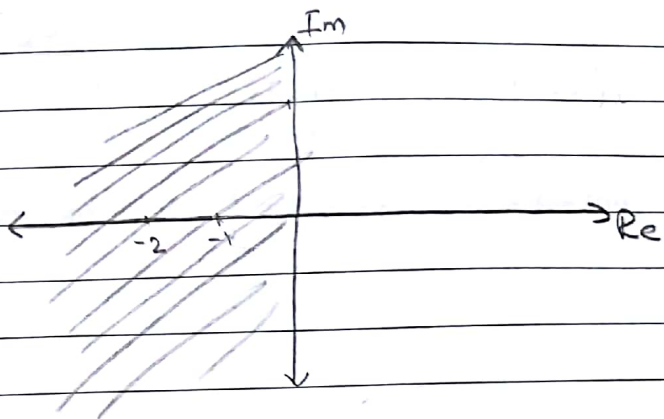
ask & recieve

4 Stability Analysis.

1) Root Locus Method

$$1 + G_c G_p G_u G_m = 0$$

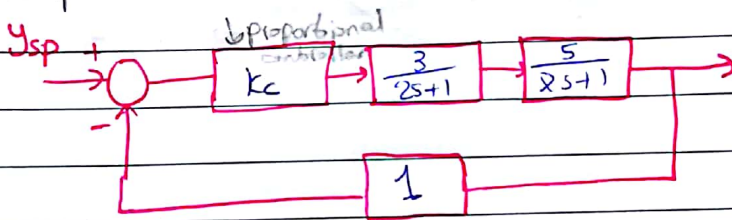
$$a_n s^n + a_{n-1} s^{n-1} + \dots = 0$$



If All Roots or the Real part of the root are (-ve), then the process is stable.

Examples: → 1) $-3+5j$
2) $-1, -2$

Simple.



characteristic eq: - $1 + K_c \left[\frac{3}{2s+1} \right] \left[\frac{5}{2s+1} \right] [1] = 0$

$$(2s+1)(2s+1) + 15 K_c = 0$$

$$4s^2 + 4s + 1 + 15 K_c = 0$$

القيمة الحرجة لـ Kc هي القيمة التي تجعل النظام مستقرًا

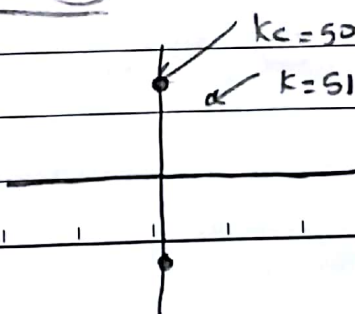
Kc	s1	s2	ملاحظات
0	-	-	النظام مستقر
1	-	-	النظام مستقر
10	-	-	النظام مستقر
15	-	-	النظام مستقر
30	-	-	النظام مستقر

unstable (النظام غير مستقر)

line Kc = 50 will be critical

critical (critical) stable

roots +ve



Five Apple

میست چیکار کنیم (T) و (K) پارامتر میست چیکار کنیم (PT) چیکار کنیم
 کنترلر

2- Routh - Hurwitz Array

Test I:- ① Write the ch. Equation as a polynomial with decreasing power
 P.S $a_0 s^n + a_1 s^{n-1} + a_2 s^{n-2} + a_3 s^{n-3} + \dots + a_n s^{n-n} = 0$

② let a_0 be +ve.

③ if one or more of coefficients is / are -ve $\Rightarrow$ System unstable.

$a_0, a_1, a_2, \dots$

④ if all the coefficients are +ve $\Rightarrow$ Go to test (two) not enough to judge.

Test (II)

From the R-H Array

	a_0	a_2	a_4	a_6	... even
	a_1	a_3	a_5	a_7	... odd
	A_1	A_2	A_3	... 0	... just give up
	B_1	B_2	0		

$$A_1 = \frac{a_1 \times a_2 - a_0 \times a_3}{a_1}$$

$$A_2 = \frac{a_1 \times a_4 - a_0 \times a_5}{a_1} \rightarrow \text{check this from Book}$$

$$B_1 = \frac{A_1 \times a_3 - A_2 \times a_1}{A_1}$$

* if all elements in column (1) are positive (stable)

* if one or more elements is negative, the system is unstable

ask & recieve

Five Apple

Example 2

$$8s^3 + 12s^2 + 9s + 1 + K_c = 0$$

	s^3	s^2	s	0
			9	
	12		$1 + K_c$	
	$\frac{12+9-8(1+K_c)}{12}$		0	
	$\frac{12+9-8(1+K_c) + (1+K_c) - 12 \times 0}{12}$		0	
	$\frac{12+9-8(1+K_c)}{12}$			

$$B_1 = 1 + K_c$$

* Conditions for stability should be positive.

$$\frac{12+9-8(1+K_c)}{12} > 0 \rightarrow \frac{12+9}{8} > 1+K_c \rightarrow 18.5 > K_c$$

$$1 + K_c > 0 \rightarrow K_c > -1$$

$$\boxed{-1 < K_c < 18.5}$$

Unstable system is (if) root $\rightarrow$ $0 < K_c < 18.5$
 $s < -2 \leftarrow K_c$

For stability, the range of K_c is $-1 < K_c < 18.5$

ask & recieve

Five Apple

Design of control system.

Stability

Design Criteria (Tuning criteria)

① Simple Criterion

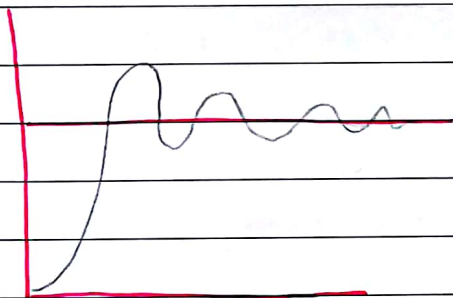
(Overall) J minimization

— one the desired objectives

— one the desired objectives

— O.S

— D.R



$$y = \frac{G_c G_v G_p}{(1 + G_c G_v G_p G_m)} y_{sp} + \frac{G_{au}}{\dots}$$

2nd order system:-

$$T^2 s^2 + 2\zeta T s + 1$$

Overshoot $\propto \zeta$

Overshoot $\propto 20\%$

what's a controller Give me response of overshoot :- ?

Decay Ratio $\frac{1}{4} \rightarrow$ ζ at $\frac{1}{4}$ is 0.25

Controller J at $\frac{1}{4}$ is 0.25

— at T, K_c

• D.R. Give ζ by ζ Controller J at $\frac{1}{4}$ is 0.25

• (oscillating) ζ at $\frac{1}{4}$ is 0.25

* Design a controller which minimizes the overshoot & the rise time?

This controller is impossible because these two conditions are opposite to each other.

Rise time $\leftarrow$ Overshoot J at $\frac{1}{4}$ is 0.25

② Comprehensive criteria :- (Overall) also used

What is the overall objective of the controller?

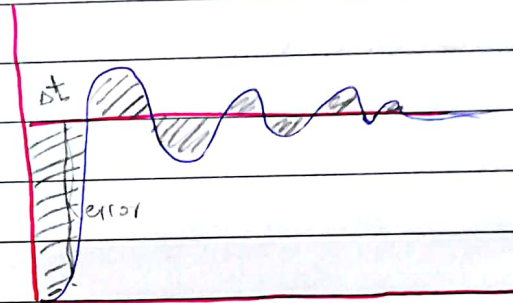
Minimize the deviation from the set point

Comprehensive I, O, WT

2.1 - Integral methods

$$\text{Area} = \int_0^{\infty} e \, dt$$

designer should aim to reduce the area under the error curve
which is $\int_0^{\infty} e \, dt = 0$ (in theory)
and the error should be zero



Error² (Jaccard's index)

Integral of square error (ISE) --- 2.1.1

$$\Rightarrow \int_0^{\infty} e^2 \, dt$$

error fraction is 0.5 (1/2)

0.5 → 0.25 (1/4)

0.5 → 0.25 (1/4)

Integral Absolute error (IAE) --- 2.1.2

$$\Rightarrow \int_0^{\infty} |e| \, dt$$

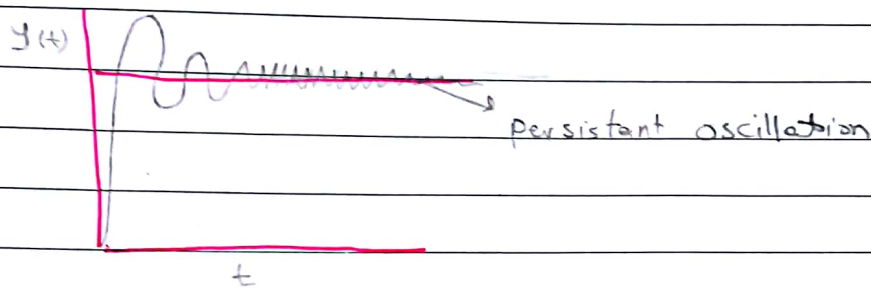
if I expect large error

its better to use ISE

if I expect small error

its better to use IAE



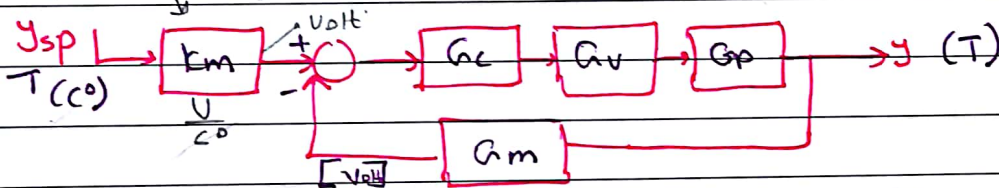


⊗ Integration of line & Absolute value of the error ~~ITAE~~ (ITAE)

$$\int_0^{\infty} t |e| dt \quad \dots \quad 2.1.3$$

2.2) Direct synthesis method. Ratio $\frac{\text{output (deviation)}}{\text{input (deviation)}}$ between setpoint & measured.

as a whole process $\leftarrow$ will



$$k_m = \frac{\text{Vout}}{c^0}$$

• $\frac{\text{Vout}}{c^0}$ is the gain of the process (km) at c^0

$$\frac{y}{y_{sp}} = \frac{k_m G_c G_u G_p}{1 + G_c G_u G_p G_m}$$

$$\text{let } G_m = k_m$$

$$\text{let } G_m G_u G_p = G$$

$$\frac{y}{y_{sp}} = \frac{G_c G}{1 + G_c G}$$

$$G_c = \frac{1}{G} \left[\frac{y/y_{sp}}{1 - y/y_{sp}} \right]$$



Control system design

→ Simple criteria

→ Comprehensive Criteria

- Integral methods
- Direct synthesis methods

$$G_c = \frac{1}{G} \left[\frac{y/y_{sp}}{1 - y/y_{sp}} \right]$$

y/ysp: performance criteria

صافي احصاء زم ضدّها .

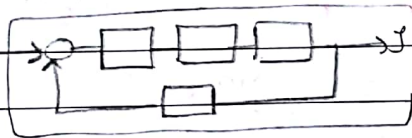
where $G = G_m G_p G_v$.

y/y_{sp}:- 1 → there is no deviation at all
(perfect control)

$$G_c = \frac{1}{G} \left[\frac{1}{1-1} \right] = \infty \rightarrow \text{controller value}$$

perfect situation
its not achievable.

overall dynamics of all control system is zero order



فلازم نزود (order)

$$\frac{y}{y_{sp}} = \frac{1}{\tau_c s + 1}$$

بجمل ازود و اقرب بال (T_c)

↳ design parameter

enable me to achieve or not achieve
the perfect control

$$G_c = \frac{1}{G} \left[\frac{\frac{1}{T_c s + 1}}{1 - \frac{1}{T_c s + 1}} \right]$$

$$G_c = \frac{1}{G} \left[\frac{\frac{1}{T_{cs}+1}}{\frac{T_{cs}+1-1}{T_{cs}+1}} \right] \Rightarrow G_c = \frac{1}{G} \times \frac{1}{T_{cs}}$$

$$G_c = \frac{1}{G} + \frac{1}{T_I s}$$

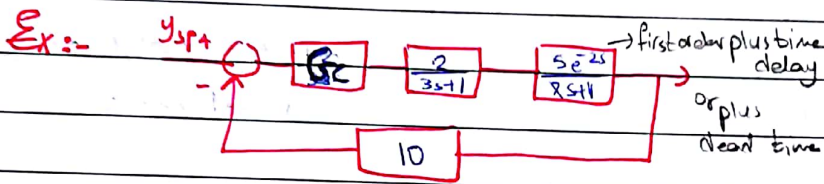
بالاضافة بطلع عندي

وحدة في معادلات

ال Controller

اللي انا احماد واخذناه قبل

$$G_c = K_c \left[\frac{T_I s + 1}{T_I s} \right]$$



في ال process

ال output

ليس في ال constant block

$$\frac{y}{y_{sp}} = \frac{1}{5s+1}$$

في ال system
اللي فوق

في ال system delay

في ال system delay

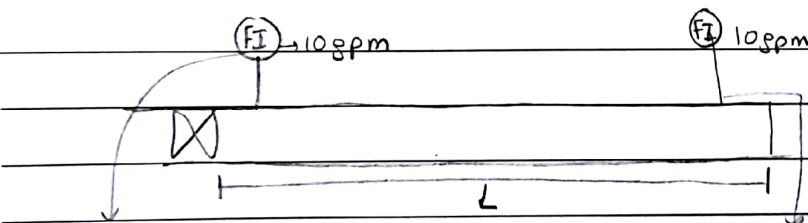
$$\mathcal{L} y(t) = y(s)$$

$$\mathcal{L} y(t-3) = e^{-3s} y(s)$$

$$\frac{y}{y_{sp}} = \frac{e^{-3s}}{5s+1}$$

time delay

there is a delayed response for any reason.



من
بالتفصيل

في ال system delay

$$t = \frac{L}{v} = \frac{L}{v}$$

delay dead time

* Example: $G = \frac{2.7(0.5s - 1)}{2s + 1}$

$\frac{y}{y_{sp}} = \frac{1}{\tau s + 1}$ or $\frac{2s}{\tau s + 1}$ is good for this system.

$G_c = \frac{2s + 1}{2.7(0.5s - 1)} + \frac{1}{\tau s}$
 positive root
 unstable zero

وكل شيء في هذا هو جيد
 لأننا نريد أن يكون
 النظام مستقر

نريد
 أن يكون

the main characteristic of the G

نريد أن يكون

$\frac{y}{y_{sp}} = \frac{(0.5s - 1)}{\tau s + 1}$ zero at $s = 2$
 zero at $s = 2$

$G_c = \frac{2s + 1}{2.7(0.5s - 1)} \times \frac{(0.5s - 1)}{\tau s} = \frac{2s + 1}{2.7 \tau s}$



→ Controller design

Simple Criteria

→ Comprehensive Criteria

* Integral

* Dsm

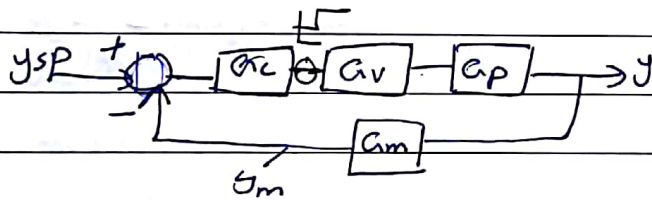
→ Empirical Method

* Cohen-coon

* Ziegler-Nichols

Cohen-coon :-

→ open loop Method



exp. test لاجل

Value J is

فإنه لا يمكن أن يكون إلا واحد

Process J (لأنه واحد)

time Input output (y)

$$G_p = \frac{K_p e^{-\phi s}}{s + 1}$$

Fitting for First order + dead time

K_p, ϕ
 τ_p

البرامتر التي نحتاجها

إذا طبقنا (np) وجدنا 1.05

في هذه الصيغة Formulas

$$PID : K_c = f_1(K_p, T_p, \phi)$$

$$T_I = f_2(K_p, T_p, \phi)$$

$$T_D = f_3(K_p, T_p, \phi)$$

(2) Ziegler-Nichols Method

based on closed-loop test

بعد التجربة وجدنا في هذه

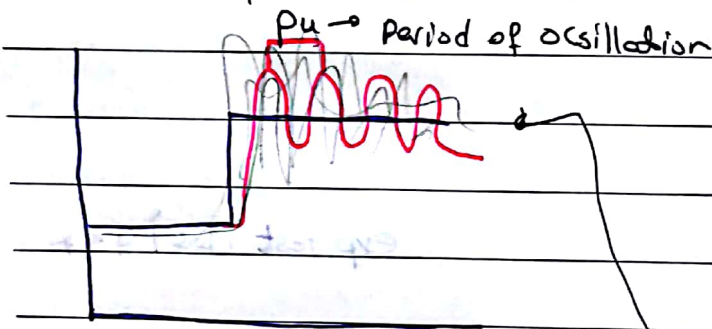
automation

$K_c = G_c$ da p, o cile

as p controller

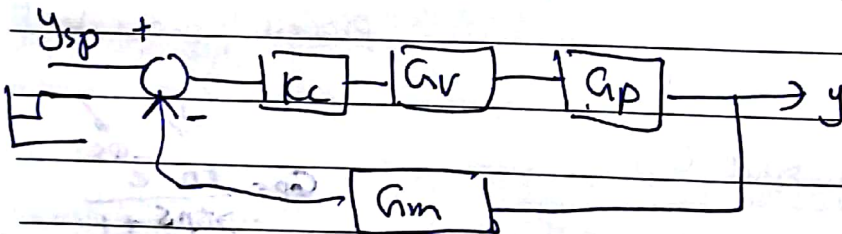
بمقدار K_c قلة

slow response → large offset



بعد أن زدنا في قيمة K_c وانما يتلذذ

(const) response oscillation



→ Continuous Sustained oscillation

K_u (max. response) K_c (the ultimate value)

بما أن K_c لا يتغير استجابة النظام تصبح غير مستقرة unstable

الحل هو أن نزيد من قيمة K_u في النظام حتى نحصل على الاستقرار stability

$$P: K_c = \frac{K_u}{2}$$

$$PI: K_c = \frac{K_u}{2.2}$$

$$PID: K_c = \frac{K_u}{1.2}$$

check!!

$$PI = TI = \frac{P_u}{??}$$

$$ID = TI = \frac{P_u}{??}$$

$$ID = \frac{P_u}{??}$$

Are these numbers acceptable or not, According to Cohen coon or Ziegler?



Cascade controller:- manipulated variable subject to changes, subject to fluctuation.

Cascade // Simple $\rightarrow$ manipulated variable $\rightarrow$ Q_1

to satisfy my original controller

Primary master $\rightarrow$ Secondary Slave

* Features of cascade :-

- ① 2 controller
- ② 2 transmitters
- ③ one control value

$y_1 \rightarrow$ setpoint

Ratio controller $\rightarrow$ ratio between A & B = ratio between setpoints = value before

Wild Flow $\rightarrow$

Outlet flow of reactor

reactor, valve, boiler

wild flow

Ratio

① manipulation ratio

② Division ratio

كل شيء في
الخط
هو
مسيطر عليه

* Selective Control $\leftarrow$ air flow sensors

high low
measuring
pressure

Over ride Control system $\leftarrow$ Controller, Controller, transmitter
Signal

lever or Flow control

(activation) $\leftarrow$
air flow

normal control

For safety or protection

Boiler or Furnace control

steam pressure $\leftarrow$ Control

ratio control

ratio between air & fuel
excess air

$P \downarrow \rightarrow T \downarrow$

analysis

air

Fluctuation

② cascade controller

air

combustion is low

Fuel $\downarrow$ air $\downarrow$

Boiler drum control

Feed ← disturbance →
→ steam p change

P → level →

→ bubble

level 1

بسیار حساس و دقیق

انتخاب (Switch)

کمیته ای (فنی) (و اقل)

بسیار کم (بسیار)

فشار (Controller)

Flow

فشار (و اقل) (و اقل)

evaporator

bubbles

level

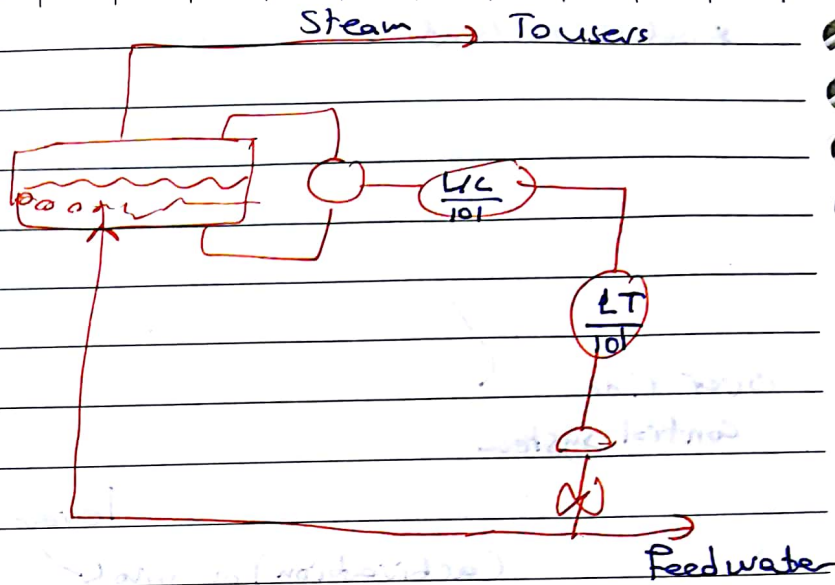
→

over 25°C

disturbance in

Feed forward

control device



وزاد P فویدر

bubble

بسیار حساس و دقیق

Shrink

level

Controller

Feed

bubbles

level

Stream

(droplets water

in steam)

Trip

turbines

