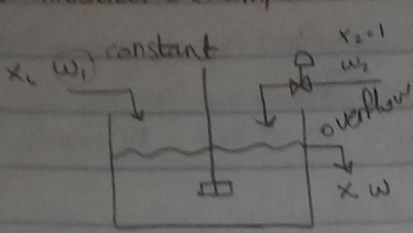


Chapter # 1 : Introduction to process control

1.2 illustrative example - a blending process



inputs x_1, w_1, x_2, w_2

outputs $\times w$

Controlled variable x (from outlets)

manipulated variable w_2 (from inlets)

disturbance variable $\downarrow$ since $x_2 = 1$ w_1 is constant
 x_1

* Design equation assuming steady state operation

① $\omega = \omega_1 + \omega_2$

$$(2) \quad xw = x_1w_1 + x_2w_2 \quad x(w_1 + w_2) = x_1w_1 + x_2w_2 \quad w_1(x_1 - x) + w_2(x_2 - x) = 0$$

$$\Rightarrow w_2 = \frac{w_1 (x - x_1)}{x_2 - x} \quad \text{but } x \text{ must equal the set point } x_{sp} \quad \boxed{w_2 = w_1 \frac{(x_{sp} - x_1)}{(1 - x_{sp})}}$$

we have nominal values to indicate steady state $\bar{w}_2 = \bar{w}_1 \frac{(x_{sp} - \bar{x}_1)}{(1 - x_{sp})}$ (*)

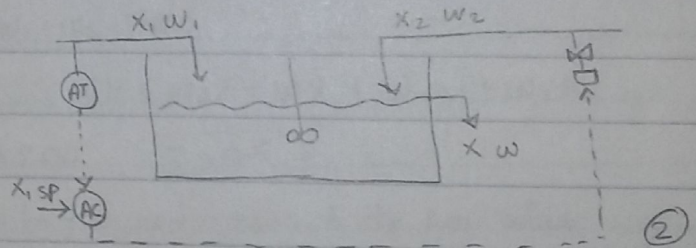
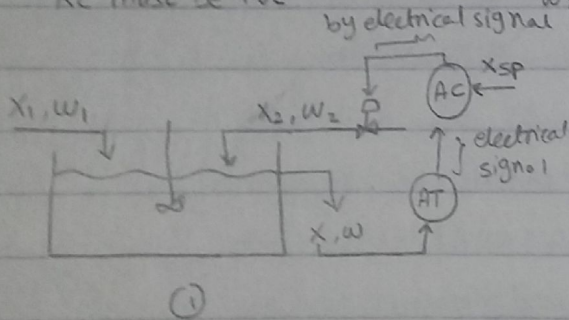
* Methods to control x

① measure x_i & adjust w_1 ② measure x_i & adjust w_2 ③ combine ① & ②

$-(\bar{w}_2 - w_2(t)) = K_c (x_{sp} - x_1(t))$ can be derived from (1) (1) large tank so not to be
 K_c must be +ve $w_2(t) = \bar{w}_2 (x_{sp} - x_1(t))$ affected, but high capital cost.

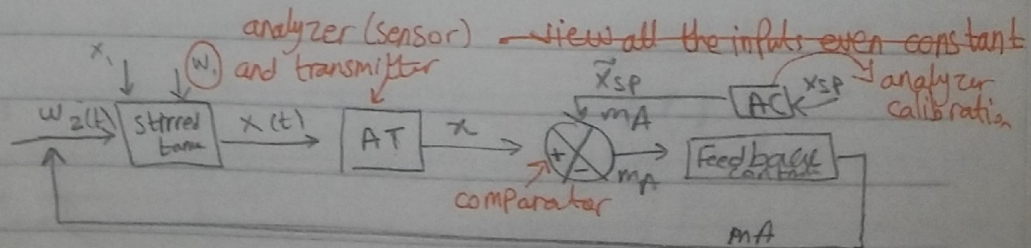
K_c must be +ve

$$W_2(t) = \bar{W}_1 \frac{(X_{SP} - X_1(t))}{(1 - X_{SP})}$$



~~1.4 a more complicated example - a distillation column~~

* Making a block diagram



Look

Ch. 2

2.2.1 Conservation Laws

→ energy conservation law in general

$$\text{rate of energy accumulated} = \text{rate of energy in by convection} - \text{rate of energy out by convection} + \text{? from surr. to system} + \text{work on system by surrounding}$$

• rate of energy accumulated

$$U_{\text{total}} = U_{\text{internal}} + U_{\text{kinetic}} + U_{\text{potential}} \quad \text{neglect } U_{\text{kinetic}} \& U_{\text{potential}}$$

$$U_{\text{total}} = U_{\text{internal}} \quad \text{rate} \quad \frac{dU_{\text{total}}}{dt} = \frac{dU_{\text{internal}}}{dt}$$

• neglect work done on system

$$\text{energy in} - \text{energy out} = -\Delta(\dot{W}\hat{H})$$

$\hat{H}$ = specific either for molar or mass flow rate

$$\frac{dU_{\text{internal}}}{dt} = -\Delta(\dot{W}\hat{H}) + \dot{Q}$$

Chapter #28 Theoretical models of chemical processes

→ Blending process example

mass $\frac{d(V\rho)}{dt} = w_1 + w_2 - w$ (1) overall

$\frac{d(V\rho x)}{dt} = x_1 w_1 + x_2 w_2 - x w$ (2) component

• assuming that the density is constant

$\rho \frac{dV}{dt} = w_1 + w_2 - w$ (*)

$\rho \frac{d(Vx)}{dt} = x_1 w_1 + x_2 w_2 - x w$

• expanding the accumulation term

$\rho x \frac{dV}{dt} + V \rho \frac{dx}{dt} = x_1 w_1 + x_2 w_2 - x w$

Substitute (*) → $\frac{dV}{dt} = \frac{w_1 + w_2 - w}{\rho}$

$x(w_1 + w_2 - w) + V \rho \frac{dx}{dt} = x_1 w_1 + x_2 w_2 - x w$

$\frac{dx}{dt} = \frac{1}{\rho V} (w_1(x_1 - x) + w_2(x_2 - x))$

Now, I have 2 ODE $\frac{dV}{dt} = (w_1 + w_2 - w) / \rho$

$\frac{dx}{dt} = (w_1(x_1 - x) + w_2(x_2 - x)) / \rho V$

Example 2.1 3-

assuming V constant = 2 $\rho = 900 \Rightarrow \frac{dV}{dt} = 0$ $w = w_1 + w_2$

(a) steady-state assuming $w_1 = 500$ $w_2 = 200$ $x_1 = 0.4$ $x_2 = 0.75$ $x?$

$\frac{dx}{dt} = 0$ $w = w_1 + w_2 = 700$

$0 = w_1(x_1 - x) + w_2(x_2 - x)$ $w_1 x_1 + w_2 x_2 = w x = w_1 x_1 + w_2 x_2$

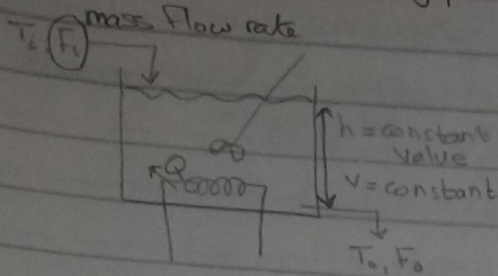
$700x = 0.4 \times 500 + 0.75 \times 200$ $\boxed{x = 0.5}$

(b) w_1 changes suddenly from 500 to 400 and remains at the new value
determine $x_1(t)$ expression & plot

Look to
Back P.19

ch. 2

2.4.1 stirred-tank heating process / Constant holdup $\rightarrow$ no mass balance is needed $F_i = F_o$



$\rightarrow$ Input: T_i, F_i, Q Disturbance: F_i

$\rightarrow$ Output: T_o, F_o Manipulated: T_i OR Q
Controlled variable: T_o Feedforward control: Feed backward

But here $F_i = F_o = w$

$\rightarrow$ Process Parameters: ρ, C_p, V

$\rightarrow$ Energy balance

$$\frac{dU_{\text{internal}}}{dt} = -\Delta(H\dot{W}) + Q$$

- assuming $U = H = W\hat{H} = \rho V C_p (T - T_{\text{ref}})$ & assuming C_p & ρ Temp. independent
- $-(\Delta W\hat{H}) = H_{\text{in}} - H_{\text{out}} = w C_p (T_i - T_{\text{ref}} - T_{\text{ref}} + T_o) = w C_p (T_o - T_i)$
- $\dot{H} = \rho V C_p \frac{dT}{dt}$

$$\Rightarrow \rho V C_p \frac{dT}{dt} = w C_p (T_o - T_i) + Q$$

Note
 $\frac{H_{\text{out}} - H_{\text{in}}}{\rho V C_p} = C_p (T - T_{\text{ref}})$
 $\hat{H}_{\text{ref. assumed}} = \text{Zero}$

DoF = 5 - 1 - 1 = 3 The process is under specified.

3 variables must be specified: T_i, F_i, T_o

2.4.2 Stirred tank heated process / Variable hold up

Process variables

Inputs: T_i, F_i, Q

$\rightarrow$ disturbance variables

$\rightarrow$ manipulated variable: Q OR T_i OR F_i

Outputs: T_o, F_o, h

$\rightarrow$ controlled variable: h OR T_o OR F_o

F_o, h & analysis, design

Process parameters: ρ, C_p assumed to be temp. independent

$\rightarrow$ Mass balance

$$\frac{dV}{dt} = F_i - F_o \quad \text{Definition (it differs in chain rule)} \quad \frac{dV}{dt} = \frac{1}{\rho} (F_i - F_o) \quad (1)$$

$\rightarrow$ Energy balance

$$\rho C_p \frac{d(VT - T_{\text{ref}})}{dt} = F_i C_p (T_i - T_{\text{ref}}) - F_o C_p (T_o - T_{\text{ref}}) + Q$$

$$\rho C_p \left(V \frac{dT}{dt} + T \frac{dV}{dt} \right) = \rho C_p \left(V \frac{dT}{dt} + \frac{1}{\rho} (F_i - F_o) \right) + Q$$

$$S C_p \left(v \frac{dT}{dt} + (T - T_{ref}) (F_i - F_o) \right) = F_i C_p (T_i - T_{ref.}) - F_o C_p (T_o - T_{ref.}) + Q$$

$$S C_p v \frac{dT}{dt} + C_p (T - T_{ref.}) (F_i - F_o) = F_i C_p (T_i - T_{ref.}) - F_o C_p (T_o - T_{ref.}) + \frac{Q}{C_p}$$

$$S v \frac{dT}{dt} = \underline{F_i T_i} - \underline{F_i T_{ref.}} - \underline{F_o T_o} + \underline{F_o T_{ref.}} - \underline{F_i T} + \underline{F_i T_{ref.}} + \underline{F_o T} - \underline{F_o T_{ref.}} + \frac{Q}{C_p} \quad \text{in book}$$

$$\frac{dT}{dt} = \frac{F_i}{S v} (T_i - T_o) + \frac{Q}{S v C_p} \quad (2)$$

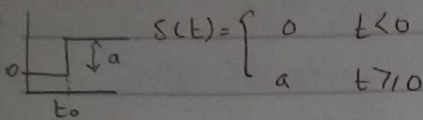
Chapter #3 & Laplace Transforms + Ch. #4 : Transfer Function models

• $F(s) = \mathcal{L} F(t) = \int_0^{\infty} F(t) e^{-st} dt$

• Constant Function $F(t) = a$

$$\mathcal{L} F(t) = \int_0^{\infty} a e^{-st} dt = -\frac{a}{s} e^{-st} \Big|_0^{\infty} = \boxed{\frac{a}{s}}$$

• Step Function



$$\mathcal{L} s(t) = \boxed{\frac{a}{s}}$$

(initial time, time zero, zero time)

• Derivative

$$F(s) = \mathcal{L} \left(\frac{dF}{dt} \right) = \int_0^{\infty} \left(\frac{dF}{dt} \right) e^{-st} dt = \boxed{sF(s) - F(0)}$$

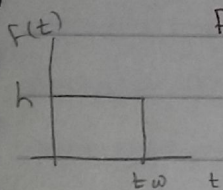
Generally

$$\mathcal{L} \left(\frac{d^n F}{dt^n} \right) = s^n F(s) - s^{n-1} F(0) - s^{n-2} F'(0) - \dots - s F^{(n-2)}(0) - F^{(n-1)}(0)$$

$$\mathcal{L} \left(\frac{d^2 F}{dt^2} \right) = s^2 F(s) - s F(0) - F'(0)$$

$$\mathcal{L} \left(\frac{d^3 F}{dt^3} \right) = s^3 F(s) - s^2 F(0) - s F'(0) - F''(0)$$

• Rectangular pulse function

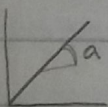


$$F(t) = \begin{cases} 0 & t < 0 \\ h & 0 \leq t \leq tw \\ 0 & t > tw \end{cases}$$

$$\mathcal{L} F(t) = \int_0^{\infty} h e^{-st} dt = \int_0^{tw} h e^{-st} dt =$$

$$\boxed{\frac{h}{s} (1 - e^{-tw s})}$$

• Ramp Function



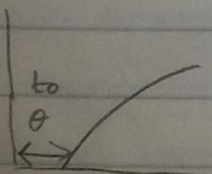
$$f(t) = at \quad F(s) = \mathcal{L} f(t) = \int_0^{\infty} at e^{-st} dt = \boxed{\frac{a}{s^2}}$$

• Transformation of integral

$$\mathcal{L} \left(\int_0^t F(t^*) dt^* \right) = \boxed{\frac{1}{s} F(s)}$$

• Time delay ($\theta \equiv t_0$)

$$F_d(t) = F(t - t_0) \quad \text{step function change}$$



$$Y(s) = \mathcal{L} F_d(t) = \mathcal{L} F(t - t_0) s(t - t_0) = \boxed{e^{-st_0} F(s)}$$

- Final value theorem

$$\rightarrow y(t)_{\infty} = \lim_{t \rightarrow \infty} y(t) = \lim_{s \rightarrow 0} (sY(s))$$

- initial value theorem

$$\rightarrow y(t)_0 = \lim_{t \rightarrow 0} y(t) = \lim_{s \rightarrow \infty} (sY(s))$$

Chapter # 5: Dynamic behavior of a first order and second order processes

5.1 2. ramp input

$$Q(t) = 8000 + 2000 s(t)$$

$$Q'(t) = 2000 \text{ st} \quad \xrightarrow{\text{Transformed}} \quad u_s(s) = \frac{M}{s}$$

5.2 Response of first order processes

$$G(s) = \frac{Y(s) \leftarrow \text{output}}{X(s) \leftarrow \text{input}} = \frac{K}{\tau s + 1}$$

K : process gain

τ : time constant

⇒ Derivation of the above equation.

general formula $a_0 \frac{dy'(t)}{dt} + a_1 y'(t) = b x'(t) \quad \div a_1$

$$\frac{a_0}{a_1} \frac{dy'(t)}{dt} + y'(t) = \frac{b}{a_1} x'(t) \quad \text{Take Laplace Transformation}$$

$$\frac{a_0}{a_1} (s Y(s) + y(0)) + Y(s) = \frac{b}{a_1} X(s) \quad \text{Zero} \quad \frac{a_0}{a_1} s Y(s) + Y(s) = \frac{b}{a_1} X(s)$$

$$Y(s) \left(\frac{s a_0}{a_1} + 1 \right) = \frac{b}{a_1} X(s)$$

$$\frac{Y(s)}{X(s)} = G(s) = \frac{b/a_1}{s(\frac{a_0}{a_1}) + 1} = \boxed{\frac{K}{\tau s + 1}} \quad \# \begin{matrix} K \\ \tau \end{matrix} \quad \text{①}$$

↳ For step function change in input &

$$X(s) = \frac{M}{s}$$

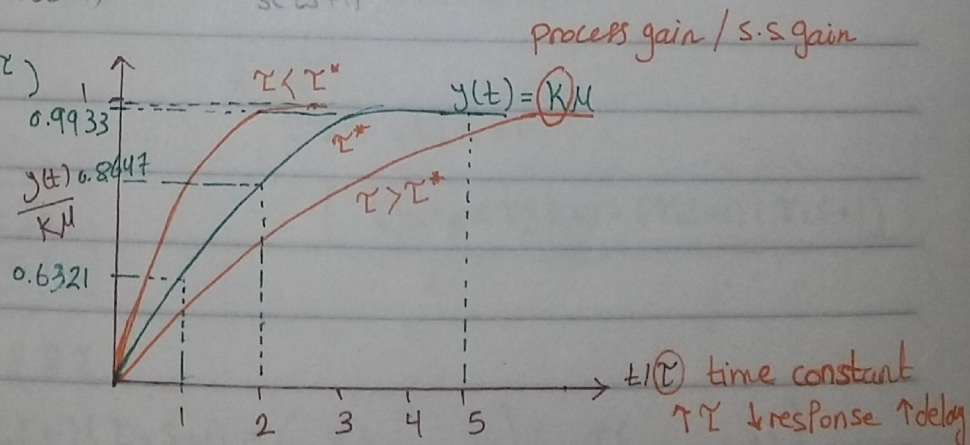
substitute in ① $Y(s) = G(s)X(s)$

$$Y(s) = \left(\frac{K}{\tau s + 1} \right) \cdot \frac{M}{s} = \frac{KM}{s(\tau s + 1)}$$

in order to see the output response $\rightarrow y(t)$

$$y(t) = \mathcal{L}^{-1} Y(s) = \mathcal{L}^{-1} \frac{KM}{s(\tau s + 1)} = KM \mathcal{L}^{-1} \frac{1}{s(\tau s + 1)} = KM (1 - e^{-t/\tau})$$

$$y(t) = KM (1 - e^{-t/\tau})$$



5.4 Response of second order processes

From 2nd order differential equation

$$a_0 \frac{d^2 y(t)}{dt^2} + a_1 \frac{dy(t)}{dt} + a_2 y(t) = b x(t) \quad \text{Divide by } a_2$$

$$\frac{a_0}{a_2} \frac{d^2 y(t)}{dt^2} + \frac{a_1}{a_2} \frac{dy(t)}{dt} + y(t) = \frac{b}{a_2} x(t) \quad \text{Take Laplace Transformation}$$

$$\frac{a_0}{a_2} (s^2 y(s) - sy'(0) - y(0)) + \frac{a_1}{a_2} (sy(s) - y'(0)) + y(s) = \frac{b}{a_2} X(s) \quad \text{cancelling zeros}$$

$$\frac{a_0}{a_2} s^2 y(s) + \frac{a_1}{a_2} sy(s) + y(s) = \frac{b}{a_2} X(s) \quad y(s) \left(\frac{a_0}{a_2} s^2 + \frac{a_1}{a_2} s + 1 \right) = \frac{b}{a_2} X(s)$$

$$\rightarrow \frac{y(s)}{X(s)} = \frac{b/a_2}{\frac{a_0}{a_2} s^2 + \frac{a_1}{a_2} s + 1} = \frac{K}{\tau^2 s^2 + 2\zeta\tau s + 1} \quad \text{Originally, but it can be as a 2 First order systems in series.}$$

→ For input as a step function $X(s) = M/s$

$$Y(s) = \frac{MK}{s(\tau^2 s^2 + 2\zeta\tau s + 1)}$$

• apply final value theorem

$$\lim_{t \rightarrow \infty} y(t) = \lim_{s \rightarrow 0} sy(s) = \lim_{s \rightarrow 0} \frac{MK}{\tau^2 s^2 + 2\zeta\tau s + 1} = MK \quad (\text{same as 1st order}).$$

→ Derivation For 2 first order system in series → It can't be underdamped

$$X(s) \rightarrow \left[\frac{K_1}{\tau_1 s + 1} \right] Y_1(s) \rightarrow \left[\frac{K_2}{\tau_2 s + 1} \right] Y_2(s) \rightarrow \text{relation between } Y_2 \text{ \& } X \text{ is needed}$$

$$G(s) = G_1(s) G_2(s) = \frac{K_1}{(\tau_1 s + 1)} \cdot \frac{K_2}{(\tau_2 s + 1)} = \frac{K_1 K_2}{\tau_1 \tau_2 s^2 + s(\tau_1 + \tau_2) + 1} \quad \text{compare with 1}$$

$$K = K_1 K_2$$

$$\tau^2 = \tau_1 \tau_2 \rightarrow \tau = \sqrt{\tau_1 \tau_2}$$

$$2\zeta\tau = \tau_1 + \tau_2 \rightarrow \zeta = \frac{\tau_1 + \tau_2}{2\sqrt{\tau_1 \tau_2}}$$

$$= \frac{K}{\tau^2 s^2 + 2\zeta\tau s + 1}$$

$$\tau^2 s^2 + 2\zeta\tau s + 1 = (\tau_1 s + 1)(\tau_2 s + 1)$$

• OR τ_1, τ_2 in terms of ζ & τ

$$\tau^2 s^2 + 2\zeta\tau s + 1 = (\tau_1 s + 1)(\tau_2 s + 1) = \left(\frac{\tau s}{2 - \sqrt{\zeta^2 - 1}} + 1 \right) \left(\frac{\tau s}{2 + \sqrt{\zeta^2 - 1}} + 1 \right)$$

$$\tau_1 = \frac{\tau}{1 - \sqrt{\zeta^2 - 1}}$$

$$\tau_2 = \frac{\tau}{1 + \sqrt{\zeta^2 - 1}}$$

$$\zeta^2 \gg 1$$

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$$\tau_{1,2} = \frac{-2\zeta\tau \pm \sqrt{4\zeta^2\tau^2 - 4\tau^2}}{2\tau^2}$$

$$= \frac{-2\zeta\tau \pm 2\tau\sqrt{\zeta^2 - 1}}{2\tau^2}$$

$$= \frac{-\zeta \pm \sqrt{\zeta^2 - 1}}{\tau}$$

$$= \frac{-\zeta - \sqrt{\zeta^2 - 1}}{\tau} \rightarrow \frac{-\zeta + \sqrt{\zeta^2 - 1}}{\tau}$$

→ Cases for ξ 2nd order systems

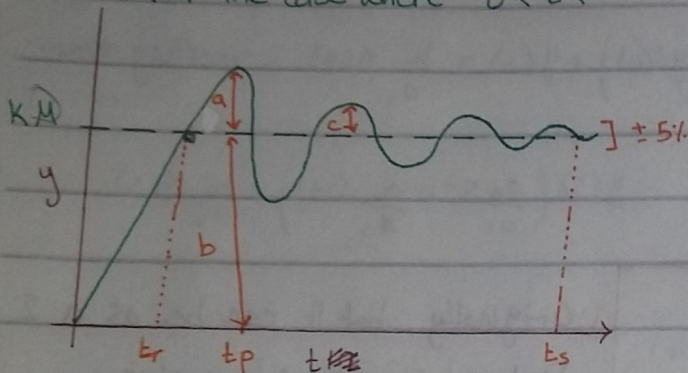
$\xi > 1$ overdamped
 $\xi = 1$ critically damped
 $0 < \xi < 1$ underdamped

2 distinct roots
 2 similar roots
 complex roots

if $\xi < 0$ it will be an unstable system that will respond to any input. have unbounded

$$y(t) = KM(1 - e^{-\xi t/\tau} \left[\cos\left(\frac{\sqrt{1-\xi^2}}{\tau} t\right) + \frac{\xi}{\sqrt{1-\xi^2}} \sin\left(\frac{\sqrt{1-\xi^2}}{\tau} t\right) \right])$$

→ For the case where $0 < \xi < 1$ →



1. Rise Time $y(t) = KM$ First time

2. Time to First peak
 Derivative
 substitute as a

$$t_p = \frac{\pi\tau}{\sqrt{1-\xi^2}}$$

3. Settling time t_s

4. overshoot $OS = \frac{a}{b} = \exp\left(\frac{-\pi\xi}{\sqrt{1-\xi^2}}\right)$

5. Decay ratio $DR = \frac{c}{a} = OS^2 = \exp\left(\frac{-2\pi\xi}{\sqrt{1-\xi^2}}\right)$

6. Period of oscillation $P = \frac{2\pi\tau}{\sqrt{1-\xi^2}}$

Disadvantage: all set appears.
 Advantage: fast response

Chapter #8 : Feedback controllers + Chapter #11

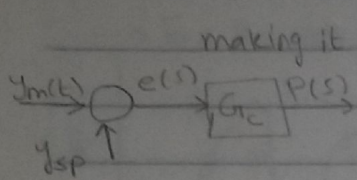
① Proportional controller

- objective is to reduce the error signal to zero
- Controller output: $P(t) = \bar{P} + e(t) K_c$

$$e(t) = \overset{\text{mostly constant}}{y_{sp}(t)} - y_m(t)$$

in order preventing "self destructive"

not $e'(t)$ because $e'(t) = e(t) - 0$



making it in the deviation form

Taking Laplace

Transfer Function

$$P'(t) = e(t) K_c$$

$$P'(s) = K_c e(s)$$

$$G_c(s) = \frac{P'(s)}{e(s)} = K_c$$

Derivation of $P(s)$: $\mathcal{L}\{P'(t)\} = \mathcal{L}\{e(t) K_c\} = \int_0^\infty K_c e(t) e^{-st} dt$
 $= K_c e(s)$

② Proportional integral controller

Proportional form
 slower than integral form.
 but eliminate offset
 However, make oscillation

$$P'(t) = K_c e(t) \quad (I)$$

$$P'(t) = \frac{1}{T_i} \int_0^t e(t^*) dt^* \quad (P)$$

* combine (I) & (P)

$$P'(t) = K_c \left(e(t) + \frac{1}{T_i} \int_0^t e(t^*) dt^* \right)$$

→ Taking Laplace $\mathcal{L}\{P'(t)\} = \mathcal{L}\left\{K_c \left(e(t) + \frac{1}{T_i} \int_0^t e(t^*) dt^* \right)\right\}$

$$P'(s) = K_c \left(e(s) + \frac{e(s)}{T_i s} \right)$$

→ Transfer Function $G_c = \frac{P'(s)}{e(s)} = K_c \left(1 + \frac{1}{T_i s} \right) = K_c \left(\frac{T_i s + 1}{T_i s} \right)$

Advantage: offset elimination

Disadvantage: oscillating

reduces the stability of Feedback control system

Parallel type

③ Proportional - integral - derivative controller

anticipate the future behaviour of error signal

by considering its rate of change → stabilize control process (counteract integral mode destabilizing) & improve dynamic response by settling time

However, not good for noisy signals (sensitive), it will contain high frequency, random fluctuation

solution → Filtered term $\frac{1}{\lambda T_D s + 1}$ $\lambda \rightarrow 0.05 - 0.2$ (0.1 as common choice)

combine for PID $P'(t) = K_c \left(e(t) + \frac{1}{\tau_I} \int_0^t e(t') dt' + \tau_D \frac{de(t)}{dt} \right)$

Laplace $P'(s) = K_c \left(e(s) + \frac{1}{\tau_I s} e(s) + \tau_D (s e(s) - \dot{e}(0)) \right)$

$P'(s) = K_c \left(e(s) + \frac{1}{\tau_I s} e(s) + s \tau_D e(s) \right)$

Transfer $G_c(s) = \frac{P'(s)}{e(s)} = K_c \left(1 + \frac{1}{\tau_I s} + \tau_D s \right)$ PID without derivative filter

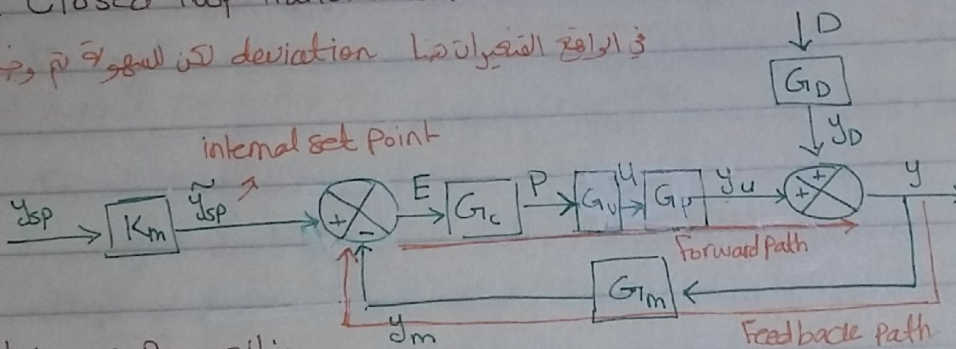
Now, to reduce sensitivity of control calculations to noisy measurement add filter term

$G_c(s) = K_c \left(1 + \frac{1}{\tau_I s} + \frac{\tau_D s}{2\tau_D s + 1} \right)$ PID with derivative filter

8.3.2 Reverse or direct action

11.2 Closed loop transfer function (To understand all set meaning) with out current to pressure transmitter

في الواقع القياس deviation في الواقع القياس



D & ysp independent

* Applying superposition

① Assuming $D=0$ (no change in D) $\Rightarrow y/y_{sp}$ "set point changes" "servomechanism"

$y = y_D + y_u$ but $D=0$ $y_D=0 \Rightarrow y=y_u$

$y_u = u G_P = P G_V G_P = E G_C G_V G_P = (y_{sp} - y_m) G_C G_V G_P$

$y = y_u = (y_{sp} K_m - y G_m) G_C G_V G_P$

$y (1 + G_m G_C G_V G_P) = y_{sp} K_m G_C G_V G_P$

② Assuming $y_{sp}=0$ (no change in y_{sp}) $\Rightarrow y/D$ "disturbance changes"

$y = y_D + y_u = D G_D + E G_C G_V G_P = D G_D + (y_{sp} - y_m) G_C G_V G_P$

$y = D G_D + y G_m G_C G_V G_P$

$\frac{y}{D} = \frac{G_D}{1 + G_m G_C G_V G_P} = \frac{G_D}{1 + G_{OL}}$ (2)

Forward $\frac{y}{y_{sp}} = \frac{K_m G_C G_V G_P}{1 + G_m G_C G_V G_P}$
Forward + Feedback $\equiv G_{OL}$
OL: open loop

Now, add ①+② in terms of y

$y = \frac{K_m G_C G_V G_P}{1 + G_m G_C G_V G_P} y_{sp} + \frac{G_D}{1 + G_m G_C G_V G_P} D$



11.3.1 Proportional control and set-point changes

$$E = \text{offset} = y_{\text{set point}} - y_{\infty}(t)$$

if it is constant, if not take $\tilde{y}_{sp}(t)$

analog → digital → Interface → controlled variable measurement
manipulated variable adjustment
transmission instruments

CHAPTER #9: Control system instrumentation

9.1 | 9.1.1

Sensor, transmitter, transducer

between sensor & controller

Just to controller

any conversion between any system component e.g. between controller and final control element.

Standards

3-15 psig

4-20 mA

1-5 V (VDC) direct current

→ 9.1.2 Sensors

Selection criteria

→ 9.1.3 Static and dynamic characteristic

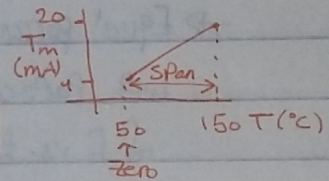
transmitters are generally designed to be direct acting

adjustable input range.

zero & span of the overall sensor / transmitter are adjustable.

if sensor power supply fails → 0 mA → controller & actuator to min. or max → if unsafe inverted to give highest value in the operating range.

For any linear instrument $K_m = \frac{\text{Output span range}}{\text{measurement range}}$
does not change if zero is changed



For non linear instrument :

tangent @ operating point of the characteristic equation

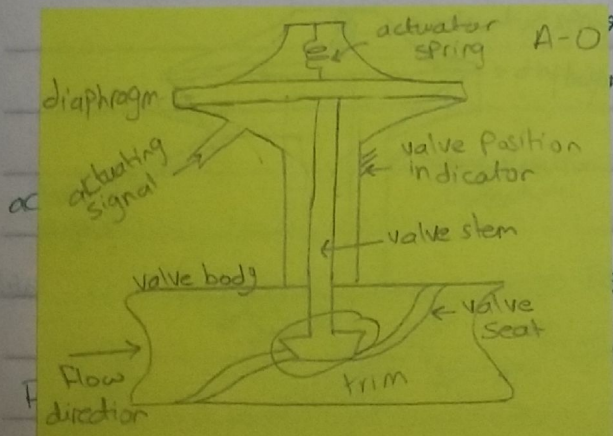
Maybe dynamics of first order " (results an error between the true and measured value) "

$$\frac{Y_m(s)}{Y(s)} = \frac{K_m}{\tau_m s + 1} \quad [K_m] = \text{mA}/^\circ\text{C if Temp.} \quad \text{"monotonic response"}$$

As a result of velocity - distance lag because of → poor sensor location
long sampling line

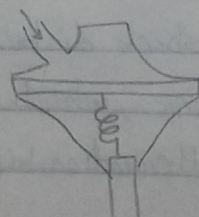
→ 9.2 Final Control elements

→ 9.2.1 Control valves

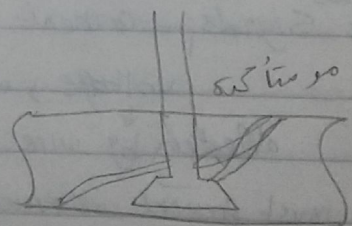


rising stem valve

A-C, reventing



OR



You can find relation function
between T_m & T

From the line

$$\textcircled{m} = \frac{T_m - T_{m_0}}{T - T_0} \quad T_m = m(T - T_0) + T_{m_0}$$

$= K_m$

$$T_m = \left(\frac{20 - 4}{150 - 50} \right) (T - 50) + 4$$

$$\begin{aligned} T_m &= 0.16(T - 50) + 4 \\ &= 0.16T - 4 \end{aligned}$$

→ 9.2.2 Valve positioners

- Just for pneumatic control valves.
- It eliminates valve dead band and hysteresis, Flow rate loading, ---

→ 9.2.3 Specifying and sizing control valves

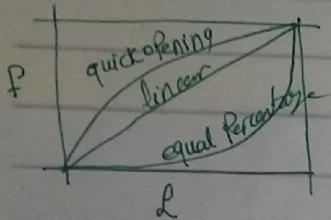
$$Q = C_v F(l) \sqrt{\frac{\Delta P_v}{\rho}}$$

valve size depends on F

depends on valve size or capacity

valve characteristics F , l : lift (extent of valve opening)

- For constant pressure drop across the valve, F is related to lift (l) by one of the following relations



linear ($F = l$)

$0 \leq F \leq 1$ $0 \leq l \leq 1$

quick opening ($F = \sqrt{l}$) "square root valve"

Equal percentage ($F = R^{l-1}$) R is a number

R is a valve design parameter 20 → 50

percentage

- Equal percentage valve is named like this because of equal change of F with particular change with l anywhere in the range. Because of slope of F vs. l (dF/dl) is proportional to F .

- Rangeability of control valve: ratio of max. to min. input signal

Imp. why I have to choose certain value from the chart?

The designer's objective is to obtain an installed valve characteristics that is as linear as possible that is, to have flow through the valve and all connected process units vary linearly with l .

Choose linear valve

if pump characteristics is flat and small friction loss

→ 9.3 Signal transmission and digital communication.

Electronic Digital Signals — current

voltage; when short distances are involved

affected by wire resistance, which affects the wire length, Temp., aging.

- You must prevent ~~attenuation~~ attenuation, biasing, or inducting noise → shielded coaxial cable